

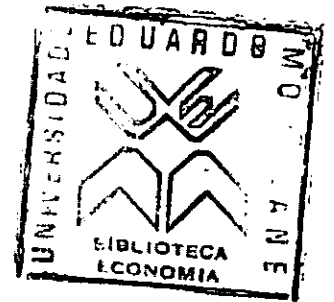
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A CRITIQUE OF PRICE THEORY WITH SPECIAL REFERENCE TO
DECENTRALIZED EXCHANGE

by

Manuel Luís Guimarães da Costa



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Robert A. Lott

Director of Dissertation

Ronald P. Winkler

Committee Member

C. E. Reeder

Committee Member

J. H. Clifton

Committee Member

Dean of the Graduate School

ABSTRACT

A Critique of Price Theory with Special Reference to Decentralized Exchange

Manuel Luís Guimarães da Costa

Progress in the theory of exchange has been conceived as a refinement of equilibrium states, and the question of existence of equilibrium as a set of prices at which purely notional trading plans are consistent has been confused with the different question of how plans based on notionally predetermined equilibrium prices can actually be carried out. Along the way, formal theory has been emptied of concern with potentially observable activities of transactors; and theoretical accounts of markets and exchange arrangements have been emptied of empirical content. The questions I raise are, first, how the neowalrasian approach evolved and led to the omission of trading and markets, and second, how it constrained understanding of the execution of trades.

The argument in this dissertation is as follows. In Chapter II, it is shown that the program set forth by Walras of providing an explanation for the convergence to equilibrium in competitive exchange is still today an unresolved question. Walras was unable to carry forward to the general model his view of the workings of free competition in markets where bargaining and trading take place in the course of the adjustment process. But if Walras settled matters upon the assumption of no-arbitrage, the neowalrasian formalization entirely lost sight of trading and pursued tâtonnement as if it described real adjustment in a competitive economy.

Chapter III begins with a comparison of adjustments to equilibrium in Walras and Marshall, to conclude that both authors are basically in agreement, and that the separation to be established is with Arrow-Debreu. Next, a line of evolution in price theory from Marshall to Chamberlin and on to Triffin is described; when the general equilibrium edifice was topped by the proofs of existence (and stability) by Arrow-Debreu in the fifties, the Marshallian tradition in price theory had become engulfed in a purification by means of which general interdependence does without markets.

Decentralized trading arrangements become thereby an oversight in theoretical analysis and this is why Chapter IV opens with a discussion of whether a theory of markets and intermediation is available, and how the consideration of transaction costs by Coase sidestepped the issue. Moreover, transaction costs have both been called to explain the emergence and the impediment to the formation of markets. 'Markets' are a misnomer for 'prices' in the theory of general

interdependence, and an unnoticed confusion between exchange and markets ensues.

A broad distinction between brokered and non-brokered markets is attempted and, next, decentralization is characterized in its dimensions, which regard information, the determination of the price signal, and logistics. In this perspective the Arrow-Debreu model of general exchange fails in all three aspects: first, because convergence is not computable; second, because for consistency of trading plans exchange rates are required to be common, given, and freely known; third, because only with centrally coordinated multilateral barter can the theory preclude bargaining by traders in attempts to transform planned trades into feasible executions.

The consistency of informationally decentralized trading with predetermined equilibrium prices has often been questioned (e.g. Ostroy and Starr [1990]), and analyses of execution have been attempted with unsatisfactory results. Direct barter at equilibrium prices hardly meets full execution under decentralized information, i.e., it is not feasible. The introduction of intermediation or a medium of exchange (monetary exchange being a special case of indirect barter, and one of central interest here because it is potentially decentralized) is shown to enable feasibility of execution. In spite of hardly fitting a world of costless exchange, the consideration of these facilitating devices helps expose the contradictions carried by attempts to dichotomize pricing and trading.

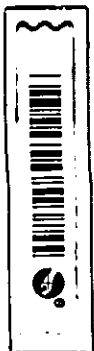
Given these negative findings, the doubt arises whether and how the Walrasian program can be furthered to include and treat logistics of exchange. Were we to stay within the Walrasian program, two possible solutions are discussed, but both face obstacles. One approach is to formalize trading in the process of bargaining, but the consideration of feasibility of decentralized execution raises doubts about the adequacy of the established notion of equilibrium (as a notional state) as a basis for understanding trading. The other possible approach is to start with logistics of transactions in an informationally decentralized setting, without postulating equilibrium prices as preexistent to trade.

Finally, Chapter V offers concluding comments on Arrow's [1959] contribution to the theory of price adjustment that reinforce my earlier arguments showing that existing theories of price and quantity adjustment which attempt to dispense with "the auctioneer" have been unsuccessful in defining alternative theoretical trading schemes that would satisfactorily describe trading phenomena in the decentralized non-brokered markets that are a ubiquitous feature of every modern economy.

Dissertation Director: Dr. Robert W. Clower

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CHAPTER I

INTRODUCTION

This is an exercise in criticism and it should be made clear at the outset that no more than that is intended. That something is wrong with the neowalrasian¹ general equilibrium approach as an explanation of the working of markets and as a basis for applied economics is common knowledge in the profession. But to assess what and how it came to be so, it has been necessary to conduct a careful review of the literature to uncover anomalies and gaps that previous writers may have overlooked or ignored.

My main result is simple. Progress in the theory of exchange has been conceived as a refinement of equilibrium dispositions, and that conception has been elevated into a concern with little else than the virtual (never actual) consistency of the trading dispositions (mental states) of hypothesized "transactors". Along the way, formal theory has been emptied of concern with potentially observable activities of transactors; and theoretical accounts of markets and exchange arrangements have been emptied of empirical content.

None of this is new; as [Hahn, 1970, 1] observed more than a quarter of a

¹In referring to neowalrasian, instead of the usual "neo-Walrasian", I follow Clower [1994d, fn.2]. Given that the links to the original model where the neowalrasian approach departed from (Walras' and Pareto's numéraire model) are lost, "...the word "neowalrasian" functions as an impersonal noun, not an adjective, and I forego capitalization accordingly."

century ago: "The achievements of economic theory in the last two decades are both impressive and in many ways beautiful. But it cannot be denied that there is something scandalous in the spectacle of so many people refining the analyses of economic states which they give no reason to suppose will ever, or have ever, come about." The focus on the so-called "problem of existence of a competitive equilibrium" is one such manifestation. It is an inconsequential exercise since the methods of proof bear no interpretation as any economic mechanism. Other intellectual puzzles created by the existence problem vastly outweigh the purely mathematical problem that was its source. Specifically, the existence problem has diverted attention away from such crucial economic issues as stability of real-time adjustment processes and real-time logistics of exchange. In effect, the existence of equilibrium as a set of prices at which purely notional trading plans are consistent has been confused with the different question of how plans based on notionally predetermined equilibrium prices can actually be carried out.

Nearly three decades have passed since Hahn's words were spoken, and in that time general equilibrium analysis seems to have developed into a sterile logical exercise. It has been perfected to the point where the question no longer is so much its alienation from empirical facts as its blind concentration on problems posed by purely logical concerns. The ascendancy of "existence" in general equilibrium theory has already been emphasized, but this kind of confusion of a mathematical with an empirical economic question extends much further, for instance, to the question of parametric pricing in supposedly "competitive" conditions. Somehow the notion that "perfect competition" describes a situation where transactors not only believe they don't, but in fact do not have any effect on price has become common, and so "competitive behavior" has been defined as the rule that individual traders adhere to passive price-taking. It has been

suggested² that interdependence creates a strategic, or incentive compatibility problem that is inconsistent with so-called "competitive behavior." In order to preserve parametric pricing, 'continuum' economies replace 'finite' economies: infinitesimal 'individuals' are randomly paired up to bargain and trade; furthermore, the question is raised whether for such a large economy a 'continuum' of commodities compromises competitive behavior. This is probably one of the extremes of unreasonableness to which the Arrow-Debreu approach has come. But my concern in this dissertation is with older "unsettled questions". I am interested in confronting the Walrasian program with its neowalrasian diversion (where such riddles arise more naturally). The questions I raise are, first, how the neowalrasian paradigm evolved and led to the omission of trading and markets, and second, how it constrained understanding of the execution of trades.

Walras was concerned with the workings of markets, though he abstracted from complications and focused on "...a hypothetical régime of absolute free competition" [Jaffé, ed., 1954, 40] in his exposition of equilibrium as a state of maximum satisfaction in exchange; and his theory of tâtonnement was meant to be "...the demonstration of the attainment of that equilibrium through the play of the raising and the lowering of prices until the equality of the supply and demand quantities are established" [Walras, 1895, 630; in Walker, 1987c, 159-60]. In short, the Walrasian program consists in describing how the mechanism of free competition "...among sellers of services who underbid one another and among buyers of products who outbid one another" [Jaffé, ed., 1954, 40n] leads to the generation of a set of equilibrium prices in general exchange.

²Cf. e.g. Aumann [1964] and Hurwicz [1972]. For a list of references on the subject, specifically on the question of how perfect competition can be distinguished from the existence of Walrasian equilibrium, see Ostroy and Zame [1994, 594]. When referring to continuum economies, beyond the latter I have also in mind another strand of literature that led to McLennan and Sonnenschein [1991].

The neowalrasian reinterpretation, though intendedly portraying a description of relevant features of the real world, concentrates on the question of existence of equilibrium as 'coherence' of trading plans. Decentralized interaction between individuals, bargaining and transactions are sidetracked and replaced by a notional state whereby equilibrium prices are exogenously determined and given, and exchange can only be supported by multilateral barter with the central 'market.' Hence, the neowalrasian diversion.

Given these general considerations, the argument in this thesis is as follows. In Chapter II, it is shown that the program set forth by Walras of providing an explanation for the convergence to equilibrium in competitive exchange is still today an unresolved question. Walras was unable to carry forward to the general model his view of the workings of free competition in markets where bargaining and trading take place in the course of the adjustment process. But if Walras settled matters upon the assumption of no-arbitrage, the neowalrasian formalization entirely lost sight of trading and pursued *tâtonnement* as if it described real adjustment in a competitive economy.

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CHAPTER II

WALRAS' PROGRAM AND THE NEOWALRASIAN DIVERSION

Walras tells us at the end of the purely theoretical portion on his *Éléments*, that his object has been to present a "scientific formulation of pure economics," and for that purpose "...it did not matter whether or not we observed [free competition] in the real world since, strictly speaking, it was sufficient that we should be able to form a conception of it" [Jaffé, ed., 1954, 255; cf.157]; and he adds (p.256) "...we never attempted to predict decisions made under conditions of perfect freedom; we have only tried to express the effects of such decisions in terms of mathematics."

In an earlier chapter (Lesson 5, 83) of the *Éléments*, Walras observes: "Value in exchange, when left to itself, arises spontaneously in the market as a result of competition. [...] The more perfectly¹ competition functions, the more rigorous is the manner of arriving at value in exchange." Continuing, he describes three kinds of markets, according to how well competition works:

(i) The best organized markets are those in which selling and buying are made by auction, ("à la criée," i.e., by being cried out) through the intermediation of agents such

¹"Selon que cette concurrence fonctionne plus ou moins bien..." [Walras, 1926, 70]. We should beware of the intrusion of 'perfection' with its later connotations (see, for instance, Schumpeter [1954, 1026n]).

as brokers, commercial agents, or criers who centralize purchase and sale offers in such a way that no exchange takes place without its conditions being announced and known, and without the sellers being able to lower the price and the buyers to raise it; as examples, stock exchanges and organized commodity markets (the markets for grain, fish, etc.).

(ii) There are other markets (Walras mentions the fruit, vegetable and poultry markets) that are less well organized, but still function in a fairly effective and satisfactory way.

(iii) Third, markets where competition appears to be "somewhat defective," but that nevertheless operate remarkably well: city streets where an abundance of stores and shops can be found - baker's, butcher's, grocer's, tailor's, shoemaker's, etc.

More broadly, Walras asserts that

... the whole world may be looked upon as a vast general market made up of diverse special markets where social wealth is bought and sold. Our task is to recognize the laws to which these purchases and sales tend themselves to conform. To this end, we shall suppose that the market is *perfectly organized in regard to competition*, just as in pure mechanics we suppose, *to start with*, that machines are frictionless. (Jaffé, ed. [1954, 84], with adaptations from the French edition, italics added)

In fact, "[p]ure political economy is essentially the theory of the determination of prices under a hypothetical régime of absolute free competition" [op.cit., 40], by which Walras means competition "...among sellers of services who underbid one another and among buyers of products who outbid one another." (Jaffé, ed. [1954, 40n]; see also pp. 83, 223-4, 255, 478). Here we have undeniably a depiction of the freedom of

individuals to offer "bid" prices or set "ask" prices, at will.²

Since we are here concerned with what was to become the enduring Walrasian legacy, the neowalrasian approach to general equilibrium analysis, we will be concerned, for the moment, only with the general model. In building his theoretical apparatus, Walras proceeds by steps, constructing, sequentially and cumulatively, theories of exchange, of production, of capital formation and credit, and finally of circulation and money. Exchange theory comprises basically two barter models, an introductory one of exchange of two commodities for each other [Jaffé, ed., 1954, Part II], and another of exchange of several commodities for one another, the general model [Part III, especially Lesson 12], where two features are introduced, one is that each trader holds several commodities, and, the other, a numéraire. As an attempt to a bridge from the first to the general model, Walras presents his arbitrage model, which is developed in three sketchy steps. First, the case of exchange of three commodities [§ 105-7]. Next, the case of "trading posts" exchange with m commodities and $(m(m-1)/2)$ "special markets," where the prices of commodities are taken two at a time [§ 108-13]. And, finally, considering the possibility of an imperfect equilibrium in trading posts exchange, Walras introduces indirect barter ("arbitrage" [§ 114-6]), also with m commodities and with each trader holding initially only one commodity. (For a detailed characterization of Walras' barter exchange models, see Walker [1993].)

²This is not a feature of modern "competitive" models (e.g., Arrow and Hahn [1971]). As Stigler [1957] shows, long historical survival can be adduced as evidence of the ubiquity and viability of competition in "city streets". The same cannot be said of "organized" commodity exchanges [Cassady, 1967, Ch.3].

Walras emphasizes that the construction of his theory involves two exercises³:

(i) The first exercise is the mathematical solution to a set of equations of exchange. This is the theoretical solution to the (static) general equilibrium model, in which the calculated prices ("prix du calcul") are the equilibrium prices (Jaffé, ed. [1954, 184-5]).

(ii) The second exercise is meant to show that the mechanism of competition in the market provides a solution identical to the theoretical solution. In Walras' words [Jaffé, ed., 1954, 162-3; also 169], "[n]ow there remains only to show - and this is the essential point - that the problem of exchange for which we have just given the theoretical solution, is the selfsame problem that is in practice solved on the market by the mechanism of free competition". To prove that (p.170), "we need only show that the upward and downward movements of prices solve the system of equations of offer and demand by a process of groping [par tâtonnement]".⁴

An important shortcoming undermines the proposed second exercise. It concerns the consistency of the two solutions, the mathematical and that asserted by way of tâtonnement. This is meshed with a discussion whether tâtonnement is an exercise in dynamics or statics, and this is the only question to be addressed here because I am just concerned with Walras' proposed line of inquiry and with his struggle to make sense of it. It is a discussion about "what Walras really said" and a tentative one at best, made

³Yet the construction of each model involves four parts (cf. Walker [1987b, 854-5]): (1) the structure of the market, (2) the process by which adjustments take place when the market is in disequilibrium, (3) the conditions of equilibrium, and (4) comparative statics. Basically, the first exercise corresponds to part (3), the second to part (2).

⁴Walras' general program in regard to this second exercise is defined in the preface to the 4th edition as: "...that the mechanism of increase and decrease of prices in the market, in conjunction with the fact of shifting of entrepreneurs from enterprises showing a loss to enterprises showing a profit, is nothing but a way of resolution by groping of the equations involving these problems." [Jaffé, ed., 1954, 44]

more difficult by Walras' failure to give a clear account of the workings of any actual economy.⁵ Other shortcomings, which Walras entirely failed to envision, will be addressed later. One is the logical consistency of his theory of price adjustment in exchange; another is Walras' failure to specify information requirements that impinge upon the construction of models that are meant to deal with the workings of markets.

Conflicting interpretations have been proposed whether Walras' work on tâtonnement deals with the dynamic process by which competitive markets move towards equilibrium, or is purely static, and is not intended to describe the behavior of real markets (cf. Walker [1987a, 758-9]). This debate has been mostly settled in favor of the second interpretation. Patinkin [1965, 531-40], Jaffé [1967], and Morishima [1977, 27-45] stand out as the influential proponents of the first view, though meanwhile Jaffé became increasingly dissatisfied with his earlier interpretation (see Jaffé's [1980, 1981] in which he embraces the static view espoused by Walker [1987a]).

Walras' theory of tâtonnement in exchange is based on the workings of actual brokered markets, namely the Paris Bourse (see Walker [1990a, esp. 653: "le marché type"]; [1990b, esp. 967]). The important features being - and this is trivial for the 2-commodity case - first, that all traders are in direct communication and thus are able

⁵To Arrow, it seems clear that "...in his famous but rather clumsy theory of tâtonnement [...] Walras did not literally suppose that the markets came into equilibrium in some definite order. Rather, the story was a convenient way of showing how the market system could in fact solve the system of equilibrium relations" [Arrow, 1968, 378]. Notice that the words "convenient" and "in fact" (in Arrow's remark) do not match. But Arrow's main idea still is valid: Walras couldn't be describing the workings of the markets, yet intending to give a 'representation' of how the result obtained by the market could be achieved. But this is just what Walras himself wrote, in the context of adjustments in the production model: "We must picture to ourselves as taking place [Qu'on se représente comme s'effectuant...] simultaneously all the operations that, for the needs of the demonstration, we have had to assume taking place successively" (Jaffé, ed. [1954, 477-8]; as translated by Walker [1988, 313]).

simultaneously to learn each other's offers;⁶ second, that bargaining occurs by way of announcement by traders of offers to purchase and sell, and price bidding takes place so that at a certain price (equilibrium price) orders to buy and orders to sell are in balance; and third, that transactions occur only when market equilibrium price is obtained for the day.⁷

But after talking about arbitrage in the 3-good case, Walras lost interest in trading processes and also in processes of price adjustment that might precede it. Walras proceeds as follows. First, he raises the possibility of an imperfect equilibrium (Jaffé, ed. [1954, 157]) and considers indirect barter. Walras discusses how indirect trades will occur: for the 3-good case, he shows (pp.158-60) that a trader will not trade directly in the trading post (AC), say, if through successive indirect barter in the (AB) and (BC) trading posts, he could obtain a more favorable exchange rate: $p_{ab} \times p_{bc} > p_{ac}$. Instead, a holder of (A) demanding (C) would replace direct exchange of (A) against (C) by indirect exchange of (A) against (B), and (B) against (C), so that the "true price" (that is, the rate of exchange at which the final transactions are expected to take place) of (A)

⁶A broker knows his demand curve (which we assume is a net demand curve if the broker has carried out all matching trades between his customer-buyers and customer-sellers). This demand schedule is composed of the cumulated price-quantity orders received from individual traders. As far as supply is concerned, he only has access to the counteroffers (price-quantity points) of individual brokers he is proposing to deal with. If we presume that each individual broker-buyer (broker-seller) has full knowledge of each other prospective trader's effective supply (demand) at any given price (i.e., that he knows each individual prospective trader's demand (or supply) schedule), then we would be led to posit a trading scheme between every pair of brokers in the same manner as if the orders to buy or sell of both of them belonged in the book 'list' of orders to transact of the broker proposing the trade. We require less-than-perfect information about brokers' (or traders' in general) "effective" demands and supplies at each price in order to make sense of (and allow for) exchange. But imperfect information is a standard assumption of decentralized exchange, and there is not much to add, although it may help to make this clear: without decentralized information about other traders' willingness to trade, exchange vanishes.

⁷Notice that, in his description of the workings of the Paris Stock Exchange, Walras does not allow for trading at 'false' prices. He is led to exclude trade "...until offer equals demand" and "[a] new stationary state is thus found at a higher price": "Theoretically, trading should come to a halt", and "[t]rade stops." (Jaffé, ed. [1954, 85])

in terms of (C) will be $(p_{ab} \times p_{bc})$. If we suppose that a given trading post displays an "imperfect equilibrium", arbitrage opportunities will be sought. By way of substitution of two trades for one direct barter, the imbalance in cross exchange rates would be transmitted to any third trading post (presumably in 'partial' equilibrium), let us suppose to the two neighboring trading posts.⁸ But here Walras faces a problem: if, given posted prices, there are advantageous arbitrage opportunities among certain trading posts, there will be either no demand or no offer forthcoming at any of these trading posts. This spillover from one trading post to the next would call forth bargaining, i.e., changes of asking or bid prices, as is accounted for in the two-good case. The problem is not easy to tackle: the fact that no agent or broker can have a full picture of the market for a commodity (all the trading posts where one commodity is exchanged) prevents any simple way to formalize adjustment of exchange rates at any trading post. (As to Howitt's [1973, 490] summary assessment of a two-good one market case, as considered in Walras' description of the Paris Government Bond Market, one should not be misled into thinking that the 'short' side can be ascertained in more general cases. The problem is trivial in a two-good market (see Appendix Note C, last section). The possible confusion is related to an aspect which interpretation in Walras is not clear-cut: Walras leads us into thinking this is the case, i.e., that the 'short' side can be ascertained, which

⁸"This condition [for stable equilibrium] was first stated by Walras. Walras, however, formulated it in a way which limits its applicability to partial equilibrium analysis. Within the framework of general-equilibrium theory the stability conditions must take into account the repercussions of the change in price of a good upon the prices of other goods as well as the dependence of excess demand (or excess supply) of a good on the prices of the other goods in the system. This has been done by Professor Hicks" [Lange, 1945, 91]. But Hicks [1939/1946] only accomplished his stability proof (save for instability due to asymmetrical income effects [66, and 316-7]) through the presumption that "... p_i is adjusted so as to maintain equilibrium in the market for x_i , but all other prices are unchanged; ... p_i and p_j are similarly adjusted; and so on" [315]. Whose 'market' information for each commodity is it that allows for adjustment?

requires the possibility that each and every broker in the conduction of trading can come to realize total demand and total supply forthcoming in the market at the announced price. In the case of a set of special exchanges (trading posts), one for each pair of commodities, no 'specialized broker' will be able to gather information on the 'market' excess demand of any commodity; that is to say, brokers cannot ascertain market conditions.⁹)

Next, unable to tackle this bargaining question, in order for a "final" and "general" market equilibrium to be achieved, Walras bypasses arbitrage by assuming it is 'done' by the market impersonally ("arbitrage operations will be effected..." [Jaffé, ed., 1954, 160]) in order to "...generalize the equilibrium established for pairs of commodities in the market" [161]. In place of an explicit account of arbitrage between trading posts, Walras introduces a set of no-arbitrage conditions.¹⁰ Having postulated these conditions, Walras replaced his collection of special markets (trading posts) with a "single general market", and introduced the numéraire so that a single numéraire price is associated with each commodity, thereby introducing by assumption the highly special condition that a single rate of exchange prevails for every admissible pairwise commodity exchange, independently of the location at which it occurs or the individuals who execute it (this creates serious interpretation problems because, for example, if two different

⁹The same imperfection in the communication and assessment of market conditions extends to the possibility of non "single valued" transaction prices (cf. Osborne [1965, 112]).

¹⁰Walras' introduction of "no-arbitrage" conditions (and the numéraire) does not complete the basis upon which the edifice of general equilibrium analysis would be built later. The key element here was Pareto's introduction of a budget equation in his *Manual of Political Economy* [1909/1927, esp.160 and 412], a concept not found in Walras that was adopted apparently without serious reflection first by Slutsky [1915], and then by all later interpreters of Walras, including Allen [1932, 210,212,216], Hicks and Allen [1934], Schultz [1935, 434-6], Hicks [1939], and Samuelson [1947]. (Notice, though, Schultz's [1935, 434] recognition of the question: "These prices are assumed unaffected by the individual's trading, so that his budget always balances: he gives (supplies) in proportion to what he receives (demands), and receives in proportion to what he supplies.") For further comment, see Appendix Note A.

money prices for gasoline are observed at a single street intersection, that "fact" can be fitted to the theory only by treating gasoline at different stations as different commodities (cf. Debreu [1959, 30]), a type of intellectual contrivance that effectively insulates the theory from empirical confrontation in all conceivable cases). In effect Walras thereby eliminates by assumption the possibility of explicit discussion in subsequent argument of "competition" or "bargaining". The economics profession subsequently somehow has overlooked this savage emasculation of the intuitive concept of rivalrous competition as conceived by all earlier economists including Walras' "sainted" father Auguste Walras. The "simplification" introduced by Walras' "no-arbitrage conditions", i.e., the introduction of numéraire prices, may go a long way to explain why Marshall, Edgeworth, and other contemporaries of Walras showed so little respect for Walras' supposed "creation" of scientific economics.

In the Preface to the *Éléments* [40-41], a picture of exchange is presented for a "market" where only consumers' goods and services are bought and sold, where once the prices of all goods and services have been cried in terms of the numéraire, and quantities offered and demanded of every good having been determined in this way, new prices are cried and the process continues so that finally "...the prices will be the *current equilibrium prices* and exchange will effectively take place." But here, in the general equilibrium model, the relevant question is not as much whether it is a realistic account of the dynamics of the equilibrating process in markets (which Walras took for granted), but whether it is logically sound (on this, see #4.3). Even though we should be aware of the dissonance between Walras' attachment to understanding tâtonnement as a real procedure, and his formal account of it, an assessment of Walras' exposition of tâtonnement in general exchange may be helpful (see Jaffé, ed. [1954, 169-72]; also Jaffé

[1981, 317-21]). A formal analysis of the Walrasian tâtonnement process can be found in Uzawa [1960, 186-8], in Arrow and Hahn [1971, 305], and in Patinkin [1965, 535].

Jaffé [1981] searches through the literature on the two views, static or dynamic, and collates rather disputable evidence from discussions Walras entered into with contemporary economists, in order to defend his contention that Walras intended his theory of tâtonnement to be understood as a virtual and mechanical solution, adhered to for analytical convenience.¹¹

Walker [1987a, 762-5] convincingly dismisses Jaffé's interpretation. He defends the opposite view that Walras - at least by the time of the third edition (1896) of the *Éléments* had not surrendered his conviction that he was describing an empirical solution on the market under the regime of free competition; and that tâtonnement in exchange demonstrates "...the attainment of ... equilibrium through the play of the raising and lowering of prices until the supply and demand quantities are made equal" [Walras, 1895, 630; in Walker, 1987a, 763].^{12 13} But the argument was then basically centered

¹¹Jaffé's view points in the same direction as Goodwin [1951] as well as a remark in Arrow and Hahn [1971]. Goodwin hinted at the similarity between "the traditional mathematical device of solving equations by trial and error" and economic dynamics regarded as "a series of iterated trial solutions which actually succeed one another at realistically great, regular intervals of time" (Goodwin [1951, 4]; in Jaffé [1981, 332]). Further, the remark is that "...in his more formal account of [tâtonnement, Walras] seemed to conceive of it as the Gauss-Seidel process" of solving a set of simultaneous equations, which being neither "a particularly attractive computational means" nor an imitation of the market "has rather little to recommend it." (Jaffé [1981, 329]; from Arrow and Hahn [1971, 306 and 322]). None of these writers seems to have any awareness of the impossibility of arriving at an exact solution by any computational technique (Manin, 1977, esp. Ch.5). Had any of them recognized this, their discussions of tâtonnement would surely have been seen to be puerile as well as (logically and empirically) pointless (cf. Velupillai [1991, esp. 32-5]).

¹²See also Walker [1988]. Most of the article is devoted to showing that [304] "...rightly or wrongly, [Walras] thought [his theory of economic tatonnement] was an abstract account of real economic behavior."

¹³Edgeworth expressed strong doubts on the possibility of giving a general solution to the dynamic behavior of markets (cf. Walker [1987c, 160-1]). Furthermore, he attacked Walras' generalization of tâtonnement as *the* rule of price adjustment in markets (the choice of free competition being only one among a variety of actual market structures): "Prof. Walras's laboured lessons indicate *a* way, not *the* way of descent to equilibrium" [Edgeworth, 1889, 435]. This rejection of tâtonnement as important to the

on the production model, which before the 4th edition (1900) displayed indisputably disequilibrium tones. Nonetheless, one conclusion seems to emerge: Walras' (and later followers') mixing of mathematics with reality is a road to serious confusion.

However suggestive these conjectures might be, the origin of the two views, static or dynamic, lies in the theory of tâtonnement in production. Such demarcation in its actual form can be traced to Jaffé's change of view from [1967] to [1981], and to Walker's [1987a] critique and appraisal. Having no clear idea of the theory of production, Walras' own views evolved over time, and thereby both interpretations could find exegetical support. There is, however, a clear line of continuity. In the summary explanation of the theory of production in the Preface to the *Éléments* [41-2] (first introduced in the 2nd edition) Walras apparently saw no need to introduce any correction in the text after a change in the mechanism of trading was introduced in the 4th edition (p.37). Exchange and production are here understood to take place in the process of adjustment towards equilibrium prices, and this may only allow for the inference that Walras didn't finally attach much relevance to the mechanism of trading, his concern seeming to be above all with the generation of a set of prices leading to maximum utility in exchange (as indicated above, Walras lost interest in the mechanics of trade before he shifted attention to the "general" numéraire model of multiple-commodity exchange). If this be the case, I can't help reading some aspects of the discussion on the subject as a little more than 'hen scratching' [Fowles, 1983, 32], which is not to say that Walras is blameless for his unsatisfactory account of price adjustment and for his superficial account of the logistics of trading in the general model. However, this remark better fits

theory of determination of prices was received acrimoniously and provoked Walras' reiterated affirmation of his position, as above (cf. Walker [1987c, 160-4]).

later writers. If Walras was beaten by the trading problem, it has been mostly evaded since.

Nevertheless, let us elaborate on the arguments the discussion involves. In the second and third editions of the *Éléments*, equilibrium in Walras' theory of production is portrayed as the result of a series of tâtonnements in production, with transactions occurring at non-equilibrium prices and production at non-equilibrium quantities.¹⁴ The numéraire price of each commodity is changed according to the Walrasian pricing rule, i.e., it is changed in the same direction as the sign of the excess demand quantity for the commodity. At each new set of disequilibrium prices, a new set of disequilibrium quantities of services is hired and a new set of disequilibrium quantities of commodities is produced. Prices are changed at each round of the tâtonnement process, and the continuation of tâtonnement is thought to lead the system of new quantities and new prices closer and closer to equilibrium, until the equilibrium set of prices and quantities is purportedly found (cf. Walker [1987a, 761]). Apparently, there is a real dynamic account of equilibrium in production, as a prior condition for the otherwise 'instantaneous' equilibrium to be obtained in exchange.

Walras struggled with this question in his theory of production. The fact is that in the 4th edition tickets or pledges ("*bons*") were introduced: Walras abandoned the view that the preliminary groping in order to establish equilibrium occurs effectively but

¹⁴Given that production requires the transformation of productive services into products: "Certain prices of services being cried, and certain quantities of products being made, if prices and quantities are not equilibrium prices and quantities, it will be necessary not only to cry other prices but to produce other quantities of products. [...] An iteration of tatonnement consists in this. At the prices of services first cried at random and then raised or lowered according to the circumstances, the entrepreneurs will borrow from landlords, workers, and capitalists the quantities of services necessary to make certain quantities of products determined initially at random, and then increased or decreased according to circumstances. Then they will sell these products on the market for products." [Walras, 1889,235; as in Walker, 1987a,761]

supposed "...instead, that it was done *by means of tickets* [*'sur bons'*]" [Jaffé, ed., 1954, 37; see also 242]. And, by doing so, he eliminated disequilibrium transactions and production from his system. Thus, in an economy in which production occurs,

... transformation of productive services into products takes place. Certain prices of services being cried, and certain quantities being produced, if these prices and these quantities are not equilibrium prices and quantities, it is necessary not only to cry new prices, but to produce other quantities of products. In order to achieve a rigorous *tâtonnement* in regard to production as in regard to exchange, all while taking account of this circumstance, it is necessary only to suppose that the entrepreneurs represent the successive quantities of *products* with *pledges*...; and that landlords, workers, and capitalists represent the successive quantities of *services* with *pledges*. [Jaffé, ed., 1954, 242; as in Walker, 1987a, 767]

Therefore, production as well as exchange only take place after a *tâtonnement* process 'obtains' the equilibrium prices, which are the same as those determined by the theoretical solution. Introducing the "fiction" that groping in production is done by means of pledges ("*sur bons*"), Walras was able to prevent any change in asset holdings until the equilibrium price is found, and thus to circumvent the problem that, in case non-equilibrium production would take place, at each step of the *tâtonnement* process the amounts of assets held by traders would be altered, thereby changing the parameters of the static equations (cf. Walker [1987a, 766]; Jaffé [1967, 9]).

The "complication" that the process of *tâtonnement* entails [Jaffé, ed., 1954, 242] should be the "distribution" parameter,¹⁵ i.e., the distribution of asset holdings held by

¹⁵Walker has a particular, and correct, interpretation of this distribution complication. He doesn't refer to distribution of asset values but to changes in asset holdings [Walker, 1987a, 766 and 767]; see Walker [1990c, 629-30] where Jaffé's view is refuted (as well as Jaffé's interpretation of Patinkin [1965, 534-5]). Walker [1971] discussed "Jaffé opinion [1967, 4 and 17] that it is more important to analyze the variations of the values than the physical components of the trader's assets. He [Jaffé] bases his view on Walras's Theory of Equivalent Distributions (...), which states that if the value of each trader's asset is constant, redistributions of the assets will not affect the price at which the market supply and demand quantities are equal. Thus Jaffé believes that changes in the value of the separate endowments result in changes in the price at which supply equals demand. These views ... are not true in general" [Walker, 1971, 1173]. He concludes that "...it is not accurate to say that, given the other constant market-day conditions, constancy of the values of each trader's asset holdings is in general necessary or sufficient to ensure the

the individual participants during the groping process; and if, as a consequence, there were a change in the numéraire value of the asset holdings (and the supply of the services of assets, and incomes, in the case of production) of the traders in any round of the disequilibrium correction process, the convergence path of the tâtonnement process wouldn't lead towards the mathematical solution.

Production only brought in a new problem different than exchange given Walras' realistic presupposition (though provisionally abstracted in the theory) that production takes time¹⁶ so that intentions of economic agents would have to be reconciled ex ante. Walras' eventual recourse to pledges in the model of tâtonnement in production has been justified on grounds of his realization that if he had allowed exchange to occur at disequilibrium prices and quantities, the conditions (the amounts of consumer goods held by traders, the stock of capital goods, and the amounts of capital good services) would vary during tâtonnement and thus the solution to the static equations would fail to render the true equilibrium values of the system (cf. Walker [1987a, 766]).

In the theory of exchange the exact same complication is present, but since traders were idealized in an organized type of market - in direct communication - there would

determinateness of equilibrium, nor appropriate to say that attention should be given to the values rather than the physical stocks held by the traders" [1174]. To show that it is not a necessary condition, he presents an example. And to show that it is not a sufficient condition, Walker first reminds that any change in the asset distribution by transactions occurring at the solution price will not alter this; moreover, as to "the constancy of aggregate values of assets," this will not be affected by trading at *any* given price, even a disequilibrium price, in case such price is quoted, although "...the price at which supply and demand are equal will ordinarily keep changing as more and more is traded at a given disequilibrium price" [ibid.]. (This same argument is summed up in Walker [1990c, 630].)

¹⁶"There is still another complication. [...] Production [as contrasted to exchange] ... requires a certain lapse of time. We shall resolve [this] ... difficulty purely and simply by ignoring the time element at this point. And later on, in Part VI [Theory of Circulation and Money], we shall bring in *circulating capital* and *money* and thereby make it possible for productive services to be transformed into products instantaneously, provided that the consumers pay the interest charges on the capital required for this sort of transformation." [Jaffé, ed., 1954, 242]

be no need for *bons* to be recorded; the simple crying out of (new sets of) prices would work it out. Walras' model of exchange contains the same distribution problem ("endowment effects", which are of the sort of income effects), but Walras' breed of realistic approach could dispense with the *bons* and allowed him to assume the "complication" away. Therefore, in the theory of exchange no room is left for the possibility that behavior/decisions may not be reconciled ex ante. (In fact, I believe that the theory of exchange is liable to a much richer set of dynamic questions than Walras acknowledged.¹⁷) On the other hand, there is the slight possibility that Walras had realized that disequilibrium trading would invalidate his equilibrium equations in exchange.¹⁸ Whatever the case may be, having postulated the suspension of trading until prices are equilibrium prices, redistribution of endowments in exchange could have no effect.

Summing up, Walras' late reformulation (4th edition) of the tâtonnement process

¹⁷That is why we shouldn't agree at large with Walker: that the allegation "...that Walras devoted his attention almost exclusively to the conditions of static equilibrium in an abstract model devoid of institutional detail, economic facts and dynamic behaviour, is a misrepresentation of his work" [1987b, 854]. His abstraction from complications in dealing with the tâtonnement in his final account of the subject (4th ed.) led him far away from any reasonable representation of the workings of general exchange; here, institutional detail is a product of sheer imagination and the equilibrating mechanism does without the market. (Moreover, in his apology for Walras' work, Walker often brings himself to the edge of historiographical imagination; see Walker [1990b, 967-8].)

However, Walker's contention that the pledges model was inserted as an afterthought to his former construction provides a good explanation for the apparent inconsistency between the formal presentation of the model and several descriptions of the working of actual markets, not only of perfectly organized markets but as well of decentralized markets. In fact, Walras often has in mind tâtonnement as working in non-brokered markets: "The rapidity and reliability of the market solution leave no room for improvement. It is a matter of daily experience that even in big markets where there are neither brokers nor auctioneers, the current equilibrium price is determined within a few minutes, and considerable quantities of merchandise are exchanged at that price within half or three quarters of an hour." [Jaffé, ed., 1954, 106]

¹⁸Walker [1987a] calls upon fragmentary evidence thereon: this is a piece of correspondence from Walras to Bertrand, "that he [Walras] had "rightly maintained" that his model of exchange was determinate because "exchange was suspended in the case of the inequality of the quantities supplied and demanded" (Walras [1895, 630]; in Walker [1987a, 766-7]).

operates with pledges in both the exchange and production models, and trading at 'false prices' does not occur.¹⁹ On trading at false prices, see Hicks' *Value and Capital* [Chapter 9, esp. Note], whose assumption of "an easy passage to temporary equilibrium" sweeps complications under the rug (for critical comments, see Appendix Note B).

Walras' attempt to provide a demonstration that "...the mechanism of competition in the market is nothing but the practical determination of the calculated prices [prix du calcul]" [Jaffé, ed., 1954, 184, adapted] led him to abandon his former and better thought-out consideration of markets as undergoing a process of adjustment whereby transactions and production take place, and thus better conducive to the understanding of the functioning of real competitive markets. Those are two separate theoretical goals, hardly reconcilable, and hence the two conflicting aims of a theory of tâtonnement. That the disequilibrium production model was incomplete and the pledges model too farfetched, can be adduced as the reasons why Walras' second exercise didn't succeed.

But the second exercise is "the essential point", as Walras remarked, for the understanding of competitive markets. To give a try to this second exercise, the workings of markets cannot be frozen (trade cannot be suspended) during the adjustment process, otherwise we end up circumventing it, as Walras' theory of tâtonnement in general exchange tacitly, though unwittingly, did.²⁰

We should, however, acknowledge that Walras, in passing, had it pointing in a

¹⁹Equilibrium becomes determinate [Kaldor, 1933-4], and the outcome independent of the path [Arrow and Hahn, 1971, 334].

²⁰I agree with Walker's appreciation of why Walrasian theory did "...fail to be useful as even a highly abstract analysis of economic behaviour": "...the pledges model is designed to be consistent with certain mathematical conditions - that is, with the solutions of a set of equations - rather than being a set of assumptions and mathematical conditions designed to explain economic behaviour." [Walker, 1987b, 860]

promising direction in his "trading posts" model, where trading ("of several commodities for one another") takes place through pairwise exchanges between traders (or trader agents) in a market "...divided into as many sectors as there are pairs of commodities exchanged" [Jaffé, ed., 1954, 158]. This is a first step into direct barter exchange (which will be analyzed in #4.3.3), but the same bargaining problem that Walras attempted to deal with when he introduced indirect barter remains basically unsolved today.

The neowalrasian diversion

General equilibrium analysis along the lines of Arrow-Debreu [1954; 1959] is usually viewed as "...an almost literal description of an idealized economy in which the notional economic plans of individual economic agents are costlessly coordinated by a central intelligence unit - the so-called auctioneer" [Clower and Leijonhufvud, 1975, 183]. This neowalrasian theory provides the solution to Walras' mathematical problem, and as to the second exercise the question raised is not Walras', "...but rather whether we can conceive of an economy that is *completely* characterized by equilibrium relations of the kind identified by Walras" [184]. And the case is that the adjustment of market prices to the mathematical solution is obtained by their model since their question is raised under the belief that the solution to the model is a proper representation of the relevant states of the real world; which Walras didn't. Walras departs from "real-type concepts" drawn from experience and then proceeds to abstract "ideal-type concepts" and reasons on the basis of these; only to return to reality with a view to practical applications upon the completion of a pure science of economics (cf. Jaffé, ed. [1954,

71)). Furthermore, when envisaging an approach to the real workings of the market, Walras stays within his view of the "rational" method, where he goes "...back to experience not to confirm but to apply ... conclusions" [71].²¹ The following quotation can be so read:²²

Finally, in order to come still more closely to the reality of things, we must also drop the hypothesis of an annual market period and adopt in its place the hypothesis of a continuous market. Thus, we pass from the static state to the dynamic state. [...] Such is the continuous market, which is perpetually tending towards equilibrium without ever actually attaining it, because the market has no other way of approaching equilibrium except by groping, and, before the goal is reached, it has to renew its efforts and start over again, all the basic data of the problem ... having changed in the meantime. [Jaffé, ed., 1954, 380]²³

In the neowalrasian approach there is nothing of the sort. (The steps of the explanation are based on Arrow and Hahn's [1971] account of general equilibrium analysis, which I shall simplistically - or even abusively (see Hahn [1970, 2]) - identify as neowalrasian.) There is an invented world, that purportedly mimics the relevant features of the real world,²⁴ and the questions raised are "...not only whether it is true,

²¹To notice the similarity to Colander [1992, 195], borrowing from John Neville Keynes, on the "art of economics" - to be differentiated from positive economics, and empirical work in positive economics. "The purpose of empirical work in the art of economics is not to test theories: it is to apply theories to real-world problems. [...] Empirical work in the art of economics should be designed to apply a theory by adding back the contextual reality."

²²Notice Jaffé's [1981, 325] opinion that this quotation appears in a final part of the *Éléments*, dealing with distinctly dynamic phenomena structurally separated from the theory of pure competition.

²³See also Walras on equilibrium as "...an ideal and not a real state," yet it is "...the normal state, in the sense that it is the state towards which things spontaneously tend under a régime of free competition in exchange and production." [Jaffé, ed., 1954, 224]

²⁴See the Introduction to Arrow and Debreu [1954] on the reasons for studying the question of existence of an equilibrium for a competitive economy, which is considered of interest both for descriptive and normative economics: "Descriptively, the view that the competitive model is a reasonably accurate description of reality, at least for certain purposes, presupposes that the equations describing the model are consistent with each other" [Arrow and Debreu, 1954, 265]. In a recent review of the theory of economic equilibrium, and referring to Walras' mathematical analysis in the *Éléments*, Debreu [1986, 405] starts this way: "The observed state of an economy can be viewed as an equilibrium resulting from the interaction of a large number of agents with partially conflicting interests." (But Arrow [1994, 5] is skeptical about

but also whether it *could be true*" [vii].

And a world was invented. The task neowalrasians propose to undertake, in a line of inquiry reminiscent of Adam Smith's Invisible Hand, is "...to show that a decentralized economy motivated by self-interest and guided by price signals would be compatible with a coherent disposition of economic resources. [...] Moreover, the price signals would operate in a way to establish this degree of coherence" [Arrow and Hahn, 1971, vi-vii]. Thus, the work of the price signals would allow a decentralized economy to attain coordination, or coherence (whatever this is meant to require, a notional, a feasible, or a potentially real state of affairs). How is decentralization defined? How does decentralization impinge upon the working of the price signals? Is guidance by price signals sufficient for a "coherent" disposition of economic resources in a decentralized economy? This sequence of questions leads to the doubt about which world is depicted in general equilibrium analysis.

Equilibrium in the Arrow-Debreu world has the strict meaning of a rest point, in which individuals' optimal plans, based on a given set of prices, are as if in harmony with each other. That is to say, "...the language is not equilibrium *is* a supply-demand

the "relation to real-life phenomena" of the use of a non-cooperative game in the "purely mathematical construct" in Arrow and Debreu's [1954] proof of existence of Walrasian equilibria.)

Notice, however, the more balanced view by Hahn [1973a, 7]; after defining the Arrow-Debreu equilibrium, he adds that "...this construction ... makes no formal or explicit causal claims at all. For instance it contains no presumption that a sequence of actual economic states will terminate in an equilibrium state. However it is motivated by a very weak causal proposition. This is that no plausible sequence of economic states will terminate, if it does so at all, in a state which is not an equilibrium. [...] [N]o description of any particular process is involved. It is also clear that weak as this claim is, it may be false"; on these two different questions, first, that "...equilibrium cannot be claimed to describe properties of all potential terminating points of any actual process," and second, that the weak claim may be false, see pp.6-16. Also, referring to the mistaken, commonly maintained, implication of general equilibrium analysis that the price system ensures the 'proper' use of exhaustible resources, Hahn remarks: "This negative role of Arrow-Debreu equilibrium I consider almost to be sufficient justification for it, since practical men and ill-trained theorists everywhere in the world do not understand what they are claiming to be the case when they claim a beneficent and coherent role for the invisible hand. But for descriptive purposes of course this negative role is hardly a recommendation." [Hahn, 1973a, 14-5]

balance," but rather "when in equilibrium, supply and demand are in balance" [Weintraub, 1991, 107]. This might just mean that Arrow-Debreu equilibrium is a solution to a set of implicit mathematical assumptions.

Stability of a general equilibrium set of prices is shown by means of an exercise whereby a central mediator selects prices and changes them until supply and demand plans of agents are balanced. That is to say, the equilibrium set of prices, if it exists, is asserted as the result of a virtual adjustment as conducted by the market-maker, a central one, the auctioneer,²⁵ and bargaining is correspondingly out of the picture. Besides, no question is raised on how individual agents assess that these prices are equilibrium prices; we could think of this convergence to equilibrium as an "as if" mechanism "...by which agents compare notes to see whether they are going to be satisfied" [Weintraub, 1991, 107]. But there is no room, and no economic incentive, for agents to devote effort to such communication. Since centralization of information gathering and dissemination is at the root of the mechanism, every attempt at "market" imagery is vain.²⁶ For sure, the neowalrasian model can be seen as an exercise dealing

²⁵The representation of market forces is assigned to the "market participant" in Arrow and Debreu [1954, 274], the "chairman" of a "central registry" in Patinkin [1956, 37], and the "Secretary of Market" in Uzawa [1960, 184]; according to Walker [1972, 356], the designation of auctioneer is due to Henderson and Quandt [1958, 95]. Koopmans [1951, 93-5] has a "helmsman" (representing the 'one' consumer) determine the initial prices of final goods, and a set of rules for price adjustment by the commodity "custodians" (cf. Hurwicz [1973, 8 and 12]); later, Koopmans [1957, esp.179] became critical of "...the view that impersonal market forces can generate the *tâtonnement* properties" and of the "...mechanical use of the Walrasian pricing rule [in *tâtonnement* models]" (cf. Walker [1972, 357,12n]). Clower [1955] appeals to the marketor function in either competitive or monopolistic market forms (see also Clower [1994b,3n]), and Haavelmo [1958, 29] summons a "market administrator" to make sense of the "demand-supply cross."

Edgeworth [1881, 30] invoked "...a sort of market-machine" to evaluate the *price* in a state of perfect competition; but he was not dealing with convergence. Walras had also referred to calculators (see Walker [1990b, 966]).

²⁶"The "supply-demand balance" ... serves, simply put, as a reference point for some fictitious market-maker to tell players to keep on playing, for they are not yet coordinated. If, indeed, all agents were to get this information for themselves, from their own actions, then the supply-demand balance idea would not be associated with equilibrium except after the fact; that is, if the message "lack of coordination" could

with an "invented world" where, in the presence of a correct set of prices, plans are harmonized.

But Arrow and Hahn's proposed claim is broader. In the study of stability, their goal is framed in the context of the Marshallian argument "...that there are forces at work in any actual economy that tend to drive an economy toward an equilibrium if it is not an equilibrium already" [Arrow and Hahn, 1971, 263]. However for analytical reasons, they keep bound within "artificial process of adjustment" [264], "laboratory situation" [282], and "unrealistic analysis ... suppose there is an auctioneer" [324]. Of special interest here is Arrow and Hahn's attempt to analyze 'trading' out of equilibrium. Here the authors relax the former assumption of tâtonnement, i.e. the mechanism of price adjustment "...in which no contract is binding except in equilibrium" [Arrow and Hahn, 1971, 282].²⁷ And, thereby, "extra realism" is gained, since "[i]nstead of supposing that prices are moved by target excess demands, we now ensure that active excess demands are responsible" [340]. Nevertheless, when introducing out of equilibrium trading, they stick to their fiction of the auctioneer: "...at any moment of time he establishes unique and public offers on which goods may be traded, and he adjusts these terms in the light of market observations by some particular rule" [324]. (On this, see Chapter V.)

We shouldn't deny the analytical difficulties under a less stringent informational

be triggered directly by the lack of harmony among agents' plans, and that message would lead to a revision of those plans in a self-correcting manner, then there would no longer be any need for the "market" to function as an information-dissemination device that says "keep on trading." [Weintraub, 1991, 107]

²⁷In fact, this "serious enough restriction on reality" [Arrow and Hahn, 1971, 285] "...seems to carry the logical implication that trade never takes place" [324]. But, as will be seen below, there is no trading, or at least no decentralized execution of trades (see also proportional 'rationing' on monetary economy [340]); this is just an exercise on convergence.

basis, but we must question the merit of solutions to problems, the range of which is set by analytical technique. In fact, Arrow and Hahn's detours from the defined goal of the analysis stem from the imperative of tractability: "What is happening now is that, having decided on one idealization (perfect competition), we run into what must be taken to be logical difficulties unless we import a further idealization: the auctioneer" [325].

Therefore, the condition imposed that trading cannot occur at non-equilibrium prices shouldn't be found in the early Walrasian desideratum to prove that the stability exercise produces the same result as the solution to the set of equations; Walras' view of the working of the organized market of reference, the Paris Stock Exchange - however unclear or wrong - allowed him to conduct analysis as an "as if" mechanism. In the neowalrasian models, the reason lies in tractability and a misplaced faith in correspondence with "the actual world".

The final construction is self-contained and logical, and yet it bears some correspondence with "...features of the world regarded as essential in any description of it" [vii]. But, despite Arrow and Hahn's oft-asserted reservations about the verisimilitude of assumptions, the overall purport of the analysis is bent towards an optimistic stand that the consideration of these features in their model does not disconfirm the claims set forth. Arrow and Hahn are not dealing with a decentralized economy, and their exercise in stability is valid only for a world with no decentralized communication between agents, where information, and planning and execution of trades involve no set-up costs.²⁸ The auctioneer is thought to perform this function of finding

²⁸Hicks [1967, 6-7] raises the question of non-proportional transaction costs. "[I]f the cost is proportional to the volume of the transaction, it is the same as if the transaction were subjected to a tax"; a Walrasian equilibrium could be attained, even though "...a Walrasian equilibrium after tax." Differently, the consideration of set-up costs of transaction originates economies of scale in transacting, and the consequences on the Walrasian model are "more serious" [6n].

and announcing equilibrium prices only because, since trading is costless and centrally coordinated, execution can be dealt with separately. Thus, their question of whether the world they create "could be true" [vii] is misplaced and misleading. Since execution of communication and trading falls under the free services of a central market organizer who monitors direct trade with the central market place (as if by means of direct multilateral trades), also the other function of the auctioneer of finding equilibrium prices stands only as a representation of an ethereal world of centrally coordinated individual trading plans.²⁹

A fine attempt to explain the effect of both these types of transaction costs on exchange is Hirshleifer [1973] (see #4.1). For a definition of transaction costs, and effects, see Niehans [1987].

²⁹For a dissection of the missing parts of the neowalrasian approach, see Clower and Howitt's *Foundations* [1993a, esp. 10ff], and for a thorough critique of Debreuvian axiomatics, see Clower [1994d].

CHAPTER III
HOW STANDARD PRICE THEORY BECAME PREDOMINANTLY
NEOWALRASIAN

In this chapter I discuss some evolutions, dissatisfactions and solutions in price theory that led to the dominating role of the neowalrasian approach, and hint at some abandoned tracks along the way.

3.1 - Marshall, Walras, and the neowalrasians: some dividing lines

Marshall and Walras stand rather often as labels to be thought of in opposition. In fact, this is misleading.¹ The contrast should be established with the neowalrasian construction, which as seen above, evolved out of Walras' and Pareto's no-arbitrage or numéraire models.

Starting off with the dissimilarities, Marshall and Walras refer their theories to different markets. And most probably as a consequence, they apparently explain the

¹See Hicks' *Léon Walras* for an appraisal of the affinities between Walras and Marshall: "For a considerable part of the way Walras and Marshall go together; and when they separate, it is a difference of interests, rather than technique, that divides them. While Walras was seeking for the general principles which underlie the working of an exchange economy, Marshall forged an analytical instrument capable of easier application to particular problems of history and experience." [Hicks, 1934, 338]

determination of equilibrium in a slightly diverse fashion, Marshall in terms of demand and supply prices and Walras in terms of net excess demands. This might mean that they were dealing with different choice variables: in Marshall agents choosing prices and in Walras quantities. However, in their explanation of adjustment to equilibrium either in exchange or in production their language is very much compatible, even though much confusion envelops the interpretation of Walras' view on the subject; the fact that he does not allow for trade to take place in disequilibrium, and that the bargaining process is not explained in the general barter model (and prices set as a result of bargaining among agents - as he does, or attempts to do, in the case of the other barter models) do not imply that Walras did not mean the finding of prices to be obtained by means of bargaining among agents in the general model (even though this might be unfeasible).

The case is different in the neowalrasian view. Here the function of finding equilibrium prices is clearly viewed as requiring a central price-maker, the auctioneer. Strangely, although Walras had started from decentralized bargaining, and general equilibrium analysis is barren in the understanding of adjustment processes, in fact the neowalrasian view of central coordination has been thought to deliver a logical and complete account of the working of Walras' general model.

Some differences are notorious between Walras and Marshall, and the first one regards the choice of market of reference for the understanding of competition. As we have seen, in the construction of his barter models, Walras supposes always the markets well organized² in regard to competition. Marshall, on the other hand, has an

²In fact, the wording Walras uses is perfectly organized, but this should probably be avoided on grounds of misleading connotations, which however were not present before the 1920's.

encompassing perspective of markets; he establishes only a gradation regarding how traders are in close communication, and the consequent definition of perfection of the market in terms of "...the tendency for the same price to be paid for the same thing at the same time in all parts of the market" [Marshall, 1920, 325]. He distinguishes the wide markets such as those of securities and of standardized commodities like valuable metals (or grain in America) and, on the other extreme, basically local markets, where competition is however indirectly felt;³ and "about midway between these extremes lie the great majority of the markets which the economist and the business man have to study" [Marshall, 1920, 329].⁴

Another aspect regards the variables on the basis of which equilibrium is defined, which can be related to the choice variables. Here Marshall and Walras rely on different definitions, and mathematical or graphical formalizations. In Marshall's temporary market-period equilibrium,⁵ equilibrium price is plainly defined as that that equates supply and demand: "The price of 36s. has ... some claim to be called the true equilibrium price: because if it were fixed on at the beginning, and adhered to throughout, it would exactly equate supply and demand (*i.e.* the amount which buyers were willing to purchase at that price would be just equal to that for which sellers were willing to take that price)" [Marshall, 1920, 333]. As to the equilibrium in production,

³"...those secluded markets in which all direct competition from afar is shut out, though indirect and transmitted competition may make itself felt even in these" [Marshall, 1920, 329; see also 328].

⁴Marshall relies on the "...broad relations which are common to nearly the whole of [economic science]," assuming "...that the forces of demand and supply have free play; ...and there is much free competition; that is, buyers generally compete freely with buyers, and sellers compete freely with sellers." [Marshall, 1920, 341]

⁵Beyond space, Marshall considers the element of time in the working of a market, and he distinguishes temporary equilibrium (market period), the short-run and the long-run, the first where supply is fixed (stocks offered for sale are a given), the second where supply is variable given capacity, and the third where capacity is adjustable.

Marshall doesn't start out as clearly, though. He states: "...when the demand price is equal to the supply price, the amount produced has no tendency either to increase or to be diminished; it is in equilibrium" [Marshall, 1920, 345].⁶ ⁷ But he immediately adds: "When demand and supply are in equilibrium, ... the price at which it is being sold may be called the *equilibrium price*." Thus, overall we may infer that, in Marshall's (partial equilibrium), net excess demand, $Q' \neq 0$ unless $p^s = p^d$. In Walras, equilibrium in exchange requires net excess demands be zero for every commodity (cf. Jaffé, ed. [1954, 41,109,253]).

The relevant question is whether these are just mirror images or whether they carry implications for the analysis. First, we may refer to Cournot who, when passing from monopoly to competition of producers, replaces the demand curve ($D = F(p)$) with the "inverse notation" ($p = f(D)$) [Cournot, 1838, 80]; without however changing his exposition, and continuing to refer to adjustments in price (see 80ff). In Cournot, the demand function is invertible,⁸ and this is all there is to this change in notation. We know, however, that this is not just a question of notation. In the theory of oligopoly it is clear that price competition and quantity competition have, for a broad class of game configurations, distinct results, the reason stemming from prices being strategic

⁶However, the exposition based on demand price and supply price as the variables to be equated in order to define equilibrium stands coherently with his view of markets of interest to investigate.

⁷The definition of supply price is the following: "...the price required to call forth the exertion necessary for producing any given amount of a commodity may be called the supply price for that amount, with reference of course to a given unit of time" [Marshall, 1920, 338]; or, as to normal supply price, "...this is the price the expectation of which will just suffice to maintain the existing aggregate amount of production" [343].

⁸Cournot assumes the market demand function ($F(p)$) is continuous, and that "the variations [of demand with price] will be of opposite signs, *i.e.*, an increase in price will correspond with a diminution of the demand." [Cournot, 1838, 49-50]

complements and quantities strategic substitutes (Bulow, Geanakoplos and Klemperer [1985]). Second, for a competitive economy, if strategic interdependence is left off the picture, and no single agent realizes to be able to influence the prices of the market, then prices can be used as economic parameters. In the study of competition, this was clearly used by Walras, and also, but less so, by Marshall. This must have come in both authors of Cournot's analysis of unlimited competition (both authors acknowledge the influence of Cournot, in general terms). But then we have a problem in both Walras and Marshall, if agents are thought of as bargaining over prices how can we also treat prices as parameters? Be that as it may, the relevant point is that the neowalrasian approach is only clearly understood with individuals choosing quantities on the basis of given equilibrium prices. And as standard price theory stands, "[i]t is not explained whose decision it is to change prices" [Arrow, 1959, 43].

Despite this different assertion of equilibrium conditions, we are very much led to the conclusion that this has no recognizable consequences on the exposition of adjustment to equilibrium by Walras and Marshall. Notice, though, that we are not looking at the consistency of bargaining and trading execution; in fact, we are looking only to bargaining and pricing in exchange; yet, to fully understand Marshall's view we have to ask how he fits bargaining and pricing in the analysis of normal equilibrium (specifically, short-run equilibrium).

In Marshall, the relation of forces of demand and supply leading towards equilibrium in the market period are explained on the basis of adjustment of price such that net excess stock demand is zero (in order to compare with the exchange model in Walras we must, first, look at temporary equilibrium). Also in Walras adjustments to equilibrium in exchange are assessed by way of variation in price, with agents bidding

against each other (Jaffé, ed. [1954, 40-1,83,223-4,255,478]), the rule applying that: "...to the left of the point of equilibrium, the demand for the commodity in question is greater than the offer, which must result in a rise in price, that is, in a movement towards the point of equilibrium" [109]. Therefore, in Walras equilibrium prices are 'obtained' through competitive bidding among buyers of products (or among sellers of services), according to the Walrasian rule. The exact same picture of price as the adjustment variable is depicted in Marshall's temporary market-period equilibrium, but for the fact that Marshall is clearer than Walras in allowing for trades during the equilibrating process (Marshall [1920, 333-4]).⁹

Moving on to normal equilibrium, where supply flows are introduced, Marshall is still concerned with movements of price (p.338), but adjustments here involve both price and quantity.¹⁰ The function of adjusting quantities concerns clearly the producing unit, the representative firm. The marketor function in Marshall's short-run period is carried out by sellers¹¹ who bring goods to market. And their function in the working of the market is twofold: one is supposedly trading ("higgling and bargaining"), the other is to issue a signal, to represent the "active force" that tends to change quantities

⁹Since Marshall was dealing with a particular market in isolation, he could show that if the commodity offered in exchange could be assumed to display constant marginal utility (money or "income"), the final rate of exchange (equilibrium price) would be independent of the path through which equilibrium is reached (cf. Marshall [1920, 334-6, and Appendix on Barter,793]).

¹⁰See Leijonhufvud [1993, 9], who considers that "...the market for a produced good has to have two servo-mechanisms - one regulating price, the other output.' Such a Marshallian market might be represented by two differential equations: (1) the rate of change of prices as a function of excess demand, and (2) the rate of change of output as a function of excess supply price."

¹¹The discussion is worded in terms of sellers, the fact that they possibly are the same people as the producers being theoretically irrelevant here. We are concerned with functions, not people.

to supply, or to produce.¹²

Now we are considering the relationship between the two functions, the determination of prices in exchange, and the choice of output in production; exchange and supply (production) are better separated in order to understand the working of the market. In both Walras and Marshall exchange is dealt with by agents - buyers and sellers - and prices obtained by means of bargaining. Further, the effect of the price signal given out on the goods markets is the same in both authors, it impinges on the producing units, which choose outputs. In Walras exchange and production are dealt with separately, one a stock equilibrium, the other a flow equilibrium. We are led to conclude that the same is true in Marshall, that is to say, in Marshall's normal equilibrium exchange plans are not specifically at stake, only production plans are; hence the reasonableness of Marshall's postulating "perfection" in regard to price in the case of normal equilibrium: "we assume that there is only one price in the market at one and the same time" [Marshall, 1920, 341-2].¹³ If this is the case, pricing refers to temporary equilibrium, and supply or production planning distinctly to normal equilibrium. By any means, this is not to say that Marshall didn't allow for supply flows to have an effect on pricing; Marshall acknowledges this influence by means of anticipations (the anticipation of the effect of the increase in supply on future prices leads buyers to intertemporal substitution, and "by waiting they help to bring the price down"

¹²"When ... the amount produced (in a unit of time) is such that the demand price is greater than the supply price, then sellers receive more than is sufficient to make it worth their while to bring goods to market to that amount; and there is at work an active force tending to increase the amount brought forward for sale." [Marshall, 1920, 345]

¹³This is an implication of his having "...assumed provisionally to be true both of finished goods and of their factors of production, of the hire of labour and of the borrowing of capital" that: "...though everyone acts for himself, his knowledge of what others are doing is supposed to be generally sufficient to prevent him from taking a lower or paying a higher price than others are doing." [Marshall, 1920, 341]

[Marshall, 1920, 333]), and dealings or contracts for future delivery [337-8].¹⁴ Thus, given prices and expectations, production decisions ensue and short-run normal equilibrium asserted. (This is not so simple; see Leijonhufvud [1974, esp.32-3] for a discussion of the ex ante/ex post character of normal equilibrium in Marshall.)

Walras has the same types of adjustments in the case of the establishment of equilibrium in a production economy:¹⁵ price adjustments are supposed to bring about equilibrium in exchange, and quantity adjustments equilibrium in production.¹⁶

Summing up, the marketor function is played by traders in both Walras and Marshall. This is not so, however, in the neowalrasian construction where prices are determined in abstraction from bargaining.¹⁷

¹⁴"Even in the corn-exchange of a country town on a market-day the equilibrium price is affected by calculations of the future relations of production and consumption; while in the leading corn-markets of America and Europe dealings for future delivery already predominate [...] Anticipations of [a] rise in [price] exercise an influence on present sales for future delivery, and that in its turn influences cash prices; so that these prices are indirectly affected by estimates of the expenses of producing further supplies." [Marshall, 1920, 337-8]

¹⁵For the conditions of equilibrium and adjustments, specifically in production, see Jaffé, ed. [1954, 40-2,253-4,478], and Marshall [1920, 345 and 807n].

¹⁶Samuelson [1947, 264n], first published in [1941], points out the "historical error" of attributing to Walras and Marshall the indication of stability conditions "in alleged contrast." He observes that Marshall "...as far back as in *The Pure Theory of Foreign Trade*" defined stability in similar terms as Walras (a formal presentation of which the author makes on pages 266-7); and the same opinion had been offered in Hicks [1939/1946, 61]. Samuelson bases Marshall's adjustment in the theory of normal price on the obvious fact that "...the quantity supplied is assumed to adjust itself comparatively slowly" [Samuelson, 1947, 264]. However, he fails to establish the broader similarity between the two authors, only because no attention was paid to the effect on adjustments of the distinction between exchange and supply. (Notice the parenthetical note on p. 270: "This rules out in the beginning cases II ["Marshallian stability conditions require that quantity increases when demand increases in every case" (264)] and IV [case of Marshall's *Foreign Trade*"]. This note refers to Hicks' stability conditions that an increase in demand increases price, and can be read as an indication that Samuelson may have been misled by Hicks.)

In fact, the same mistake appears in Hicks [1939/1946, 62n], who states that Marshall's stability condition is more appropriate to conditions of monopoly than to perfect competition. Furthermore, on what basis does this sentence by Hicks apply: "In deciding to treat the general theory of exchange before dealing with production, we are following the example of Walras rather than Marshall." [57]

¹⁷Let us quote these sentences from Samuelson [1947], which though drawn from a welfare reasoning, are nonetheless meaningfully innocent of the marketor role in the determination of prices: "although each individual in pure competition takes price as given, for the market it is a variable," and "[t]he only

Now we may be ready to resume the discussion on choice variables in Walras and Marshall. The problem is one of logical coherence between adjustment of price by agents in exchange, and the role of prices as parameters in the analysis. First, we have to bear in mind that both authors rely on the assumption of 'perfect' information on market prices in the process of adjustment, in the planning of production, even though Walras also specifically assumes this in bargaining (which is possibly due to his assumption on markets of reference). And this is where the view of prices as parameters enters. It doesn't mean, though, that there is no room for adjustment of price; that is to say, pricing is viewed as the result of bargaining in exchange, but all other prices in the market are taken as given 'in the interim'. Second, convergence to equilibrium prices in exchange is meant to happen quite fast (Walras), or without consequence, although fast as well (Marshall). Therefore, quantities exchanged are decided on the basis of these known prices, and the planning of output to produce can take place, based on prices determined in exchange (equilibrium prices, in Walras' pledges model). This is quite so in Walras. In Marshall we have seen that the distinction between temporary and short-run equilibrium brings in anticipations of future supplies, so that prices determined in exchange are not independent from expectations regarding the 'normal' situation, which is not so in Walras' theories of exchange, or of production, where the market "day" is seen in isolation from past or future events (cf. Hicks [1967, 3]). But

distinguishing feature of pure competition, as compared to any other mode of behavior, is that the market conditions facing each individual are taken (by him) to be "straight lines" involving trade at unchanging price ratios" [Samuelson, 1947, 204].

Notice this comment by Kornai and Martos [1981, 44] on Samuelson's dynamic price formula: "For Samuelson price changes over time are functions of excess demands. But he does not specify how the magnitude of excess demand is determined or estimated by market participants."

the question of the role of prices as variables of choice by agents, or as parameters, should by now be more clear, and interpreted on fairly similar terms in both authors.

3.2 - From a partial to a general equilibrium approach

From the thirties on, general equilibrium analysis was following its own course along two fairly separate routes. One is traceable to Cassel's *The Theory of Social Economy* [1918/1932] and it led to the Arrow-Debreu-McKenzie models.¹⁸ The other arises following Hicks' learning of the general competitive model in the writings of Pareto (and Walras), and its exposition in *Value and Capital* [1939] - in a form, as much readable as lacking in precision and clarity;¹⁹ this had a thorough undermining influence on both sides of the economics' new divide. On the aggregative side (macroeconomics) Hicks originated a reformulation of Keynes' *General Theory* along

¹⁸In fact (cf. Weintraub [1985, Ch.6]), the development of ideas that proved conducive to the eventual formalization of general equilibrium analysis in the Arrow-Debreu-McKenzie models gathered initial moment with the influence of Cassel's *The Theory of Social Economy* [1918/1932] upon a circle of Viennese economists, namely Karl Menger, Abraham Wald, Karl Schlesinger, Oskar Morgenstern. Meanwhile, by way of lectures at Princeton by the mathematician J. von Neumann (and his subsequent obtaining a permanent position there), and an "westward movement" of Austrian economists to the United States around 1937 (Wald, Menger, Morgenstern, Tintner), this research program eventually combined with the ongoing "studies on the general theory of economic measurement" at the Cowles Commission - which Kenneth Arrow (among others) joined by 1947.

In the forties "[g]eneral equilibrium was in the air," however much through the influence of Hicks rendering in his *Value and Capital* [1939] to English-speaking economists of the value theory of Pareto (and Walras) with a view to its application to dynamic problems of capital.

Finally, with the *Theory of Games and Economic Behavior* by von Neumann and Morgenstern [1947] and its generalization by Nash [1950] to the n -person equilibrium, together with the development of activity analysis and programming, the ground became laid to the Arrow, Debreu and McKenzie models, which ensued in the early fifties.

(For another account of this development, see Arrow [1968]; for the contributions of K. Arrow and G. Debreu, see Feiwel [1987, esp. 29-45] and Hildenbrand [1983], respectively.)

¹⁹See Morgenstern's [1941] review and strongly critical appraisal of the book. (Young's [1991] survey on this and other early critiques is of interest.)

Walrasian lines.²⁰ As to price theory, *Value and Capital* sidetracked the recently proposed theories of imperfect or monopolistic competition, and eventually helped to bring forth Triffin's appeal to general market interdependence. Those theories of imperfect competition had evolved, though, from a different approach, Marshall's partial equilibrium (and the welfare analysis of Pigou), which dominated standard price theory in Britain and the United States. Let us elaborate on this last point.

From Marshall to Chamberlin

Studies of price adjustment by firms in competitive markets (of which Arrow's *Toward a Theory of Price Adjustment* is paradigmatic) view the individual firm as facing a downward-sloping particular demand curve. Thus, in the background of any of these analyses lies the question of monopoly, monopolistic competition or imperfect competition, however the setting of such models. In the early thirties, these subjects were brought to the fore mainly with a view to solving Marshall's gap in the explanation of long-run equilibrium of firms displaying increasing returns.²¹ Industries were thought to conform either to conditions of the theory of competition or to the theory of monopoly, only the case of duopoly presented a special embarrassment, and was deemed in an unsatisfactory state.

²⁰Aggregative economics was molded into the general equilibrium framework; eventually, Lange [1945], Klein [1947], and Patinkin [1956] perfected this neowalrasian reconstitution.

²¹The predominant attention this subject was receiving was, according to Hicks, brought about mainly "...on grounds inherent in the development of economic theory itself" [Hicks, 1935, 362], by which he meant both the interest in mathematical economics that "...turned attention back to the work of Cournot", as well as concern on logical gaps in the work of Marshall.

To notice that Cournot, who had adopted the monopoly solution as a starting point for the study of competition, based his analyses of markets on the behavior of the individual firm. This contrasts with the Marshallian tradition and is in line with the general equilibrium analyses of Walras and Pareto (Lausanne School).

Marshall's attention was directed to the equilibrium of a competitive industry. Even though he was also concerned with the equilibrium of the firm (the "representative" firm, an equilibrium firm²²), his method stopped short of the posterior definition of a perfect market, which was put in so strict terms as entailing the necessity for the equality of marginal costs and marginal revenue of the individual business. The conditions imposed on the long-run supply curve of the individual firm that are compatible with equilibrium within a competitive industry was questioned on the grounds that increasing long-run returns was taken as the common situation in manufacturing. The solution to this problem of the determination of equilibrium at the firm level took primarily the way of postulating that marginal revenue should fall, with increasing output, faster than marginal costs fell; hence, the introduction of the concept of the individual demand curve (cf. Andrews [1964, 20-1]). Downward sloping demand curves bring about falling marginal revenue curves and the presence of increasing returns is no more the problem. The problem is then the economic basis for such downward sloping particular demand curves. Joan Robinson's demand curves were sketched as a ready-made "implicit" device to allow in theory the equilibrium of the firm, but rather than solving the problem it just concealed it.²³ Although issuing from reasons unrelated to the above controversy, Chamberlin explained his falling demand curves in terms of underlying consumers'

²²Marshall's recourse to the "representative" firm withdrew any meaning to the equilibrium of the firm, just meant postulating it.

²³J. Robinson's demand curves were so vaguely defined that imperfect competition became in her construction indistinguishable from oligopoly. The demand curve shows what the firm will sell at each price when all other adjustments are complete: "The demand curve for the individual firm may be conceived to show the full effect upon the sales of that firm which results from any change in the price which it charges, whether it causes a change in the prices charged by the others or not." [J. Robinson, 1933, 21]

preferences for the products of individual producers, on the basis of product differentiation within the group (of products that are close substitutes for each other). He distinguishes, though, the 'perceived' demand curve (dd') from the 'share-of-the-market' demand curve (DD'), which were instrumental in the explanation of adjustment to equilibrium, either of the firm in isolation or of the group.

Chamberlin's solution was received as a complete answer to the problems of the day: equilibrium of a competitive industry had become compatible with decreasing costs at the level of the firm. His success in getting a determinate solution for the large-group as well for the individual firm regardless of cost conditions made *The Theory of Monopolistic Competition* the most influential work in the attack to the dichotomy of competition and monopoly. Firms are partially isolated from their competitors, with product differentiation as a monopolistic element, and the preferences of consumers for variety, and the possibility of firms to change their product, or of new firms to enter, as the competitive elements. Thus, the Marshallian gap in the explanation of the long-run equilibrium of the firm was filled by making monopoly and competition compatible in a partial equilibrium set-up.

Several criticisms were immediately addressed to the new theories, but we would have to wait until the sixties for its demolition. A first set of critiques points towards the internal consistency of the functioning of the model.

First, let us consider an exercise in comparative statics. As to the relationship between the elasticity of the dd' curves and the number of firms in the group, Kaldor [1935; 1938, 84-6] pointed to the likelihood that the density of product varieties will increase the elasticity of each producer's dd' demand curve. Therefore, with entry of

new firms (brands), if we assume that demand doesn't change, then the shift of the DD' curve to the left goes with the dd' curve becoming more elastic. If we consider an increase in demand, however, the DD' curves move to the right, but the entry of new firms shifts them back to the left; the direction of the effect on equilibrium price and size of plant depends on the effect of market share on the dd' curves, which is not known (cf. Archibald [1961, 16-8]). The reason for this inability to predict arises because the relationship between the DD' and dd' curves is not specified. This argument is limited, though, to the variables price and quantity (capacity) and it omits advertising expenditure or quality which are integral variables to the monopolistic competition model. Comparative statics dealing with two variables at a time failed to recognize for long that the model is empty in regard to predictive power. If these other variables are added to the analyses as they should be since they belong in the model, problems with comparative static exercises become compounded. In fact, Archibald [1961 and 1967] showed that this model is unsuitable to qualitative comparative static predictions, either for the case of the equilibrium of a firm taken in isolation, or for the equilibrium of the group.

Second, Chamberlin's recognition of differentiation notwithstanding, his assumptions²⁴ of 'uniformity' of demand and cost conditions throughout the group, and of 'symmetry' (the effects of the adjustment by one firm impact evenly throughout the group) clearly affected his construction. And the reasons are that uniformity is only compatible with product homogeneity and, hence, horizontal demand curves; and that

²⁴The fundamental assumptions adhered to as a first step in the large-group analysis were two: first, "[i]t is required only that consumers' preferences be evenly distributed among the different varieties"; also, the symmetry assumption as to the numbers problem, "...we assume *for the present* that any adjustment of price or of "product" by a single producer spreads its influence over so many of his competitors that the impact felt by anyone is negligible and does not lead him to any readjustment of his own situation." [Chamberlin, 1933, 83]

symmetry is incompatible with competition among heterogeneous products. If the first assumption is abandoned there will be profits throughout the group in equilibrium, and if the second is abandoned the oligopoly uncertain outcomes are present, and we are unable to define equilibrium for the group. Both assumptions in conjunction imply that "...we cannot have downward sloping demand curves *and* the tangency solution together" [Archibald, 1961, 6; on Stigler, 1949, 313-4].

Also, the concept of industry fades away when differentiation and 'general' impact of each firm's adjustments on competitors are brought together; since the distinction between large and small cross elasticities is an empirical question, the critique goes that theory is left with no intermediate concept between the firm and the general market. This is where Triffin's argument sets in, even though his proposed solution does not escape the exact same problem of mixing together differentiation and the symmetry assumption; allowing for differentiated units as the molecules of the general market, he only pretends the problem soluble by posing it at a larger scale.

Furthermore, beyond the methodological choice of partial versus general analysis, a real problem is whether the individual firm is theoretically viewed as facing a horizontal or falling demand curve. And here there is no basic change from Chamberlin to Triffin. As seen in this perspective, the question would boil down to parametric pricing in competition versus pricing on the basis of full information about demand schedules in an economy made up of competing monopolies.

Another line of criticism to monopolistic competition stems, however, from the use of the perceived, subjective or conjectured demand curve. Hicks [1935] surveys the state of the art immediately after the main contributions towards the solution of the above

referred Marshallian gap had been proposed.²⁵ Hicks is very skeptical about these innovations. His doubts on the usefulness of the new "apparatus" derive mainly from the subjective character of individual demand curves confronting a monopolist, or for that matter any competitive firm that cannot maintain the belief that output has no limits, for demand reasons.²⁶ In monopolistic competition, the perceived demand curve is introduced in order to explain adjustments to equilibrium; the question arises whether the firm is supposed to perceive demand correctly at equilibrium only or whether information of the full schedule is necessary, which will be dealt with later (Chapter V, and Appendix Note F).²⁷

²⁵In its limited scope, the survey looks quite appropriate as of today; see, for instance, Franklin Fisher's [1979] *Diagnosing monopoly*, where Hicks [1935] is the only reference on the subject.

²⁶"Whether competition is perfect or imperfect, the expansion of the individual firm will be stopped by factors which are purely subjective estimates ... by rising subjective costs, or costs of organization; ... by an estimated downward slope revenue curve. Objective facts give us no means of distinguishing between them" [Hicks, 1935, 382]. We are interpreting Hicks' judgement in broad terms, though. His focus is on long-run equilibrium of the firm, and we are extending his rationale to the short-run decision problem - which is the one of interest to us, here.

²⁷Under the symmetry assumption, the perceived demand curve is obliterated, since no consideration is finally paid to the question of adjustment of the individual firm in isolation (cf. Chamberlin [1933, esp. 89-93]). Otherwise, if each competitive firm is observed facing a particular inference problem, uncertainty has to be dealt with. Arrow [1959] envisages the problem and poses the right questions. Uncertainty is pervasive since in the process of adjustment the individual demand curve is shifting while the firm is attempting to infer it; and in order to know the 'whole' demand curve (which is required of the 'now' monopolist as a profit maximizer), a premium is put on the acquisition of information, beyond that on the prices and quantities that the firm can itself gather (cf. Arrow [1959, 46-7]). But Arrow stops short of the question whether the demand curve is the real or a conjectured one.

If the correct demand curve is, for whatever reason, deemed unknowable -- for instance, the frequency of shifts or, (and consequently) experimental limitations, may prevent the monopolist to know present or lagged demand curves -- the monopolist, in order to approach maximum profit, may have to do with the adjustment of a conjectural demand curve (conjectured in the light of a sequence of sales and price data); which can be shown as tending toward the 'true' equilibrium (cf. Clower [1959]).

Nevertheless, more often than not price adjustment is analyzed on the basis of certain information on the demand curve, be that of the monopolist (e.g., Barro [1972]) or of the competitive firm (e.g., Phelps and Winter [1970], where individual firms face a share-of-the-market demand curve; and the rate of change in each's firm proportion of the total customers is a function of the moments of the (customer-weighted) distribution of other firms' prices; the element of subjectivity introduced being the 'simplification' of the objective law that determines customer flows, that a firm will only pay attention to the average market price).

Despite Hicks' undermining the bridge from Marshall to Chamberlin by exposing the problem of uncertainty, construction went forward. In fact, Hicks played a double role for the reason that his critique of the apparatus of the falling demand curve goes with a defense of the sufficiency of the perfect competition and the monopoly models for the analysis of markets, and consequently he stands for Marshall's dichotomy (Stigler's view is more clearly so). But, meanwhile, since he comes to subsuming competition under general equilibrium, his criticism of imperfect competition was without consequence (even in his own research²⁸). This time Triffin comes to underpin the argument with the Walrasian framework, so that we come circling back from Marshall to Walras.

From Chamberlin to Walras

Triffin's role was to draw the logical consequences of what he thought was the main contribution of monopolistic competition theory, the interdependence of firms:

As soon as substitutability becomes imperfect, each competitor may choose to charge either a higher or a lower price than any of his rivals. Although the range of freedom may be more or less narrow, this is only a matter of degree. Monopolistic competition throws us into the stream of general competitiveness between non-homogeneous products. In kind, the theoretical problems to be dealt with will be the same, no matter the degree of that heterogeneity, no matter whether the firms would be classified as belonging to the same or different industries. Particular equilibrium methodology is no longer of any help. We may just as well face immediately the problem of general economic interdependence, as presented by Walrasian theory, rather than sacrifice generality without being rewarded by any gain either in simplicity or in definiteness. [Triffin, 1940, 86; see also 3 and 88]

²⁸See Hicks' *The Process of Imperfect Competition* for the "assumption of a stationary state of demand for the products of the industry" [1954, 53] where "[i]t is assumed (for there is no advantage in assuming the contrary) that actual demand during the ... period coincides with expected demand." [43]

That is to say, the argument goes that given the theoretical difficulties of confining an industry, the abandonment of partial equilibrium analysis was thought theoretically inadequate and "...the general theory of economic interdependence has to be constructed so as to encompass interrelations among all firms in an economy" [Negishi, 1987, 535]. This solution, by pushing the argument forward for the sake of generality, goes at the high cost of turning meaningless the concepts he bases the argument on. Triffin is not referring to firms and to industries, these are only mere 'dummy' indices; even the concept of a firm may not withstand the critique to the question of the group, for with general product heterogeneity it seems that only the single unit fits; moreover, he fails to realize that rivalry is an empty concept in his purely virtual construct of purely virtual competitiveness; and his reference to the Walrasian theory seems misplaced since in general equilibrium analysis there is no direct awareness of competition, or choice of "a higher or a lower price" by competitors, only of a central market-maker.

The consequences of Triffin's purification of price theory were profound, though. "Modern theories of monopolistic competition and general equilibrium such as Negishi (1961), ... Arrow and Hahn (1971), ... should be seen in this historical perspective" [Negishi, 1987, 535]. Thus, there is a deflection towards general equilibrium, which certainly eventually came to hamper the development of standard economics along the Marshallian tradition (see Leijonhufvud [1974]).²⁹

²⁹According to Weintraub [1991], a shift in the meaning of the word "equilibrium" occurred which may be traced in the works of Hicks, Samuelson, and Arrow-Debreu.

"Hicks [1939] offers two images of "equilibrium". The first is associated with mechanics and is impersonal in tone (e.g. "in balance", "equally opposed forces"). The second brings to mind individuals acting as if in harmony with one another...". One speaks of a "market" and the other of a "person"; "the market equilibrium was associated with Marshall, whereas the more individualistic alternative was associated with Walras..." [Weintraub, 1991, 100-1]. And "[Hicks] believed that his method of analysis

Markets (the group, or industry, in Triffin's words) are entirely dispensed with for theoretical purposes and relegated to empirical observation:

In the restricted place where it is now confined, the concept of group, or industry, acquires a significance entirely foreign to the significance it had with the classicists. [...] It is now seen to be merely the outcome of an empirical investigation, a summary of factual findings. It does not give us any additional knowledge. It opens no avenue to theoretical reasoning. All it does is to crystallize into convenient moulds the results of our market observations. [Triffin, 1940, 89; see also 188]

Theory and factual analyses are compartmentalized (Triffin [1940, 189]). Theory, being drawn from arbitrary assumptions, is unsuited to the analyses of the variety of concrete cases; therefore, their individual aspects would be more advantageously analyzed with attention to relevant factual information and less to general theory. Our criticism is very much in line with Triffin's coherent concluding remark that: "The present stage of pure theory appears undoubtedly very formal, lacking in concrete content and practical significance." [189]. It is a sad, though unsurprising, outcome that no place for a theory of markets would be left, and that industry analyses would be deprived of guidance from the existent standard price theory. General equilibrium can only go together with individual actors, consumption and production units, so that interactions in the economy conflate to a single marketplace (where multiple or general coincidence

added a Marshallian dynamic theory to the static theory of Walras...".

Also, according to Weintraub, Samuelson intervened and "...obliterated the distinction between equilibrium as a behavioral outcome and equilibrium as a mechanical rest point", "for if one were careful in defining (mathematically) the notion of a static system, then both interpretations would collapse to a simple formal definition" [103]. "Indeed, from the standpoint of comparative statics, equilibrium is not something which is attained; it is something which, if attained, has certain properties" [Samuelson, 1947, 9].

Finally, with Arrow and Debreu "the language is not "equilibrium is a supply-demand balance," but rather "where in equilibrium, supply and demand are in balance." And "the "supply-demand balance" is thus what remains of the older images of balance beams and forces. It serves, simply put, as a reference point for some fictitious market-maker to tell the players to keep on playing, for they are not yet coordinated. If, indeed, all agents were to get this information for themselves, from their own actions, then the supply-demand balance idea would not be associated with equilibrium except after the fact..." [Weintraub, 1991, 107].

of wants is obtained by way of a synchronized direct multilateral barter exchange); in fact, the assessment of the logistics of trade is not easy, and may be rather long-drawn-out (see #4.3.3). Markets as organized by traders in order to facilitate exchange disappear, and with them the concern with the flows of information and the logistics of exchange vanishes.³⁰ At this time, there was no recognition that general equilibrium in the Walrasian mode left no room for any market arrangement but that provided by an "auctioneer," and that this implied sidetracking any assessment of intermediaries in markets and, hence, adherence to centralized coordination of exchange. This was not so in Marshall's discussion of the competitive industry where there is a crucial role for intermediaries (merchant-middlemen) which is to relay information among firms in the industry and consumers (although the role of the firm was not integrated in the working of the market). They hold inventories, put orders and attend to the bargaining process. The role of trader agents, or of firms, in creating markets so organized as to allow for the working of competition may be the starting point in bridging the void among individuals in the market.

Triffin's endeavor to deliver a general theory, or as Fisher [1989, 117-8] puts it "generalizing, as opposed to exemplifying," may very well be perfectly legitimate. In fact, there is no general theory explaining the "context" in which agents act and how markets operate:³¹ theories of monopoly, monopolistic competition as well as all breeds

³⁰Rejected markets were adopted by the fledgling specialized discipline of industrial organization. Even though we should have in mind that it is not methodologically unified, standard accounts commonly suffer from the same fault: firms and consumers are the basic elements of the analysis, the market in between conflated in an undefined way. Markets, and their intermediation structures, are sidetracked; that is to say, distribution channels and the structure of retail trade are not object of even cursory interest, in most accounts of them.

³¹Which possibility of building is an open question.

of oligopoly rely on stripped-down constructions that do not allow for generalizations. But Triffin's apparent success in providing a general theory came at a high cost, of totally doing without such context, of clearing any meaningful allusion to institutional settings, unless we are prepared to accept the "Walrasian institutional setting" as such.³² Be as it may, we might indict Triffin for outlining the obituary of markets in standard price theory.

All could be just an outgrowth of the manner static theory of pricing would have to evolve if theoretical purification were ever to be attained. Why pay attention to context in formal static general equilibrium analysis? The case is different in models where "...timing and information structure faced by firms" require "constructing" [Fudenberg and Tirole, 1987, 176]. Understanding adjustment processes quite possibly begs the definition of context and can only be worked out along such lines.

3.3 - Equilibrium states and adjustment processes

Price theory evolved from the thirties on in a misguided way and this is mainly due to the confinement of economic analysis to equilibrium configurations. The logical completeness of the general equilibrium approach was as much a challenge as a promising basis to frame the research agenda, and this may explain its overriding acceptance as the profession's canon. However, a derived result may have been that this

³²Triffin refers to Walrasian institution even though he is utterly unconscious of the clearing-house, central monitoring type of marketplace his construction on the Walrasian foundation implies. Also, see Triffin's comment on methodology, regarding "the claims and domains of "institutional" versus "theoretical" economics" [Triffin, 1940, 15-6].

predominance in focus gained currency due to a "subtle point", according to Weintraub [1985, 129]: "Specifically, perhaps the *focus* on equilibrium can lead an economist to a belief that equilibrium positions are the important states to investigate" (cf. Fisher [1983, Introduction]).^{33 34}

That these analyses played their role and therefore are important, no doubt, but basic assumptions and technical apparatus devised to comprehend questions of equilibrium are not the right ones to tackle other questions of interest, namely those we are proposing to study, adjustment processes in a decentralized economy.

I am not interested in reconstructing the whole sequence of developments in price theory. The only aspect to be investigated is how the way to a refinement in economic analysis led to overcome some previous lines of research that are of interest to our topic. As seen above, Triffin is of interest here. His work conflates a trend towards such a restricted state of affairs. Exploring contradictions in Chamberlin's work, and setting the analysis of monopolistic competition in Walrasian terms, he helps subdue the Marshallian tradition.

The interest here is not documenting evolution of the general equilibrium approach from Walras and the Austrian tradition on to the Arrow-Debreu model. This is a marginal aspect to this study. The evolution we are dealing with here is one that

³³This question arises in the sequence of several quotations of criticisms by "Post-Keynesians" to the Arrow-Debreu-McKenzie equilibrium notion.

³⁴See Hahn [1970, 1] for stronger doubts about the attractiveness of the study of equilibria, and of the danger of restricting analyses to the refinement of equilibrium states, which possibility or likelihood of materializing is not even questioned.

And, also, Marshall's admonition is of interest: "The Statical theory of equilibrium is only an introduction to economic studies... Its limitations are so constantly overlooked, especially by those who approach from an abstract point of view, that there is a danger in throwing it into definite form at all" [Marshall, 1920, 461].

comes from Marshall to Chamberlin and Joan Robinson to a dead end. If Triffin's role was of recasting this tradition into a general equilibrium framework, it reflects also the vanishing of an interest in 'competition'³⁵ and markets.

A complementary question regards the above hinted fact that the study of adjustment processes requires a broadening of fundamental assumptions. Or better, it requires that some fundamental assumptions common to the Arrow-Debreu model be given a different, we would say, more concrete form. These fundamentals are knowledge and markets.

In order to understand adjustment processes of individual agents in a competitive economy (which fits into prevailing economics as adjustment to equilibrium positions, and is usually studied under stability of equilibrium), the logic of the Arrow-Debreu model is not the right choice. Assumptions on information ("full relevant knowledge") and on how individual choices are coordinated "in interrelated markets" may have enough content in the study of interdependence in a static world as in Arrow-Debreu general equilibrium (cf. Weintraub [1985, esp.109]). Not so in adjustment situations. Arrow [1959] raised the question of knowledge but he didn't notice that his question begged another one on markets: in disequilibrium, uncertainty springs up in a deeper (no more one single price) and broader (it overflows to other variables, prices are not sufficient information for decision taking) form that can only be made sense of in case of non-brokered markets. Otherwise, in centralized markets such uncertainty is vacuous and the

³⁵ "...what the theory of perfect competition discusses has little claim to be called "competition" at all... The reason for this seems to me to be that this theory throughout assumes that state of affairs already to exist which, according to the truer view of the older theory, the process of competition tends to bring about (or to approximate) and that, if the state of affairs assumed by the theory of perfect competition ever existed, it would not only deprive of their scope all the activities which the verb "compete" describes but would make them virtually impossible." [Hayek, 1948, 92]

problem of adjustment has a narrower interest in theoretical terms. Thus, markets are due some content, which Arrow-Debreu models dispense with.

From this broad picture, two lines of inquiry arise: one is to explain how inattention to markets evolved, as well as to show how exercises on price adjustment were proposed and solved without regard to this logical gap, that in disequilibrium states information and market arrangements need content; another is to explain how agents and markets would work in adjustment situations.

CHAPTER IV

ON MARKETS

4.1 - Markets as institutional arrangements

In standard price theory, market stands as the organizational focus for the study of interdependence in exchange, the theoretical program of which dates back to Adam Smith's "invisible hand".¹ Demsetz describes the problem that the "hand" is supposed to address as "whether extreme decentralization leads to chaotic resource allocation."

Referring more to modern theory than to Smith, Demsetz then adds:

Perfect decentralization is realized theoretically through assumptions guaranteeing that authority, or command, plays no role in coordinating resources. The only parameters guiding choice are those that are given - tastes and technologies - and those that are determined impersonally *on* markets - prices. All parameters are beyond the control of any of the model's actors or institutions, so these

¹The "market" plays a role in Smith's *The Wealth of Nations* but he is vague as to its organization. For instance: "The town is a continual fair or market, to which the inhabitants of the country resort, in order to exchange their rude for manufactured produce. It is this commerce which supplies the inhabitants of the town both with the materials of their work, and the means of their subsistence. The quantity of the finished work which they sell to the inhabitants of the country, necessarily regulates the quantities of the materials and provisions which they buy" [Bk.III, Ch.1, 4]. (See Coase [1977, 320-1] on the institutional basis for the working of the price system in *The Wealth of Nations*.)

Market here just means interdependence, and the "invisible hand" [Bk.IV, Ch.2, 9] the energy that drives exchange among interdependent individuals. Only cursory attention is paid to the mechanisms of exchange proper. Moreover, "market" is taken for granted as the 'setting' where the market price is obtained. "The market price of every particular commodity is regulated by the proportion between the quantity which is actually brought to market, and the demand of those who are willing to pay the natural price of the commodity." [Bk.1, Ch.7, 8]

assumptions effectively deprive authority of any role in allocation. They are fully justified by the theory's remarkable yield - a compact, coherent, subtle yet simple model for deducing the equilibrium consequences of extreme decentralization of resource ownership. [Demsetz, 1988, 160, italics added²]

Despite some misplaced use of the notion of institution, as well as the hazy use of the notion of decentralization (see #4.3), Demsetz's point may be granted. What he presents is the bare bones of modern microeconomics: (i) firms as model "agents," embodying parametrical technologies, and (ii) markets as institutions that impersonally determine prices. Firms maximize profit with no information, information processing or management costs. More from Demsetz:

...the model sets the maximizing tasks of the firm in the context in which decisions are made with full and free knowledge of production possibilities and prices. The worldly roles of management - to explore uncertain possibilities and to control resources consciously, where owners of such resources have a penchant for pursuing their own interests - are not easily analyzed in a model in which knowledge is full and free. "Firm" in the theory of price is simply a rhetorical device adopted to facilitate discussion of the price system. [Demsetz, 1988, 160-1]

Furthermore, allocation is obtained by means of an institution, markets in which no transaction costs are incurred by any agent. But, as we saw above (#3.2), on these assumptions markets vanish from standard price theory to be left with only "the general market," which can only be conceived as a common meeting point³ where the allocation problem is impersonally solved to determine prices. Like the firm, markets or the

²Arrow's [1994, 4] answer to the question "What individual has chosen prices?" in the general competitive equilibrium model is: "In the formal theory, at least, no one. They are determined on (not by) social institutions known as markets, which equate supply and demand."

³This interesting image is adumbrated in Edgeworth [1881, 18] while establishing his concept of competition (or, better, the necessary and sufficient conditions for a competitive price): "There is free communication throughout a *normal* competitive field. You might suppose the constituent individuals collected at a point, or connected by telephones - an ideal supposition, but sufficiently approximate to existence or tendency for the purposes of abstract science."

general market are properly envisioned in standard price theory as merely a rhetorical device,⁴ which for lack of being an actor could only be labelled as an institution. Since no agent can possibly solve the suggested coordination problem in this "decentralized" setting, only some disembodied entity could be assigned that role. "Institution" is as good a label as any other, it is just devoid of theoretical or empirical content.

It being granted that not all economic problems can be tackled with vacuous notions like "the firm," and "the institution" of markets,⁵ I propose to consider the further point whether we can find a theoretical basis to understand the emergence and working of trading arrangements brought about by economic agents.

In general, my view is that both markets and firms are specialized coordination devices, respectively the interfirm and the intrafirm modes. As Winter has stated the matter:

Orthodox theory recognizes two aspects of the problem of coordinating economic activity, the interfirm aspect and the intrafirm aspect. Markets are shown to be the answer to the interfirm aspect. What the answer to the intrafirm aspect may be is not explicitly addressed but presumably it is contractually based authority of the "entrepreneur." However, since the functioning markets and the firm-qua-production sets are given data of the theory, there is no opportunity for an analysis of the division of labor between these two coordination modes. Hence, as Coase observed, there is no question of why markets do not do the coordinating that firms do, as no answer to the obverse question of why one big firm would not work as well as a market economy. In short, textbook orthodoxy

⁴A similar comment about markets as "a figure of speech" is proffered by Tobin [1980, 796].

⁵In the course of his discussion of the neglect by economists of the "internal arrangements within organizations" and of their concentration on the determination of prices in the market, Coase makes this same point, that in modern economic theory "[t]he firm and the market appear by name but they lack any substance. The firm in mainstream economic theory has often been described as a "black box." And so it is. [...] Even more surprising, given their interest in the pricing system, is the neglect of the market or more specifically the institutional arrangements which govern the process of exchange" [Coase, 1992, 714].

A brief comment on "[a] market as an institution for the consummation of transactions" can be found in Stigler [1957, 245], where he deplores "...that ... a market is commonly treated as a concept subsidiary to competition."

provides no basis for explaining the organization of economic activity. [Winter, 1991, 182-3]

This raises two questions, one which Coase took up, the other which he passed by. The first question is "...which transactions would be organized by which mode of organization and why"⁶ [Williamson, 1991, 7], and this can be addressed in terms of the comparative account of Coasian transaction costs⁷ and the costs that will have to be incurred with alternative modes of coordination. This is a question of production management (or production allocation): where are specific transactions relevant, in the market, the firm, or hybrid organization? That is to say, to what extent will costs be internalized? According to Coase, to answer this question "...we still have a long way to go" [Coase, 1988a, 67]. More to the point, we might ask why any of this is relevant anyhow; surely we economists need be concerned only with what goes on 'before' and 'after' output is produced, not with the particulars of production engineering or management.

Of course, this is altogether different from saying that Coase explained the existence of "the firm." In fact, Coase dealt only with the internal organization of the

⁶This was not the question Coase proposed to answer. Coase's concern in *The Nature of the Firm* was "[i]nstead, a very general comparison of the benefits and costs of firms (in relation to markets)" [Williamson, 1991, 7]. See Coase [1988a, 63; 1992, 718] for his conceding the "hardly surprising" shortfall that in the early thirties he couldn't have attempted a systematic incorporation of transaction costs into economic analysis.

⁷These are costs of "...using the price mechanism. What the prices are have to be discovered. There are negotiations to be undertaken, contracts have to be drawn up, inspections have to be made to settle disputes, and so on" (Coase [1992, 715]; see also [1937, 21-2]). As far as I could read, I couldn't dispel the doubt if these are not set-up costs. In Coase there is apparently no awareness of the fact that transaction costs only impinge upon the workings of coordination if they are set-up costs, i.e., costs that are lump-sum, since largely independent of the amount contracted or transacted; otherwise, they explain nothing. However, Coase [1937] leaves the matter undecided: for instance, referring to labor services contracts [21-2] he is better understood as dealing with set-up costs, though the opposite happens in the case of, e.g., costs of organizing spatially [25].

firm, i.e., the internalization of costs, and provided no foundation for explaining the emergence or existence of the firm, Coase's claim to the contrary ([1937, 20]; [1988b, 6]; Clower and Howitt [1993b, 14]; notice, however, that Coase's more recent view is different [1992, 715-6]). The firm is assumed to exist, and costs of coordination within or, alternatively, outside the firm (the price mechanism) are assessed. I think transaction costs are, in fact, central to explain the emergence of intermediation, and the organization of trading arrangements; but this may have to start from the analysis of the execution of exchange⁸ (see Coase's [1992, 716] mention of money as reducing search and transaction costs of barter exchange). Therefore, we cannot say that Coasian transaction costs added fresh content to the firm as a theoretical entity.

The second question is deeper. After transaction costs enter the analysis of the pricing mechanism and the firm is *ex hypothesi* introduced into the construction, can we still treat markets as given? And are the supposedly different entities,⁹ the market and the firm, theoretical primitives? I think not (cf. Clower and Howitt [1993b, 14-5; 1994, 25-26]).

⁸In order to explain intermediation, production is a doubtful accretion. There is no need to fuss about exchange versus production economies, and we should be content with Clower's view as quoted in Joan Robinson: "An ongoing exchange economy with specialist traders is a production economy since there is no bar to any merchant capitalist acquiring labour services and other resources as a 'buyer' and transforming them (repackaging, processing into new forms, etc.) into outputs that are unlike the original inputs and are 'sold' accordingly as are commodities that undergo no such transformation. In short, a production unit is a particular type of middleman or trading specialist." [J. Robinson, 1977, 6]

⁹Coase was aware in *The Nature of the Firm* that "...it is not possible to draw a hard and fast line which determines whether there is a firm or not. There may be more or less direction" [Coase, 1988a, 55]; on this basis, he rebuts a criticism by Klein, Crawford and Alchian [1978] who found that Coase's "...primary distinction between transactions within a firm and transactions made in the marketplace may be often too simplistic. Many long term contractual relationships (such as franchising) blur the line between the market and the firm" [326].

But Coase's theoretical point is that "[t]he existence of such mixed relationships does not mean, for me, that we should abandon the view that "the distinguishing mark of the firm is the supersession of the price mechanism," as I put it in "The Nature of the Firm" [Coase, 1988a, 55-56].

For the sake of the argument, let us suppose that Coase's analysis could explain the existence of the firm. Having included transaction costs in his analysis, Coase is led to think of the firm in isolation from the price mechanism. Then we have a firm deciding¹⁰ whether to carry out a transaction within the organization, or through the marketplace. The firm economizes on transaction costs and this allows for the definition of the scope of its activities, internalizing transactions otherwise carried out through the open market or through another firm. On this procedure markets are assumed, not explained, not integrated in a theoretical construction built upon transaction costs. There is an organized market out there through which the firm can sell its product, or from which it can obtain desired inputs. Simply put, Coase gives us no theory of markets, no account at all; and without an explanation of markets, which Coase mistakenly treats as pre-existing the creation of firms, he lacks a necessary foundation for his treatment of the emergence of firms.

A note on Coase's view on markets is due at this point. My first contention is that all of Coase's writings (as well as the major part of the literature that has sprung up from his insights) are centered in production rather than exchange (see *The Nature of the Firm* [1937], Introduction to *The Firm, the Market, and the Law* [1988b], his [1988a] reflections [Williamson and Winter, 1991], and his [1992] lecture). Moreover, Coase treats markets as organized markets in the fashion of the Chicago Mercantile Market or the London wheat market. As to the first aspect, his explanation of how his approach "...succeeded in linking up organization with cost" [Coase, 1988a, 47] involves mainly

¹⁰Whether it is a decision or the result of an evolutionary weeding out process is not relevant at all.

the consideration of production activities of the firm. Much more significant, though, is his discussion of weaknesses in *The Theory of the Firm* (cf. Coase [1988a, 67]). Let me put it this way: if transaction costs are considered, and firms are formed so that costs of conducting transactions through the market are thereby avoided - i.e., "...if the costs avoided were greater than the costs that would be incurred by the firm in coordinating the activities of the factors of production" - then certain transactions are carried out within the firm; and their inclusion in the internal organization of production replaces the market. Coase acknowledges that he didn't try to indicate determining factors of that choice between organization within the firm or through the market; he just invoked grounds for the reasonable assumption that costs of coordinating factors of production within the firm could often be presumed comparatively lower. Furthermore, in order to cope with such limitations, Coase raised the need for a theory to explain "... what the institutional structure of production will be. That depends on which firms can carry out this particular activity at the lowest cost and this is presumably largely determined by the other activities that the firms are undertaking" [Coase, 1988a, 67]; yet, he admits in *The Institutional Structure of Production* [1992, 718] that his lack of indication of such "factors" has made it difficult for others to incorporate transaction costs in such a way as to support construction of a satisfactory theory. Coase's focus throughout has been not the organization of markets by firms but the organization of production within firms.

My second contention is that Coase focuses too much on organized commodity exchanges and too little on commonplace entrepreneurial market-creating activities. Despite Coase's statement that "[t]he provision of markets is an entrepreneurial activity" [Coase, 1988b, 8], his consideration of exchange revolves around organized markets.

Markets are organized by traders in order to reduce transaction costs, be it "fairs and markets" or "commodity exchanges and stock exchanges"; and only as an approximation to such "perfect markets", is decentralized exchange called forth (pp.8-10). Institutions are set up that require not only "...the provision of physical facilities" but more importantly "...the establishment of legal rules governing the rights and duties of those carrying out transactions in these facilities" [10].¹¹ Nonetheless, Coase's view in his Nobel lecture [1992] is well balanced: "It makes little sense for economists to discuss the process of exchange without specifying the institutional setting within which trading takes place...", as is the case "...when trading takes place outside exchanges (and this is almost all trading) and where the dealers are scattered in space and have very divergent interests, as in retailing and wholesaling"[Coase, 1992, 718].¹²

It being granted that Coase's explanation of *The Nature of the Firm* is weakened by his presumption that markets pre-exist the creation of firms, then to carry the argument to its logical completion we should dismiss the assumed presence of the open market and explain its emergence in a decentralized economy. If we are to explain the emergence of markets as created and maintained by specialized agents, we complete the whole construction with "firms" that are market-makers. The existence of "markets" does not precede the "firm's" existence, both have the same origin in the activities of

¹¹Legal rules that "...may be made by those who organize the market, as in the case with most commodity exchanges", or otherwise that "...have to depend ... on the legal system of the State", which applies "[w]hen these facilities are scattered and owned by a vast number of people with very different interests, as in the case with retailing and wholesaling" [Coase, 1988b, 10]. See also Coase [1992, 718] for the same distinctive role of "private law" and the laws of the State.

¹²Coase adds: "The time has surely gone in which economists could analyze in great detail two individuals exchanging nuts for berries on the edge of the forest and then feel that their analysis of the process of exchange was complete, illuminating though this analysis may be in certain respects." [Coase, 1992, 718]

agents who incur costs in order to reduce transaction costs in exchange.

"Markets are institutions that exist to facilitate exchange, that is, they exist in order to reduce the cost of carrying out exchange transactions" [Coase, 1988b, 7], but they do not preexist exchange transactions. They are created by means of specialized agents who make or devise market arrangements to earn income as the condition for their activity to succeed or survive.

That is why in a decentralized economy markets have to be explained and not just taken as unquestioned presuppositions. A first step toward explanation is to ask how exchange might be organized so as to be less "clogged and embarrassed in its operations."¹³ This is addressed in Alchian [1977], Chuchman [1982], and in Clower [1977; 1994a; 1994c], Clower and Friedman [1986] and Clower and Howitt [1994, 14-5]). The essential point in all these papers is that the emergence of intermediation in exchange depends crucially on the existence of set-up transaction costs (i.e., costs that are in large measure independent of quantities traded). The existence of such costs not only creates a reason for middlemen to emerge, but also encourages the provision by middlemen of specialized trading services. That is to say, set-up transaction costs not only explain the emergence of market arrangements but also explain why particular kinds of specialization ("monetary exchange") are a ubiquitous characteristic of every ongoing

¹³Adam Smith recognized clearly this problem with barter exchange, but his idea was different. He stated [Bk.I, Ch.4, 1-2] that the use of a commonly accepted commodity, by making exchange less "clogged and embarrassed in its operations," will permit an extension of the division of labor. In Smith, economies of scale in production can be better exploited if the market is extended by means of monetary exchange. (This could be extended to the case of "specialists in trade," as in Ostroy and Starr [1990, 29]: "Among the forms of specialization we expect to see in a low transaction cost economy is specialization in the transaction process itself. [...] Consistent with Smith's viewpoint, the distinct function of intermediary agents can be explained by scale economies in transaction costs.")

Here, the reasoning is that set-up transaction costs (and economies of scale in exchange) lead to intermediation. The further idea that monetary intermediation may allow for a better exploitation of economies of scale in exchange is Smith's, but requires explanation. In any case, the two aspects need to be dealt with separately.

market economy.

The role of transaction costs in intermediation is first attempted an explanation in Hirshleifer's *Exchange Theory: The Missing Chapter* (Hirshleifer [1973] and also [1980, Chs.7 and 8]). Hirshleifer shows that proportional exchange costs create a gap between the selling and buying prices of prospective transactors, and hence *room* for intermediation. The gap "...can be thought of as the price of "middleman" services" which "...are assumed to be competitively supplied", so that, in general equilibrium, "...the implied gap G must be such that middlemen are induced to provide exactly the requisite quantity of [demand for middleman services]" [Hirshleifer, 1973, 135 and 137].

This point is more clearly treated in Demsetz [1968]. He asks whether transaction costs are affected by the scale of trading in the New York Stock Exchange (NYSE). In transaction cost he includes brokerage fees and ask-bid spreads; the latter are paid to specialized intermediates "[t]o cover the cost of standing ready [...] to sell or buy at stated prices immediately upon receipt of a matching order." Middlemen provide a service of "immediacy": "If buy orders and sell orders could be counted upon to arrive simultaneously, ... there would be no demand for the services of persons to stand ready and waiting" [Demsetz, 1968, 36-7]. The ask-bid spread of intermediated exchange (by brokers or specialists, though we need not consider risk-taking here) will be comprised between two (theoretical) equilibrium points, which make an ask-bid spread of non-intermediated exchange: one, the equilibrium ask price, determined between "...those who desire immediate purchases" and "...those who stand ready and waiting to sell to those who demand immediate servicing of their purchasing orders"; and another, the equilibrium bid price, defined in a similar way. (Among Demsetz's conclusions, the most important is that the time rate of transactions, by lowering the cost

of waiting, is the main influence on the reduction of spreads in the NYSE, which is "...a form of scale economies" on trading in a particular security [41].)

But, having provided room for intermediation, Hirshleifer then seems to fail to propose a reason for the comparative advantage of intermediated exchange as provided by middlemen; like, for instance, any 'technological' advantage on their supply of intermediation services, which we might think of as reducing the proportional cost,¹⁴ and thus would allow for a reduction of the lag as compared with the unassisted barter situation. This is not contradicted in his argument, but there is no explicit recognition of the question.

Furthermore, Hirshleifer explains the emergence of stocks of inventories of transacted goods when "...costs of exchange take the form of a fixed lump-sum *charge per transaction*" [1980, 246],¹⁵ and "[a]s before, some individuals will find it advantageous to use some or all of their resources to provide middleman services" [1973, 141]. Corresponding to this lump-sum character of exchange costs is the bunching of acquisitions and sales (and, as a consequence, holding of inventories); this creates a demand factor for intermediation, even in a world of perfect information of trading partners and their offers: if we assume a given dispersion of endowments among individuals, a buyer benefits from bunched purchases and sales, thus saving on fixed

¹⁴It seems hard to find any support for a technological advantage of the proportional type either than on "pure transfer costs".

Of "trading costs" I can think of information costs (or those that make for goodwill, as in Alchian [1977]), but this brings us into a messier world than Hirshleifer meant (see his assumption of perfect information [1980, 236]). Hirshleifer's argument is valid under perfect information and let us be so confined. In any case, in order to explain the emergence of brokers or merchants (of the proportional commission type, let us say) we might need to indicate how they allow for lower information costs in the market. But, the further question arises of whether we can think of information costs that are not lump-sum, if only to some degree.

¹⁵Beyond "...assuming some cyclical or other imbalances in productive, consumptive, or trading flows" [Hirshleifer, 1973, 138].

costs of exchange.

Therefore, for intermediation to emerge we may need either a technological advantage of intermediated supply or set-up transaction costs, independently of the consideration of another factor involving also fixed costs, e.g. imperfect information (that is beyond the case considered by Hirshleifer). Hirshleifer makes room for intermediation in the case of proportional costs of exchange but he fails to discuss the benefits brought about by middlemen in this case; we might then tentatively propose that, in order to explain intermediation and markets, we need set-up costs of exchange of informational nature.

I gather that Hirshleifer is absolutely right on "missing" exchange, but he takes markets for exchange. He seems to mix the question of existence of markets due to the presence of transaction costs, with the (observable) effect of changes in the magnitude of such costs on the survival of markets, and thus is mistaken in concluding that "...given that trading costs exist, markets can easily disappear or become non viable" [1980, 245].¹⁶ Once lump-sum costs of transacting are brought into the picture, a change in perspective is required. It is relevant here to mention an apparent contradiction between the view in Clower and Howitt [1994] and Coase (cf. Coase [1992, 716]), and the literature on "missing markets" (cf. Hahn [1989a, esp.1-2]). The first view is that the existence of set-up costs of transaction fosters the emergence of markets - so organized by traders as to economize on such costs. The literature on missing markets argues that the existence of set-up costs explains the non-existence of markets - as provided by godly

¹⁶Another instance where Hirshleifer seems to take markets for granted - and the difference between exchange and market is unclear - is his view of monetary exchange: "As compared to barter, the system with a medium of exchange will have lower trading cost in proportion, but possibly larger trading cost in total due to the enormously greater volume of transactions" [1973, 144].

decree. As Arrow puts it: "Transaction costs are the costs of running the economic system," which "...in general impede and in particular cases completely block the formation of markets" [Arrow, 1969, 48; from Williamson, 1987, 590]. More specifically, Hahn notes that "...the more finely time is divided, the more goods and transaction dates there are. If we had allowed for set up costs (and increasing returns), we could argue that to have markets at every t for all goods dated $t' \geq t$ must always use more resources when time is more finely divided. In that case one may be able to show that in any equilibrium many markets will be inactive" (Hahn [1971, 436]; see also [1973a, 15-6]). But this only begs the question of why they should be active in the first place. However, before this question is tackled two comments are in order. First, without explicit consideration of the logistics of exchange¹⁷ there are no a priori grounds to believe that an Arrow-Debreu economy where all contracts, for present and future exchange, are carried out at a single date involves a smaller number of contacts (both contracts and transactions) than one with contracting at every date. Second, that markets may vanish, as brokered markets in case of hyperinflation have, is an empirical fact that is good to explain, but is not the same question as the one here. Here the question is why do we see markets to start with, not why exchange in some dynamic juncture may suffer certain adaptations, which compromises the viability of a market. In any case, let us attempt an explanation inspired in Demsetz [1968]. To begin with, let us assume that transaction costs have a lump-sum component. If we would imagine a world without specialized intermediation in exchange (e.g., commodities or securities markets), in case

¹⁷Except for positing "technologically feasible" marketing activities at each date (t), "fully integrated, ...under the control of a single firm" [Hahn, 1971, 428], which I cannot distinguish from the case of multilateral exchange with the central market.

of increased uncertainty in hyperinflation conditions the willingness of traders to stand ready to meet counteroffers to trade immediately (cf. Demsetz [1968, 35-7]) would be drastically reduced, so that the (theoretical) spread between the (unassisted, or non-brokered) equilibrium ask price and the equilibrium bid price could contract to such a degree that it would lie within the bid-ask spread that pays for the survival of brokers. The organized market is, therefore, compromised.

Be that as it may, the aforementioned distinction between the literature on "missing markets" and the view here is just false. One perspective is that the world as envisioned in its purity should conform to the needs of the theorist (its creator);¹⁸ if we lack a few prices, and consequently a few markets where they presumably would be asserted, then (an oversight by the theorist?) some factor must explain that omission. Transaction costs. The other is that the economy is opaque to individual traders, and that we attempt to bring some order to what we perceive in it. If we have markets at all then we must think in the first place that their working is paid for by costs they supersede; and the costs we can make sense of for their emergence are set-up transaction costs.

There is a more interesting implication of this argument. Everything would be just right if, instead, we talked about 'missing exchanges' (or even, with a different meaning, 'missing prices'). The trivial fact that transaction costs of the set-up type reduce the volume of transactions has nothing to do with markets, or impediments to their functioning. If transaction costs were absent why would any organization of trade be necessary, what would trading posts, and specialists, merchants or even brokers be

¹⁸"...gaps in the traditional theory. In particular, it is now widely recognized that it postulates there to be many more markets (...) than we observe. 'Missing markets' lead to reformulations and questions. The economy has to be studied as one in which there is trading at every date." [Hahn, 1989a, 1]

doing there?

The economy envisioned in Debreu's account of general equilibrium analysis relies on m entities who maximize utility by planning a set of trades *given* the accounting (numéraire) prices of n commodities, for t market dates in a single "general market"; ignoring contingencies and locations, we have $((n-1) \times t)$ exchange rates. For aggregate consistency of plans, prices must be the same for all prospective transactors, and for this it is also convenient that they be given independently of the quantities proffered for trade, and known; independently of the specifics of the logistics of trade, we might accept that the $((n-1) \times t)$ prices are freely known and adhered to in exchange. Now, in a world without transaction costs it is a matter of indifference whether there is centralized multilateral barter (cf. Jaffé, ed. [1954, Lesson 12]; Hicks [1939/1946, 58ff: "multiple exchange"]; Patinkin [1965, esp.11-12,36-38]), or a set of $(n(n-1)/2 \times t)$ trading posts, at each of which the individuals may trade two commodities (cf. Jaffé, ed. [1954, 157-60]); or simply presume that pairwise or larger combinations of individuals can somehow meet and conclude desired barter (spot or future alike) transactions as a kind of "do it magically" affair! After all, if the every aspect of trading activity (search for prospective opposite parties, bargaining and closing deals) is truly costless to prospective transactors, intermediation of any kind serves no purpose that is worth paying for, so it will not be provided (neither is it-needed), so literally anything would be admissible in "the organization of trade."¹⁹ In a world without transaction costs there is no room for

¹⁹"In general equilibrium without transaction costs, the network of exchanges is indeterminate; there is no constraint on the gross trading volume," and "[t]he presence of transaction costs makes the exchange network determinate. In such a network, certain traders, in view of their lower transaction costs, probably emerge as middlemen, brokers or intermediaries. [...] Transaction costs, therefore, are the key to an understanding of intermediaries and of the structure of the markets." [Niehans, 1987, 321, and 325]

any notion that could have any resemblance to the markets we know in experience (cf. Clower [1994d, fn.9] commenting on Hahn's [1973a, 15] "empirical confrontation"). We might see multilateral barter, successive encounters in trading posts, pairwise meetings of each with everyone else in any fashion our wildest fancies might suggest (cf. e.g. Ostroy [1973], Diamond [1982a; 1984a], Kiyotaki and Wright [1989], Aiyagari and Wallace [1991]). Therefore, absent any goal, the problem of "missing markets" is a shot in the dark.

We could acknowledge that in a world with transaction costs there is economic incentive for lumps of intermediation to shape amorphous exchange. In this light, the proposition that transaction costs prevent the proper crystallization of trade in organized markets is unsound. (The wonder is that the amorphous mass has gained some shape, not that crystals don't pervade the universe.) Markets are to be explained in, not explained out, for without set-up transaction costs there is no reason to have them to start with.

If something is missing that the theorist needs,²⁰ this is prices as given to traders. But if we believe that this is the right state of affairs, to explain consistency of plans for a given common price set, then we are constructing our theory as if it were based on brokered markets, where traders know current *market* prices (spot or future, alike) and use this as a signal to issue their decisions to trade.

²⁰This is clear from Hahn [1971, 430-1]: "...many markets will be inactive in an equilibrium", but "...one is asked to suppose that prices are established for all possible markets, active or not." Also "...adjustment without prices (markets)." [Hahn, 1982, 746]

4.2 - Brokered and non-brokered markets: some general considerations

The objective here is to lay some basis for the understanding of the working of decentralized markets, the interest of which stems from the difficulty to answer "...such basic questions as who sets prices and under what motivation, and why transaction-quantities are determined the way they are" [Howitt, 1986, 77].

Standard microeconomic theory is founded upon a fictional market arrangement derived from a cleaned-up version of Walras' theory of exchange without bargaining, and 'naturally' without disequilibrium trading, i.e., as an auction that precedes actual trading. The adjustment of prices, as orchestrated by the central auctioneer, is the only equilibrating mechanism, and equilibrium is ascertained as a matter of logic as a notional consistency of plans. There is no account of pricing or trading interactions among economic agents, and market organization is not considered; decentralized mechanisms of control are therefore of interest for the simple purpose of exploring an alternative to the established, empirically blind and theoretically obscure, foundation of standard economics.

Thus, a set of questions arises which will be the unifying line of our query, throughout: How are markets organized? And who creates and runs markets in a way that facilitates the interaction among the trading decisions of the economic individuals? That is to say, who creates and runs markets in a way that the interaction among willing traders is rendered less costly than it would otherwise be if trading decisions of economic units were left to their unassisted endeavor to make double coincidence of wants and timing possible?

I believe that markets are not given and are costly to set up and to run.

Therefore, bringing them in to an analysis of exchange begs the question of the benefits they purvey, or the opportunity costs they supersede. Robert Clower's *The Fingers of the Invisible Hand* [1994a] lays out a basis for understanding how self interested economic agents may be led to specialize as middlemen and set up trade arrangements whereby markets evolve and become so organized as to reduce both search costs and transaction costs of willing transactors. Otherwise, they would tend to be autarkic.

At this point our objective is humbler. Since there is no coherent view of the workings of markets, and only very tentative theoretical accounts have been advanced that may provide a basis toward the replacement of the (neo)Walrasian fiction, we will be content only to identify market organizations of empirical relevance that may help us bring the question of decentralization to the fore.

An incredible mass of literature, all factual, is available on the workings of markets, but no analytical basis can be sifted from it. Of interest in this regard is a classification of price-making mechanisms defined in R. Cassady's *Auctions and Auctioneering and Exchange by Private Treaty*, who distinguishes take-it-or-leave-it administered pricing, private treaty pricing through negotiation, and competitive bid pricing (see Appendix Note C).

On auctions, which are "...direct extensions of the usual forms of bilateral bargaining," theory is abundant (Wilson [1992, 228]). However, specifically on dynamic double auctions ("bid-ask markets") to which commodity markets and some financial markets comply, little theoretical work has been accomplished.²¹ Among these we

²¹"Dynamic procedures, such as bid-ask markets, have received little attention although they have paramount importance in practice. [...] Scant progress has been made in building theories with generality comparable to the Walrasian model of general equilibrium, even though the enigma of price formation in the Walrasian model is a prime motivation for studies of auctions." [Wilson, 1992, 271]

should notice Daniel Friedman [1984], Wilson [1986],²² and, on commodities exchanges, Working [1967], Telser [1967], and Telser and Higinbotham [1977]. Development in this area has been chiefly motivated by experimental studies; for a recent survey on experiments on double auctions see Friedman and Ostroy [1989] and for other references, Wilson [1992, 260-1]. Among this growing literature, I would select Davis, Harrison and Williams [1993] where convergence to "nonstationary" equilibria is studied, to conclude that double auctions tend to converge quite fast, and are relatively efficient.

Furthermore, it is most typical of financial markets for double auctions to be conducted by specialists "...who maintain inventories and order books of bids and offers in order to sustain continual trading opportunities and price stability" [Wilson, 1992, 259]. Factual references to securities exchanges can be found in Osborne [1965; 1977]; and for some theory, see Wilson [1992, 255-6] and, for dealer quotation markets specifically, Reiss and Werner [1994, 6].

Some attempts at formalization on alternative intermediation contracts (merchants versus brokers) are found in Hackett [1992; 1993], though most refer to financial markets. Townsend [1978] is of interest, and a notable (more general) exception is Rubinstein and Wolinski [1987] on endogenous middlemen, as a "time saving institution" as derived from a search theoretic basis.

Factual literature is also vast on non-brokered markets. On market places, studied

²²In Wilson [1987, 56-61] this model is summarized, and the deficiencies - or better "challenging topics for research" - are clearly acknowledged. It is recognized that the result "...is implausible as a positive predictive theory" [60], namely for experimental purposes. Beyond the referred limitations of the model, I would point out this: with a known initial distribution of valuations, and admitting common knowledge of completed transactions and transaction prices (which allows for probabilistic inference of outstanding valuations of the remaining traders), the model is far away from any representation of a continuous bid-ask market. Informational and computational problems would be compounded.

especially by anthropologists and geographers, see Hill [1987] for references. On negotiated pricing, Cassady [1974] is an excellent reference. Otherwise, the literature on non-brokered markets is meager, but a few remarkable exceptions attempt some theory (elements of which will be of great help in Appendix Note F, in order to give body and behavioral content to the 'market-maker'): these include²³ Okun [1981] on "customer markets," Daniel Friedman [1989] on "producers' markets," and Clower and Friedman [1986] on "trade specialists." The latter stands as a category of its own since it brings to life figures that take on the function of organizing and running bilateral exchange, i.e., specialist traders who, acting as middlemen, lead to a decentralized working of the market.

It should be evident that with regard to market organization, several types of markets of empirical relevance exist. Our goal now is to establish a broad distinction concerning the collection and dissemination of information as well as the degree of decentralization of the price signal. Two types of market organization of empirical relevance are sufficiently contrasted for our purpose, namely brokered markets and 'decentralized markets.'

First, we consider brokered markets where trade is conducted through agents who

²³Hicks [1989, Ch.3] constitutes producers as *the* market organizers, who historically replaced the wholesalers in both functions of stockholding and price formation. (In any case, Hicks has a diverse view in *A Theory of Economic History*; although referring to an earlier historical stage of industrial evolution, Hicks considers the distinction between pure trader and producer not fundamental: "It is a technological, not an economic distinction" [1969, 28].)

But this seems an unpromising old story that had large currency in the forties. J. S. Mill in his *Principles* [1848, 246] makes a distinction between wholesale markets and other trades. Hicks, in *Capital and Growth* [1965, 55-6] and in his [1976] article *Time in Economics*, presents an outline of what became the above argument. Joan Robinson [1977] recalls Kalecki's [1939] distinction between two systems of price formation, one dominated by supply and demand and one by costs plus profits, which Hicks had recently rediscovered. She writes: "For manufactures, in modern times, the producers have taken over the merchanting function. They offer their commodities at an advertised price and produce for sale what the market will take." [J. Robinson, 1977, 18]

gather information of offers to buy or sell and match transactors at their bidding and asking prices, so that the price at which each transaction takes place is announced to other traders and is therefore the 'running price' before a next transaction is completed at a different price. Such ruling price is produced as a result of trading among buyers and sellers, although transactions are carried out through trader agents - brokers²⁴ - who trade on behalf of their customers. Buyers and sellers communicate their bidding and asking prices to brokers, and each broker has the possibility either to carry out trades between his customer-buyers and customer-sellers (i.e., crossing buy and sell orders for his customers), or to deal with any other broker that is an agent of a buyer or a seller, in order to match the orders made to him to buy or sell by his customers.

Attempting a general approximation, when a certain broker is on the market as a supplier he will attempt to trade with whoever has the highest bidding price, be it his or other brokers' customers-buyers; when he is arranging a purchase for a customer he will have a bid price and he will face asking prices by other brokers acting on behalf of their customer-sellers - he will take the lowest asking price so that he can obtain his commission (or otherwise make the largest margin²⁵).

Several kinds of markets exist that conform to this picture, although the characteristics and the degree of organization vary a lot. In all of them, however, the volume of trade may be such that it will seem to the individual participant that price is produced anonymously by the workings of the organized market. But this is only

²⁴For the moment we are focussing on pure brokered markets, although we may allow for the possibility that brokers place limit orders for their own account (cf. Demsetz [1968]; Osborne [1965, 88]); the identification of some changes the presence of trade specialists or dealer-middlemen may carry with, is attempted in footnote 28, below. .

²⁵Dealers or merchant-middlemen are compensated by a profit margin, whereas broker compensation can take the forms of a revenue-sharing scheme (commission) and/or of a fee.

achieved either by means of auction, or set as a result of a bargaining process among a number of middlemen who at every moment concentrate a fraction of the information conveyed to the market by acting as agents or brokers (or otherwise, acting as trade specialists, merchants, or dealers who change their bidding and asking prices to take advantage of arbitrage or speculation opportunities).

Second, we consider 'decentralized' markets that lack any central mechanism of information gathering and production. These are non-brokered markets where the matching of willing transactors is not provided by a specialized trading agent. And besides, where there is no ruling price - asking prices are posted by sellers and not a single buyer in the market has costless information about ongoing transaction prices. Transactions imply a search process for trading partners, for prices, or for other information.

As a familiar example, let us consider the case of a hamburger sandwich vendor, for instance, Old MacBurgher. Like his competitors, he opens his shop sometime in the morning and serves whoever comes at a price he has posted on a bright display over the cash register. Our consumer has an idea of the price paid on his last few visits and even has a fuzzy recollection of an advertisement on television some days before. On his way he also comes across some other hamburger vendors, about the quality and price of which he has some expectation too. Anyway, he enters Old MacBurgher, pays the price and has a sandwich. Here, the asking price is also the transaction price and this is typical in customer markets. Other examples exist where transaction prices may vary from customer to customer, and a large fraction of trade may occur below the posted

price.²⁶

Now let us look specifically to the degree of decentralization of the price signal. The price signal is the most commonly studied control mechanism in price theory, and the only one in the Walrasian tradition standard textbook (micro)economics is imbued with. I shall attempt a distinction regarding the origin of the price signal as a control mechanism in the workings of markets, which is intended to bear correspondence with the distinction above between brokered and 'decentralized' markets.

First, the price signals are formed by individual transactors, and no mechanism is available to currently transmit this information to other prospective transactors in the market. One example might be a market where individual transactors post their price for the good, and admit no negotiation. Another example is when (regardless of there being or not a posted price as a starting point) transaction prices are asserted as a result of communication and bargaining between prospective transactors; i.e., the information available to traders is obtained only by means of communication between whom some prospective transaction is meant to take place (or, alternatively, as a result of costly search): either buyer and seller communicate bidding and asking prices to each other, or each individual trader posts an asking price and a bid price for the good(s) he is willing to sell or purchase, in case of a bilateral market for the good.²⁷ (Common to these pricing schemes is the pervasiveness of set-up costs: go to familiar seller to avoid

²⁶In some markets for homogeneous goods like, for instance, cement and some metal commodities, many transactions appear to fit this model. For some of these commodities two market systems coexist, organized exchanges for spot or future trading, and merchant trades, usually on a long-term supply contractual basis.

²⁷Another example would be just the buyer to communicate orders to the seller in the case of an order-signal as a decentralized control mechanism; this was studied by Kornai [1979], Kornai and Martos [1981; esp.42-3]; on this topic, see Hurwicz [1973, 10-1].

them.)

And second, a price signal is produced by the participant transactors, in such a way that each transaction price becomes currently available to broker agents as well as to buyers and sellers (or at least to a subset of these, including specialist or middlemen traders).²⁸ Transaction decisions to buy or sell are therefore guided by this current 'running' price - so that this price works as a signal for transactors to decide on the bid or asking prices at which they are willing to buy or sell a certain quantity. One example is provided by the 'running' market price in relatively thick organized markets (see Appendix Note D). Even though the market may be atomistic, the control mechanism is not decentralized. In the first case, on the other hand, independently of how thick the market is, the control mechanism is decentralized: price signals are formed by individual transactors without guidance from currently communicated transaction prices (which is not to say, without knowledge of market conditions, or expectations about price(s) deemed relevant for their businesses).

Broadly, the first case is typical of non-brokered markets and the second of brokered markets. But such a stark distinction between brokered and non-brokered markets is only tentative; for further elaboration we need a clearer idea of

²⁸If we abandon our assumption of a pure brokered market and allow for the presence of dealer-middlemen - as not only facilitating, but also making a ready market by means of their own investment in inventories - several adaptations will have to be considered to our previous reasoning, which are anyway independent of the risk-taking function (whether this is or not the most significant function of specialist traders). First, since dealers are compensated by a profit margin on their trades, they have a bigger incentive to develop trading efforts. Second, they are in a better position to take advantage of speculation and arbitrage opportunities than buyers and sellers do (these are required to be intermediated by brokers in their orders to the market). Third, if brokers and dealers have different transaction costs, the signalling function of posted transaction prices is somewhat weakened: there will be a market spread between bid and asking prices but this is a lesser reliable guide to particular transactions involving different types of market operators. That is to say, if consideration is paid to the magnitude of transaction costs, which depend on the type of middlemen as well on the type of traders, there will be a market spread but anyhow it will be only a reference for transaction prices; bargaining power will be relevant.

decentralization.

4.3 - Decentralization of exchange: information and feasibility

Next we analyze decentralization. First, decentralization is defined, and the Walrasian model of general (barter) exchange is characterized as the centralized model of reference. Second, we attempt to follow the common procedure of dropping the functions assigned to the central market organizer in Walras' general market. One is the handling of the logistics of trade. The other is the finding of the equilibrium prices and its communication to traders. If we drop these functions of the auctioneer of providing costless "disequilibrium coordination," and attempt to explain exchange in a decentralized setting, we end up in an impasse. Logical inconsistencies and analytical difficulties leave us with only a few threads aiming at a proposal to coherently understand decentralized exchange.

4.3.1 - The dimensions of the decentralization problem

Decentralization is not an established concept in economics. Hahn's [1970, 2] dissatisfaction seems to apply as of today: "When we talk of decentralizing a plan we think of agents maximizing at given shadow prices and not of the design of decentralized information systems and responses which have only recently begun to be discussed". As to the common view, reference is often made to "decentralization of resource ownership"

(Demsetz [1988, 160]; in line with Debreu [1959, 79] and Arrow and Debreu [1954, 266]). Other senses that are suggested by this one, but are more operative and may be conducive to substantiate Hahn's proposed aim, concern the following three aspects: information, the origin of the price signal, and logistics.

(i) Informational decentralization

Decentralization of information happens when we allow only for a limited exchange of information among economic agents. Specifically, it comprises two elements:²⁹ One regards the "initial dispersion of information", i.e., the nature of the information each trader is assumed to have prior to any market interaction is considered. Information about each trader's characteristics or situation (resource endowments, preferences, technologies) is private, and its communication is (too) costly.³⁰ And, therefore, decentralized information implies that each trader's net excess demands are private information. The second aspect regards "limited communication", and has been called the "privacy-preserving" property,³¹ which implies that information of other agents' characteristics is only conveyed through explicit or "formal" messages (cf. Calsamiglia and Kirman [1993, 1157]). When two traders meet, communication to the

²⁹Cf. Hurwicz [1972, 428], and Hurwicz [1973, 24]; for a more rigorous definition of informational decentralization, see Hurwicz [1960, 398-401]. Though important Hurwicz's contributions are in order to clarify the notion of decentralization, he basically focuses on the informational requirements for optimality in resource allocation, be it in the context of adjustment processes or of mechanism design. See also Ostroy and Starr [1974, esp.1097] and Ostroy and Starr [1990, esp.13 and 33].

³⁰Or even unfeasible, for if "localized" information can be assumed reasonable for the individual trader in his decisions, in case centralization of information is considered this is not sufficient: "...whole maps are to be conveyed" [Hurwicz, 1973, 8].

³¹"...which means that no participant, including an enforcement agency if any, has any direct knowledge of others' preferences, endowments, technologies, etc." (Hurwicz [1972, 448; see also 455,6n] and Hurwicz [1994, 3]).

other of each one's information on net excess demands, and/or proposed exchange rates is the sort of explicit or "formal" messages that are relevant here.³² Limited communication precludes centralization of information, both the 'initial' information on endowments and preferences, as well as the proposed actions of all other traders, viz., their net excess demands. These two elements of decentralized information signify incomplete information,³³ and this is common to brokered and non-brokered markets of empirical resemblance.

The following aspects focus on communication of information in the market by means of messages sent and received (e.g. prices), or as a result of trade interactions.

(ii) The determination of transaction prices, and/or their communication to prospective transactors

Standard microeconomics implicitly separates these two functions, the determination of prices as a result of the adjustment to an equilibrium set of prices, and the information about these, assumed at the command of individual traders. The first function is conducted by the 'market' or the 'price mechanism', and is supposed to

³²Or, as Hurwicz [1969, 514] puts it: "This communication is accomplished in the competitive mechanism through bids (representing quantities supplied or demanded) and prices attached to those bids."

³³Though they don't imply that knowledge is not 'complete' in the 'market.' Stigler, elaborating on Knight's assumptions of perfect competition, explains:

"Consider first complete knowledge. If each seller in a market knows any n buyers, and each seller knows a different (but overlapping) set of buyers, then there will be perfect competition if the set of n buyers is large enough to exclude joint action. Or let there be indefinitely many brokers in any market, and let each broker know many buyers and sellers, and also let each buyer or seller know many brokers - again we have perfect competition. Since entrepreneurs in a stationary economy are essentially brokers between resource owners and consumers, it is sufficient for competition if they meet this condition. That is, resource owners and consumers could dwell in complete ignorance of all save the bids of many entrepreneurs. Hence knowledge possessed by any one trader need not be complete; it is sufficient if the knowledge possessed by the ensemble of the individuals in the market is in a sense comprehensive." [Stigler, 1957, 258-9]

require only the aggregate of individuals' net excess demands. But, as we have seen, excess demands are private information by adherence to the tenets of informational reasonability of pure competition. Thus, the determination of prices relies on information individuals have no way to convey to the market: their excess demands, as required for the computation of equilibrium prices, are planned, notional or target, hence private information. They are not effective, which could only occur in case trade out of equilibrium was not assumed away.

The second function is not explained, it is just postulated that individual traders know the equilibrium set of prices. This is meant to be a virtue of decentralization of the market mechanism³⁴ that individual participants in the economy need only information about prices, beyond their own knowledge of resources, preferences and technology, privately held. This is hardly so, and only as an 'as if' market mechanism. In fact, the adjustment to the equilibrium price set is based on aggregate information, which cannot be known to any market participant (unless it is a central one); and the process of dissemination of this information (prices signals) is not even contemplated. Thus, we must rework the definition of decentralization at this point.

The control mechanism is completely decentralized³⁵ when each and every individual agent is not endowed with information about prices (or about proposed prices and/or proposed quantities to trade) either than that each agent has obtained in pairwise meetings with prospective traders, or that he has sought for. Decentralized price

³⁴"...the information needed by firms and consumers consists solely of their technologies or utility functions plus prices, while the adjustment of prices is based only on the aggregate of individuals' decisions. It is the minimization of information requirements for each participant in the economy which constitutes the virtue of decentralization" (Arrow and Hurwicz [1960, 42]; see also Demsetz [1988, 160]).

³⁵On decentralized control mechanisms, see Kornai and Martos [1981, esp.36-39] and Martos [1990].

determination should, as a starting point, be thought of as coming about by pairwise bargaining (cf. Rubinstein and Wolinski [1990, 63]).

A less strong, and the commonly used, understanding of decentralization is that implied in pure competition: individual traders making their decisions "...based on a fairly small body of universally communicated information (e.g. prices)".³⁶ This misconceived notion of universal knowledge of prices will be the most referred to in the analysis below. However, we should be aware that it is only good for constructions that freeze the function of finding market-clearing prices to focus on the execution of trades; its purpose is exclusively of analyzing the logistics of decentralized barter exchange, given equilibrium prices. In any case, this is not a suitable definition; the information about the market-clearing price set cannot be assumed to be costlessly known to traders (as Stigler [1961] first pointed out), for a consistent comprehension of decentralized exchange.

(iii) Logistical decentralization

For the logistics of trade to be decentralized, the trading arrangement is required to be based on decentralization in the first sense above, specifically that information

³⁶This is the definition in Ostroy and Starr [1990, 33]. It is also unreservedly followed by Veendorp [1970a, 2]; he sees, however, the need to justify this assumption, which he does mainly by reference to Hayek [1945], even though his other assumption of organized exchanges doesn't play a lesser role. The notion of known prices, commonly espoused, is erroneously based on Hayek's demonstration of the informational efficiency of the price mechanism. Hayek never presupposes anything like universal communication or free information, rather he only asserts that the price system works like a mechanism for the communication of information, so that "...only the most essential information is passed on, and passed on only to those concerned." Moreover, relevant information is transmitted through market interaction of individuals possessing only partial knowledge: "The whole acts as one market, not because any of the members survey the whole field, but because their limited individual fields of vision sufficiently overlap so that through many intermediaries the relevant information is communicated to all." [Hayek, 1945, 526, 527 and 530]

about each trader's net excess demands be private information.³⁷ The precise assumption on knowledge of market prices is left open. One possibility is that agents are endowed with information on the set of current market prices, supposedly equilibrium market prices; another would be that information of each agent about ongoing prices is limited to the degree of search he does accomplish.

In any case, logistical decentralization involves bilateral trade and search for transactors. Absence of a central authority in charge of trading coordination is a necessary first step, but in order to focus on the logistical problems of exchange we have to let individuals on their own conducting transactions pairwise. Exchange occurs in the course of transmission of information between traders on proposed price and/or quantities to transact, and is reasonably thought of as involving bargaining; or alternatively, under certain suitably specified institutional settings, the posting of an asking price by the seller, or of a offer price by the buyer (prices set on a take-it-or-leave-it basis).

Summing up, with a view to a broad classification of trading schemes as to the

³⁷Ostroy and Starr's definition of a decentralized trading rule seems to suffer from a logical gap (cf. Ostroy and Starr [1974, 1097]: rule D.3 - which however was dropped in the 1990 paper). Literally interpreted it applies to each pair of traders in isolation and to an instant in the sequence: knowledge of contemporaneous excess demands of the other trader and of excess demands communicated between this pair of traders in previous meetings [1990, 33]. On the other hand, centralization implies contemporaneous knowledge of every other trader's excess demand [1990, 33], or of their histories of excess demands as well [1974, 1074]. The logical gap is due to the fact that traders meet sequentially: under rule D.3 they would be able to gather series of historical excess demand data in the course of meetings. If, at any meeting, information obtained at previous meetings with other traders is not called to memory this is a peculiarly defective "memory"; if it is called to memory, then each trader is endowed with historical information on traders either the one he is actually meeting, though not contemporaneous; and if this is so, "...each trader would be able to make more precise estimates of the probable excess demands of future partners" [Ostroy and Starr, 1974, 1097, 7n]. Although everyone trades with everyone else, and this makes it difficult to set a range for decentralized information, this question had better not be disposed of, as in fact it was in the 1990 article. (For a brief comment on 'restrictions on memory,' see Hurwicz [1972, 455, 6n].)

degree of decentralization, we may present a set of assumptions regarding the three aspects of decentralization we considered: 'initial' information, predetermination of the price signal, and logistics.

The assumptions about communication of private information are common to all the trading schemes that are set out below, namely:

(a) - Information on endowments and preferences of individuals is private; also, net excess demands are private information.

- Communication of information on net excess demands or proposed exchange rates is limited to the parties trading (limited to bilateral meetings between prospective traders).

Regarding the two other aspects, the price signal and execution of trades, we make the following distinctions. As to the determination of transaction prices and its dissemination in the market two possibilities are considered:

(b₁) - Equilibrium prices are predetermined, as the solution to an aggregate consistency of trading plans by means of an implicit auction.

- Information on the equilibrium set of prices is costlessly available to all traders.

(b₂) - This second case doesn't allow for a centralized computation/determination of equilibrium prices. Rates of exchange (prices) are contracted by way of bargaining, or are adjusted by trading post specialists.

- Communication of transaction prices (as well as asking and/or offer prices if bilateral bargaining is presumed to occur) is limited to the participants in the transaction.

As to the logistics of trade, let us distinguish centralized and decentralized

execution:

(c₁) - Execution is carried out with a central market place, so that trading can properly be seen as multilateral exchange mediated by the services of a central agent.

(c₂) - The execution of trades is left to pairwise meetings between traders.

A typical model involves a mixture of the assumptions in all three aspects. Combining these assumptions, we arrive at the following trading schemes:

(I) Assumptions (a), (b₁), and (c₁) correspond to the centralized neowalrasian model.

(II) Assumptions (a), (b₁), and (c₂) correspond to a situation of logistical decentralization, where however we allow for knowledge by each trader of the set of relevant equilibrium prices contemporaneously prevailing elsewhere in the economy. Ostroy and Starr, and the search models fit this pigeonhole.

(III) Assumptions (a), (b₂), and (c₂) make up a more radically decentralized scheme: decentralized bargaining and execution. Individuals only gather information and determine transaction prices by way of bilateral meetings with prospective transactors. Besides, logistical aspects is all there is to this case, obtaining information and contacting trading partners is part of the same logistical process. Or, the other way around, potential trades are assessed in the process of obtaining information, either through search, pre-assigned cycles of meetings, or through consultation of trading-post agents.

This framework of trading schemes is a good basis to organize this section. As a reference, it is pardonable to introduce the neowalrasian model since every theoretical

attempt at decentralizing exchange could hardly escape the fetters of general equilibrium analysis. Then the consistency of informational requirements of convergence and execution will be questioned. Next, I shall try to make sense of the progress made by a few authors to decentralize the logistics of trade, maintaining equilibrium prices as given. Finally, a few steps will be discussed that may be required towards the construction of a theory of decentralized exchange in all three aspects.

4.3.2 - The neowalrasian model of centralized exchange

As we have seen, Walras depicted exchange in markets where free competition takes place by means of bargaining whereby price bidding among traders leads to equilibrium prices, and, given those prices, exchange takes place. A few drawbacks weaken his construction. Even if we take for granted the dichotomy between the determination of the equilibrium set of prices and its execution, we will have to raise doubts regarding, first, the determination of those equilibrium prices, second, their assessment by or communication to traders, and third, the logistics of trade. All three regard the degree of decentralization of the market mechanism Walras envisioned but was unable to logically complete. The irony is that, though outwardly the neowalrasian theory is a reconstitution of the Walrasian system, it is thought to represent a complete rendition of general exchange - yet for a world of imagination, as we have seen, without exchange - while Walras was not for a market "perfectly organized in regard to competition."

Before a critical appraisal of those drawbacks, referring to disequilibrium

coordination, I shall attempt to succinctly characterize the neowalrasian model of general exchange as basically centralized, and present a few notes on equilibrium coordination.

The neowalrasian model of general exchange relies on a centralized market mechanism. The following functions are assigned to the fictional auctioneer:

- (i) Finding market-clearing prices, and their communication to traders.
- (ii) Providing the organization of trade, i.e., the execution of trade, by means of a clearing house; or, as Arrow and Hahn [1971, 329] put it, "...that it is part of the auctioneer's job to freely disseminate offers to buy and sell."

Both these functions³⁸ regard "disequilibrium coordination," according to Howitt [1990, 4]: "Perfect disequilibrium coordination - the fact that all trades occur at equilibrium prices - reflects two basic sets of assumptions. One is the set of technical assumptions guaranteeing existence. The other is the set guaranteeing that everyone knows the equilibrium prices."

The first function performed by the auctioneer is that of coordinating the beliefs of traders (through prices). *Tâtonnement* is supposed to converge to a given equilibrium set of prices, and since the process of gathering and disseminating this information is costless, traders are, therefore, informed of equilibrium prices.

³⁸A third function is usually thought required: enforcing the budget constraint (by means of some sort of a "record-keeping device" [Ostroy and Starr, 1990, 11]) to guarantee that trading plans are carried out at the competitive prices. This is imputed to avoidance of the moral hazard problem created by the presence of private information: by anticipating the effect of his offers to buy or sell on the formation of prices, a trader would have an incentive to misrepresent his offers in order to alter prices to his benefit.

On this question of "individual" incentive compatibility in competitive behavior "...in a "nonatomistic" world of pure exchange", under the requirements of informational decentralization, see Hurwicz [1972, 443-54, esp.446] and [1973, 27-32]; the author uses the "...term "atomistic" in the old fashioned sense, meaning that every participant is infinitesimal as compared with the total market. (In modern measure-theoretic language this case is called "nonatomic")" [Hurwicz, 1972, 456, 9n]. Thus, in Hurwicz "nonatomistic" means "finite." Some posterior literature has disintegrated this finite economy and showed that, in the limit, as the economy becomes 'large' the incentive compatibility hindrance vanishes. However, as is observed below, this is an excrescence of centralized exchange.

The second function has the auctioneer guaranteeing that buyers' and sellers' proposed transactions match by means of direct 'multilateral' barter exchange with a central clearing-house. The auctioneer is in charge of keeping records of disposals and acquisitions so that trading plans are carried out, the single budget constraint enforced, and no trader's proposed trade is left unmatched. Buyers and sellers transact directly with a central clearing-house, 'simultaneously' and at no cost, and therefore the logistics of trade bring no impediment to a full consistency of trading plans, as assessed in the course of the determination of the equilibrium set of prices. In fact, traders have communicated to the central market-maker their net excess demands, which are dispositions to trade on the basis of the pre-announced prices. If, given this set of prices, buyers' demands and sellers' offers are equalized on the aggregate for each and every good, then the auctioneer stops; he concluded his first function. This will be a signal for traders that their last decision on dispositions to demand and to offer will be their effective trades. And this is the case. Plans to trade coincide with effective trades, as warranted by the frictionless execution of exchange. The auctioneer's second function allows dispositions to eventuate. (See Arrow and Hahn [1971, 264] on tâtonnement as sidestepping the difficulty that "...some agents will find their plans cannot be brought to fruition"; but this is not the whole story, only under the implicitly posited execution will traders be spared disappointment.)

There is also the question of equilibrium coordination. Perfect equilibrium coordination, "...the fact that plans made at equilibrium prices constitute a Pareto-optimal allocation" [Howitt, 1990, 4], is a property of the Walrasian general equilibrium. Equilibrium coordination means that decisions of individual traders are based "on mutually consistent beliefs" [2], this involving agreement upon a common set of priors

(as to the model of the economy), and the requirement that all interactions between economic agents be exclusively mediated by prices, of which each trader is informed and which he takes as given. However, even if disequilibrium coordination obtains, information by every individual trader of the equilibrium price set is not sufficient to guarantee an optimal allocation, i.e. equilibrium coordination. Because it introduces questions to be handled later, we consider this aspect more closely in Appendix Note E, where a critique of search barter models is attempted.

4.3.3 - Execution given convergence: two exercises at odds

In the Walrasian setting, we have to distinguish existence, convergence, and execution.

Proofs of existence of equilibrium of a competitive economy³⁹ were obtained on the basis of a fixed-point theorem⁴⁰ for an economy that satisfies appropriate axioms, like convexity and monotonicity of preferences. Existence has been asserted either based on the preference relations of individual consumers (e.g. Arrow and Debreu [1954]), or just on the excess demand correspondence (e.g. McKenzie [1954]). Constructive proofs of the existence of an equilibrium price set were developed by Scarf (see Scarf [1982]

³⁹Even though at variance with the prognosticated descriptive realism in Arrow and Debreu [1954, 256], existence proofs do not deal with exchange. Referring to multiple equilibria, Debreu admits that: "[t]he pathology [of infinite equilibria] is due to the manner in which the agents are matched, a situation entirely different from that of existence theory where it was possible to give general conditions on the behavior of each agent separately" [Debreu, 1976, 233].

⁴⁰See Uzawa [1962a], Debreu [1982], and Scarf [1982]. For references on variants and alternatives, see Debreu [1982, 697-8]. See also Mas-Colell [1985] for a differentiable approach, in the line of Smale [1976a].

on combinatorial algorithms for the computation of "approximate" fixed points), and Smale [1976a] who proposed a "differential process". Here the question of existence of an equilibrium price set is given the underpinning of computability; and if the proof of existence is mathematically equivalent to the proof that a fixed point exists that is computable, it also allows its "approximate" computation.⁴¹

These constructive proofs of existence are not, however, the same as proofs of stability of the price adjustment process.⁴² It is Scarf's opinion that "...the price adjustment mechanism can be used neither to provide a proof of existence of competitive equilibrium nor an effective computational procedure for the general case" [1982, 1012]. But in the case of Smale [1976a]⁴³ the distinction between existence and convergence becomes hazy since the algorithm for the computation of equilibrium prices uses an adjustment process, where the price change of a commodity depends on the properties of the excess demand for all other commodities (Hahn [1982, 767]); and even more so in Saari and Simon [1978], and Saari [1985], where the rate of adjustment of a price is proportional to the (market) excess demand of that commodity only.

⁴¹Cf. Hildenbrand [1974, 162ff] on the meaning of "approximate" equilibrium price. Also, Scarf [1973, 93], when discussing "the sense of approximation" of an algorithm for the computation of a fixed point in the general Walrasian model, concludes: "...if the grid is sufficiently fine, the discrepancy between supply and the market demand at prices π will be small for all commodities. Unintended inventories, arising from a price vector that does not clear all markets precisely, will be insufficient to provide a signal for the revision of prices." We have to ask: Signal to whom, the auctioneer? For decentralized pricing, how could this be maintained? (See comments on Arrow [1959] in Chapter V.) But this question, such as Scarf's reference to signal, is wide of the mark; the computation of a fixed point cannot be interpreted as any economic mechanism.

⁴²The purposefulness of existence exercises is problematical (Clower [1994d, 20-1]; cf. Punzo [1991, 36]). Constructive proofs of existence or the analysis of stability of convergence processes are eventually all there may be to it, since the question of local uniqueness is closely tied to convergence analysis for purposes of comparative statics (cf. Dierker [1982, 796-7]; see also Hahn [1989b]). In any case, since even the "market imitative" processes [Arrow and Hahn, 1971, 307] are notional and involve no activities or transactions, on strict logical grounds stability analyses add little to proofs of existence.

⁴³Smale uses Newton's method of solving non-linear equations (Arrow and Hahn [1971, 303]). Smale [1976a] fostered work by Saari and Simon [1978] and Mas-Colell [1985].

Stability⁴⁴ deals "...with endogenous processes operating in an economy which may bring about an equilibrium. Indeed, the latter is often implicitly or explicitly defined as a stationary point of such a process" [Hahn, 1982, 745]. Of these processes the most commonly considered is "the law of demand and supply", and the price mechanism in general exchange that of tâtonnement of Walrasian extraction, which will be our main concern in the following. However, other mechanisms have been proposed (cf. Hahn [1982, 745-6 and 772-85]; Fisher [1983, Ch.2]) that allow for exchange at out of equilibrium market prices. One possibility is to keep the auctioneer but assume that markets are orderly⁴⁵ at each date, as in Hahn and Negishi [1962]. Another possibility was considered by Uzawa [1962b] and Smale [1976b], that dispenses with the auctioneer: common prices are not given, and exchange occurs if and only if it is "budget feasible" and a transaction between each pair of individuals takes place whenever it is utility improving (cf. Hahn [1982, 772 and 778] and Uzawa [1962b, 219]).

But let us concentrate now on the stability of tâtonnement equilibrium. The Walrasian tradition poses tâtonnement as an iterative calculation of the set of equilibrium

⁴⁴Thorough surveys on stability of the competitive equilibrium are Negishi [1962], Hahn [1982] and Weintraub [1991].

⁴⁵"Markets are orderly if no agent is restrained in his planned demand (supply) of a good when that good is in aggregate excess supply (demand)" [Hahn, 1982, 746]. An interesting comment is added: "Exchange is now with an anonymous market. At all times (including $t=0$) markets are *orderly*: no agent has excess demand (supply) for a good which is in aggregate excess supply (demand). The idea is that there is very good information in all markets so that (instantaneously) agents know of all supplies and demands. It is not a very convincing assumption but it has lately become popular in rationing models (e.g. Drèze (1975))" [Hahn, 1982, 781]. (Cf. Martos [1990, 19] for a definition, and Kawasaki, McMillan, and Zimmermann [1982] for some empirical results.)

Moreover, as will become clear in the following, this mention to trading out of equilibrium is mistaken: for feasibility, the orderly rule implies central allocation of trading opportunities. This is purely an exercise on convergence, and one that fails the requirement of information decentralization, for that matter.

prices. This function is generally assumed realized in the model of general exchange by an external entity, the auctioneer - though the question of whether it is tractable, and under which informational assumptions, is seldom and only marginally appended.

First, we have to question convergence. Commonly, analyses of general equilibrium assume that a set of equilibrium prices can be computed and announced to traders, and therefore is taken as a given. And the conclusion is that it can't be shown - in general, it is not true. Then we intend to question the beliefs of traders, i.e., their reliance on this information in the workings of the general barter model. Next, the analysis proceeds by analyzing the feasibility of trades, execution, or logistics. For this purpose, the informational assumptions are chosen to be as close as possible to those underlying pure competition, the informational efficiency of which is thought to be a central property. Decentralization of information is, thus, a starting point in the study of the feasibility of trades, only to arrive to the conclusion that execution of planned trades is generally not feasible.

No denying that analysis should be decomposed in manageable steps. The question I am raising here is whether those analytical steps are informationally congruent with each other. Dichotomization between convergence to the equilibrium price set and execution of trading leads to analytical inconsistencies in decentralized exchange: given the different informational setup, there is no clear logical point in relating or comparing them. Only in centralized exchange does the problem of convergence to an equilibrium set of prices mirror that of convergence to a set of coordinated trades, and therefore the whole exercise can be curtailed to getting prices right.

Now, the argument is developed in detail. The objective is to analyze the consistency of the three exercises, existence, convergence and execution.

(i) Convergence

The traditional and most commonly considered price mechanism is a tâtonnement process whereby individuals take centrally determined prices as a given to assert their planned trades, and only consider trade if planned trades are consistent in the aggregate, i.e., if net excess demands for every commodity are zero. The auctioneer is supposed to cry out a set of prices, to collect information on aggregate excess demands for the communicated set of prices, and change prices if excess demands are not zero. In the limit of this process, prices are supposed to converge to equilibrium. (The problem of convergence in the Walrasian world is limited to getting prices right.⁴⁶)

Stability analysis was initially dealt with on continuous time, and proofs were obtained only under special restrictions, like the cases of gross substitutability or of a 'representative' consumer (cf. Arrow and Hahn [1971, esp.322-3] and Hahn [1982, 754-70]). But, configurations of excess demand functions have been constructed (e.g. Scarf [1960] and Gale [1963]) for which this tâtonnement process is unstable; by simplifying the construction of such (counter)examples, these results were strengthened by some theorems of Sonnenschein-Debreu-Mantel⁴⁷ "...which, roughly summarized, show that any arbitrary set of excess demand functions continuous on the interior of the simplex and satisfying Walras' Law, can be generated by utility maximizing behavior of agents for some utility functions and endowments" [Hahn, 1982, 745]. The results of Sonnenschein-Debreu-Mantel have a negative implication on proofs of stability founded

⁴⁶In the Walrasian tradition, tâtonnement is usually meant not only to get prices right but also the right prices: the same prices for the "theoretical" and the "practical" solutions (i.e., to achieve a determinate solution).

⁴⁷Cf. Sonnenschein [1972; 1973], Debreu [1974] and Mantel [1974].

on 'decomposed' excess demand functions. This literature⁴⁸ concludes, for the case of finite economies, that models of general exchange - built on individuals' excess demand functions as derived from standard behavioral assumptions - do not have enough structure; i.e., aggregated excess demands cannot be generated that present sufficient restrictions (beyond continuity, homogeneity, and Walras' identity) for a well behaved convergence.

Two other related questions arise here. Proofs of convergence to the equilibrium set of prices have been sought on the basis of informational decentralization (endowments and preferences are private information);⁴⁹ thus the first question concerns the information required to assert stability. Another question is of convergence 'time.'

As to the first question, the most complete answer is provided by Saari [1985]. He develops the case of a tâtonnement process for discrete time,⁵⁰ which was initially dealt with in Uzawa [1958], and presented in Arrow and Hahn [1971, 307-9] for the

⁴⁸For a review of the negative results of Sonnenschein-Debreu-Mantel on proofs of uniqueness and stability - proofs of asymptotical local stability of general equilibrium of an exchange economy (cf. Hahn [1982, 745 and 763]) - founded on "individualistic assumptions", see Kirman [1989, esp. 128-33] and Hildenbrand [1983, 25-7].

And for a survey on "[t]he problem of decomposing arbitrary excess demand function" [Mas-Colell, 1985, 242], see Shafer and Sonnenschein [1982, 679-88].

⁴⁹The Walrasian tâtonnement has widely been presumed paradigmatic as an informationally decentralized mechanism, i.e., "...involving lower processing (transaction) costs" (Hurwicz [1994, 4,11n; also [1969, esp. 515ff]). See also Hurwicz [1973, 12] on the gradient process as informationally decentralized. For the definition of an informationally decentralized adjustment process in resource allocation, see Hurwicz [1960], and for a general but short summary, Hurwicz [1994, 2-5].

⁵⁰For continuous time, Saari and Simon [1978] have most unsuccessfully questioned the possible reduction of the informational requirements of Smale's [1976a] "globalized Newton method" that the price adjuster needs for a convergent mechanism. ("The globalized Newton method can be viewed as characterizing a story where instead of prices changing in response to supply and demand, they change in a fashion which always preserves the ratio of the aggregate demand for commodities. Thus this dynamic preserves the ratio $z/|z|$ [$z(p)$ denotes the aggregate excess demand function at the price p], and it is only the scale which changes. To the best of my knowledge, no one has examined whether this dynamic admits an economic justification." [Saari, 1985, 1118-9])

special case of gross substitutes. He attempts a more general conclusion, which however is basically the same - that knowledge of excess-demand functions will not be sufficient for stability. A (traditionally) held position is that the auctioneer is not required to be endowed with knowledge of every individual's excess demands; to find equilibrium prices, only aggregate net excess demands for each commodity would be needed. The function of determining and announcing equilibrium prices would be centralized, even though information were decentralized. This is not right, though. (See discussion referring to Meyer et al. [1992], in Appendix Note E.)

Saari attempts to identify what is required in order to find a "universal" adjustment process, one that converges for any economy which satisfies convexity ("standard concave utility functions") and regularity conditions (aggregate excess demand function is single valued and smooth), as well as that puts *no* restrictions on the forms of the excess demand function. This is "...an unresolved aspect of the theory because the standard story of prices adjusting according to supply and demand need not correspond to a convergent process" [Saari, 1985, 1117 and 1119].⁵¹ Saari considers "...any iterative procedures which can be expressed in a standard form, which depends smoothly on the aggregate excess demand function, and which stops when it reaches an equilibrium"; and the basic result is that the "...informational requirements can be very large ... and they are not of the type suggested by the usual tatonnement process. This is true even in the two commodity case!" [1118].

⁵¹Examples have been devised for exchange economies with more than two commodities where there is no convergence (Scarf [1960]; Gale [1963]; Veendorp [1970b]); and, as seen above, this result was broadened after a theorem of Sonnenschein [1972]. In general, if equality of supply and demand is to be asserted as the limit of a price adjustment process, then this can only be shown for special sets of assumptions: for instance, that all goods are gross substitutes in continuous time, or the case of a 'representative' consumer.

The dynamical process associated with tâtonnement is more appropriately thought of as a discrete time iterative process, since a differential dynamic would require a continuous updating of information at each instant of time, which can be seen as going beyond the computational ability of the "auctioneer." But, given that the continuous case may be viewed as approaching, in the limit, the iterative mechanism, "...it is only natural to expect the informational requirements of the iterative dynamics to mimic those given by the differential equations" [Saari, 1985, 1119].

Locally converging mechanisms require information of the excess demand function ($z(p)$) and of all the marginal rates of each component of the aggregate demand with respect to each price ($Dz(p)$, the Jacobian of $z(p)$).

For globally convergent mechanisms, it is shown that there does not exist an iterative mechanism "...which depends upon the information obtained solely from z , Dz , ..., $D^N z$, where N is any positive integer" [1120]. Knowing that local information is not sufficient,⁵² which global information would be required could not be specified, in order to find a universal process.^{53 54}

⁵²There are problems with the mechanism. The main one lies in lack of information about price points where to start the iteration and that there is an uncountable number of these points which dynamic is not convergent (cf. Saari [1985, 1122-4]). In order to obtain convergence, the choice of the iteration function (step size) may have to be restricted (see Uzawa [1958] for an equivalent conclusion) but this would be incompatible with a universal mechanism since it requires global information about the underlying differential function. But "[t]his type of information is a long way from the usual story where the information is sought strictly from the reaction of the people in the market" [1124]. Furthermore, as to "...supplemental global information to assist the process" Saari hints at the possible need to include prices directly as in the Scarf algorithm (i.e., not only indirectly through the excess demand function).

"[T]he basic reason [of the impossibility result] behind Saari's theorem ... is [that] the function space is so rich that for any given procedure we can construct smooth maps which 'trap' the procedure into a small region of the domain containing no equilibria of the function" [Bala and Kiefer, 1994, 302].

⁵³Saari's impossibility result has led Bala and Kiefer [1994] to look for a generalization of the class of mechanisms considered by Saari.

As to the second question, for those settings where convergence is shown to exist, the speed of convergence may be very slow, be it in "model" or "computer" time [Hahn, 1987, 137]. Referring to stability in the short-period equilibrium as asserted by means of tâtonnement processes, Arrow and Hahn frame the question properly:

Is it possible to say that the auctioneer's rule is stable, when that notion seems to imply time going to infinity and we are confining ourselves to a finite time interval? The answer is that we have used time as an expository device so far; what is really at stake is that the number of steps - price changes undertaken by the auctioneer - goes to infinity, and that is clearly possible in a finite time interval. While in a formal way we can avoid being silly, it is true that in practice price adjustments do take time and that if the tâtonnement is to be taken seriously as in some sense connected with reality, then it must face the objection that even if the process is stable it is only asymptotically that equilibrium is attained. [Arrow and Hahn, 1971, 310]

This same problem is implied in rules of price adjustment either in continuous time, as a limit of a function,⁵⁵ or in iterative mechanisms. Saari [1985, 1124] refers that convergent points exist that can take innumerable iterations to even settle into the appropriate convergence interval.

Therefore, the computation of the equilibrium price set by way of an iterative

⁵⁴Referring to adjustment processes in discrete time, Hahn recognizes that "[t]o obtain results now we must do more than restrict the form of the excess demand functions; restrictions must also be placed on the adjustment speeds", which "...is fundamentally a negative conclusion since we have no theory to help in this matter. Indeed, if the theory is to be taken as in some way descriptive we could not exclude mixed difference-differential equations for price adjustment and theory would yield few qualitative results" [Hahn, 1982, 768-9]. For the same conclusion, even in the case of gross substitutes, see Arrow and Hahn [1971, 308].

For a further comment on adjustment methods (like Newton's method, as used in Arrow and Hahn [1971, 303] and Smale [1976a]) that violate "...the supposed economy in information of decentralized economies", see Hahn [1987, 136].

⁵⁵Cf. Samuelson [1947, 261] referring both to "[e]xamples of functional equation systems", and to "*perfect stability ... in the limit as time becomes infinite.*"

As to quasi-global stability as defined by a Lyapounov function, Arrow and Hahn [1971, 274] state that "...so far, while we can predict that after a sufficiently long lapse of time prices will be arbitrarily close to some equilibrium." And also, raising doubts on the logical validity of ruling out trading at out of equilibrium prices, the authors grant that "...if [the auctioneer's rule is stable], trading will be permitted only "in the limit" (i.e., as t approaches infinity), for it is only in the limit that equilibrium and "called" prices coincide." [324]

process requires information surpassing the limits of private information. And, even if such information is assumed, iteration is not guaranteed to converge in a finite number of runs.

(ii) Beliefs

The communication of prices presents two problems, one the means by which it takes place in general exchange, and the other, whether, being known to traders, these beliefs play any role. As to the first, this is appropriately dealt with neither in Walras nor in other accounts of general exchange. As Walker notices, Walras' general model lacks the definition of the means how information is produced, and by whom, and how it is disseminated in the market among prospective transactors. Information requirements, and the logistics of information gathering and communication that underlie trading, are implicitly assumed away as relevant features of the intermarket adjustment problem. And if this failure impinges in the first place on decision taking on planned quantities to trade during the equilibrating process, the informational problem is also present in equilibrium transactions after the general equilibrium set of prices is reached:

Even if the rule existed [the rule that trade cannot occur until excess demand quantities in all markets are zero], it would not be sufficient. There would also have to be a means of collecting and disseminating information so that all traders are informed when all excess demands are zero, features that also do not exist in [Walras'] models. In short, the barter models lack the institutions, technology, rules, and procedures that would be necessary to generate the necessary characteristics of information, adjustment, and coordination. [Walker, 1993, 1444]

The import of all this lies in the construction of beliefs that prices are equilibrium prices. In the Walrasian system, this coordination of traders' beliefs is presumed ensured

by completion of tâtonnement (cf. Howitt [1990, 4]), despite the inexistence of any mechanism to communicate to traders that their plans are coordinated ex ante. However, since information gathering and dissemination is costless, there is no room for the consideration of such a mechanism. The possibility that the constructed beliefs could be invalidated in the course of transacting doesn't also exist since in strict logic no (direct) bargaining over exchange rates takes place. Price determination and trading are both centralized, and for this invented world no contradictions exist. Beliefs are inconsequential. All the problems arise when specks of decentralization are introduced in the mechanism.

(iii) The consistency of bilateral barter with predetermined prices

A thorough account of a pure barter model is Veendorp's [1970a] critique of general equilibrium analysis on the grounds "...that the existence of a set of positive prices at which demand equals supply on all commodity markets does not assure the existence of a set of positive exchange rates at which demand equals supply on all commodity exchanges" [Veendorp, 1970a, 3],⁵⁶ and further he contends that "...the analysis of the existence of equilibrium exchange rates in barter economies is closely

⁵⁶General barter exchange is set in the framework of purely competitive assumptions, i.e., "...all traders should be well informed about the exchange rates that prevail on all commodity exchanges and should consider these exchange rates as given. However, no additional information on the part of individual traders concerning the preferences and endowments of the other traders should be required" [Veendorp, 1970a, 2].

In the context of these informational assumptions of a "purely competitive system", general equilibrium analysis handles two separate problems, one "...of deriving conditions for the existence of a set of equilibrium prices" and the other "...of deriving conditions for the convergence of a competitive price adjustment process, the adjustment being made by an auctioneer whose actions are meant to reflect market forces." [ibid.]

related to that of the actual trading process". The procedure by which individual traders are meant to carry out their trades is, in the case under analysis, by bartering as taking place successively in trading posts, one for each pair of commodities.⁵⁷

In order to analyze execution of trading by direct barter as carried out by individual traders, we should pay attention to two assumptions. One is that equilibrium prices have been determined, i.e., planned net excess demands for every commodity are zero. The other is the absence of a central exchange agency, i.e., a clearing center where participants would maintain an account, where excess suppliers were credited their deposits of excess supplies, and afterwards, from where excess demands were collected. However, it is assumed the existence of organized commodity exchanges for the exchange of any two commodities, trading posts. At each trading post, the restriction prevails that total demand for one of the commodities in exchange for the other must balance total supply of the first in exchange for the second (p.3), so that equilibrium exchange rates are not disconfirmed at any exchange. Hence, a 'specialized broker'⁵⁸ is assumed to attend ongoing pairwise transactions, and enforce the condition that total demand and total supply of each commodity in exchange for the other are in balance at any trading post. In addition, during the execution of exchange the "necessary condition"

⁵⁷Trade within each trading post is not tackled by Veendorp; if it were, he would have to consider successive barter for each pair of transactors and goods, both.

⁵⁸I use the odd designation of "specialized broker" to distinguish from specialist: in a partial equilibrium set up (dealing with a single commodity against 'money') they are equivalent, as they would be if referring to brokered markets of empirical extraction. This is not so in the trading post barter general model. (Walras, by the time of the first edition of the *Éléments*, refers elsewhere to calculators to whom "order-books" are given, in his explanation of the mechanism of exchange; see Walker [1990b, 966].)

With exchange at given, and known, equilibrium prices this broker is dispensable. The accounting function he is supposed to perform is conveniently solved by the quid pro quo condition of each pairwise trade.

Anyhow, if trading at out of equilibrium prices is allowed, this trading post operator is called upon to perform the extra function of rationing (e.g. Benassy [1975] and Drèze [1975]); but this specialist can't know who to ration.

for market equilibrium in a barter economy is extraneously maintained "...that the total excess demand for any commodity (summed over all individuals and all commodity exchanges) equals zero" [5]. As may be clear, two equilibrium conditions are imposed at each step of the barter process: one, the market clearing rule, that net excess demand for any commodity be zero, and, second, a trading rule⁵⁹ that at any trading post total demand and total supply of each commodity in exchange for the other match.

Then the author presents an example where the final result of barter, independently of the sequence in which trade takes place, shows that the existence of a set of equilibrium prices at which notional excess demands are consistent does not assure the existence of a set of exchange rates in direct barter trading on all commodity exchanges (cf. Veendorp [1970a, 3]).

Two main comments are due, the second built upon the first.

(i) In the spirit of Walras and central to Veendorp's argument, we should stress the condition that restricts each commodity's net excess demand - given the predetermined equilibrium price set - to be zero during the execution of barter trades.⁶⁰ We should notice however that the assessment of this condition of zero net excess demands is beyond the information endowments of individual traders or the information

⁵⁹The trading rule is equivalent to the quid pro quo condition in an aggregative form over all trades taking place at a trading post, under the assumption of known equilibrium prices. Either equilibrium prices are assumed to be known and we can presume traders to enforce quid pro quo at such prices, or they aren't and a "market" restriction, as defined by Veendorp, becomes binding; this is why if prices are assumed to be known and adhered to in every pairwise trade, the market equilibrium condition becomes redundant. Veendorp seems never to believe his assumption that prices are known to be equilibrium prices; it is a very sensible suspicion, but one that helped raise doubts on his argument.

⁶⁰This is assumed by Walras and Isnard (cf. Jaffé [1969, esp.30 and 34-5]); Pareto [1909/1927, 432] refers expressly to it. As seen above, it may be redundant: if transaction prices are equilibrium prices, quid pro quo implies this restriction.

capabilities of the 'specialized brokers' and so it is not enforceable by (each of) them. Complying with assumptions of pure competition, individual traders are assumed to have knowledge only about market prices and their own endowments and preferences (p.2). And also, 'specialized brokers' at each trading post are only informed of proposed demands and supplies of the pair of commodities which exchange they attend, and consequently cannot gather information on market net excess demands of these two commodities.

Barter is occurring on a direct, pairwise, quid pro quo, 'sequential' way, which is decentralized. However, during the execution of barter trades, the working of the market is restricted by some entity who is assumed to gather and aggregate information over all individual traders, and enforce continuously the condition of net excess demands of zero.⁶¹ So, the working of market trading is supposed to call forth centralized information, which individual traders, and "specialized brokers" as well, have no way to know. Barter is assumed direct but the information required for the working of the market is not decentralized. This seems inconsistent; in effect, Veendorp has missed the problem to which he was responding in his paper.

If we envision the execution problem as direct barter and rely only on decentralized information, we have to be content to impose only such restrictions, or 'rules,' as are based on market information available to individual traders (prices), or are meant to be 'enforced' by them ('sequential' quid pro quo, which in any case is a 'rule' that can be assumed 'enforced' by the trading partners, independently of knowledge of

⁶¹As seen above, if beliefs that prices are equilibrium prices were maintained, quid pro quo at these prices would be sufficient, and the market condition redundant; also, the trading rule would just be identical to quid pro quo in the aggregate for trade at each trading post.

market prices). The maintenance of the market clearing assumption - reasonably logical for centralized exchange, where the relevant aspect is not only to get prices right but also the right prices - during the barter process is fruit of forcing the transplant from centralized to decentralized exchange of the dichotomization between existence/convergence and execution. In order to assess decentralized exchange this may be ineffectual. For decentralized exchange, convergence to an equilibrium set of prices and existence of a coordinated set of trades cannot be separated,⁶² and thus convergence and execution lose autonomy. Moreover, in decentralized exchange, the meaningful exercise is not of convergence to an equilibrium price set but the convergence to a feasible set of trades (for a tentative explanation, see next section (iv)).

In fact, as traditionally defined, existence is a notional state, and convergence is a virtual exercise. Trading, however, involves not the consistency of plans but the matching of active demands and supplies. A tentative conclusion⁶³ seems thus to be, for the sake of 'conceptual coherence,' entirely to subsume convergence to the equilibrium price set under convergence to (and execution of) a coordinated set of trades, relying on a coherent set of informational assumptions. For decentralized trading arrangements, convergence to the equilibrium price set cannot sensibly be imposed as an

⁶²Veendorp [1970a, 10] notes the importance of this distinction, between "...the problem of convergence of a bartering process from that of the existence of a feasible trade."

⁶³Veendorp's suggested solution to the problem of the inconsistency between existence and execution is to redefine existence as requiring feasible sequences of barter exchange. We agree with Veendorp, that in the case of direct barter economies "...it should be realized that the traditional conditions for the existence of an equilibrium solution are insufficiently restrictive. To be economically meaningful the equilibrium solution of a direct barter economy should not only satisfy the usual non-negativity conditions for relative price and consumption levels, but feasibility conditions for direct barter as well" [Veendorp, 1970a, 6]. I agree, but not exactly to salvage existence. My argument derives only from an attempt at consistency regarding information assumptions in direct barter. (Another 'solution', as suggested by Veendorp [1970a, 7], is interesting since it allows to question the absurdity of defining an equilibrium solution of a direct barter economy as implying feasibility conditions for direct barter as well: "Working backwards ... one can generate feasible excess demand patterns".)

a priori postulate.

(ii) Veendorp [1970a] makes the point that a decentralized exchange arrangement like direct bilateral bartering may fail to allow trading plans to correspond to feasible trades. The author started however from the assumption that prices were equilibrium prices, and deduced the logical implications of such knowledge he endowed his traders with. From this standpoint Veendorp's conclusions are devastating enough.

But now I would like to ask the reader to imagine himself not as the omniscient storyteller but as one of the characters in the story lacking full information. Let him be a trader in a decentralized market. And now let us observe his certainties and his questions or doubts.

Suppose first that the trading rule is able to accomplish feasible trade, so that planned trades are consummated. If this is the case, the quid pro quo condition (which is decentralized) is sufficient to generate this result. Let us suppose, alternatively, that direct barter in a set of trading posts is unsuccessful, given prices; i.e., predetermined trading plans cannot be accomplished. If execution cannot be accomplished by any set of trading rules of the storyteller's creation, that obeys some restrictions like informational decentralization, we say it is not feasible under such restrictions. What could our trader infer, or what can some decentralized viewer infer from the observation of the results, that direct barter was unfeasible given equilibrium prices, or that, on the other hand, prices were not equilibrium prices to begin with? If he would give a thought to it, he would be unable to infer. So should the character in our story.

Full execution may be feasible under quid pro quo, at given predetermined equilibrium prices (the market clearing condition is not binding in such possible case).

It may not be feasible, though (and the trading rule becomes binding). On the other hand, if we assume that prices are not equilibrium prices, full execution is not feasible (both the trading rule and the market clearing rule are binding). As a consequence, unfeasibility of trading would provide a noisy signal to any "decentralized" market participant in our story that would care to mind. Let us put this in perspective, in the mind of the storyteller.

Under quid pro quo, inability to complete planned trades in direct barter provides a 'mixed' signal to traders and 'specialized brokers'; their response may be to attempt to carry out some unfeasible trades at the going prices by way of bargaining. They may be leading the price signals towards equilibrium or, on the contrary, give rise to a derailment of the (notional) equilibrium price signal.

Decentralized information is compatible with quid pro quo (or its aggregative form, as in Veendorp). The market clearing rule is not - under limited knowledge of other traders' excess demands and supplies, individual traders cannot compute market excess demands at any step of barter - and accordingly we should leave it aside as a control mechanism in trading. Thus, if we postulate information decentralization, individual traders who face the inability to complete their desired trades may be led to proceed exchange and attempt to bargain, in order to further their "gains from trade" - consequently adjusting prices. To just potentially end up 'derailing' the price signal, which might just possibly as well be the equilibrium set of prices. We are led to the discomfoting conclusion that in decentralized barter there is lack of information in the market to let individual traders infer which state they are at, whether in a notional equilibrium where exchange is unfeasible, or in a situation of market disequilibrium to begin with. We aim at a world of decentralized exchange: in pairwise meetings,

transactors don't know and don't care about anyone else, about rules, or market equilibrium. Rather, the presupposition of equilibrium prices can be dropped, without harm and possibly easing the understanding of the logistics of barter. In fact, if we contemplate barter of given quantities (g) of two goods (i and k), between two individuals (j and l), exchange means that g_j trades for g_l , and so we have $g_j/g_l=1$ (cf. Pareto [1909/1927, 178]). Or, in general, $g_j/g_l=p_k=v_k/v_i$, with v_k and v_i standing as the value of goods k and i in exchange⁶⁴ (expressed in a common unit of account⁶⁵). Thus, barter is balance.

(iv) Feasibility of trades

As to the meaning of feasibility, Ostroy [1973, 609] has the right perspective: "...the term "feasible" denotes what *could* happen, ignoring individual behavior, not what *would* happen."

It is, first, a thought experiment with no claims to deal with any facts of experience of trade, but unlike the exercise on convergence, it ascribes actions to

⁶⁴Using the foregoing notation, we can express Walras' equation of exchange (Jaffé, ed. [1954, 87]) the following way:

$$g_j \cdot v_i = g_l \cdot v_k, \quad \text{or: } g_j/g_l = v_k/v_i = p_k.$$

"Thus: *Prices, or ratios of values in exchange, are equal to the inverse ratios of the quantities exchanged*" [ibid.]. Jaffé explains that "[t]his concept of value in exchange as a term in a ratio which is inversely proportional to the ratio of the quantities exchanged was adumbrated ... in Isnard" [499]. In the exchange of (only) two commodities, g_j and g_l correspond to excess supplies at the 'values in exchange' v_i and v_k , which are equilibrium values in exchange (since we are considering the exchange of given quantities of only two commodities between two individuals); the ratio v_k/v_i being designated by Walras as the "relative price" of commodity k (p_k) (cf. Jaffé [1969, esp.26]). (See Jaffé [1969, 28] for his reference to Walras' v 's as "...semantic rigmarole about value in Parts I and II of the *Éléments*").

⁶⁵The v 's are either Walras' "absolute" values (cf. Jaffé [1969, 28]) or "valorie" [van Daal and Jolink, 1993, 14], or expressed in an "imaginary commodity" ("Cournot's *tertium comparationis*") [Jaffé, ed., 1954, 499].

individuals. Consequently, and second, it is not an assertion of equilibrium or notional plans, it requires the description of transactions of goods between individuals according to defined rules. Third, some criterion or restriction is needed to define feasibility. If unqualified, feasibility has no meaning, this is only given by some restriction - as we know, centralized exchange as conducted by the auctioneer, if feasible, is only trivially so. The set of restrictions of interest concern primarily information decentralization.

Mandatory 'givens' are a set of individual traders, a set of goods, the distribution of certain quantities of these goods to individuals (endowments), and the trading rule(s) individuals are supposed to comply with in the execution of transactions; an optional given, normally postulated, is a set of common exchange rates for each pair of these goods, as predetermined before trading starts. Then, the execution of trading by individuals in compliance with the rules is described. But, in order to assess a feasible execution we need to ponder whether prices are predetermined or not:

(a) For the most commonly considered case (e.g. Ostroy and Starr), where an equilibrium price set is given, if trading can be shown to be executed to completion of the desired/planned trades without infringing the restriction, we say that execution is feasible, given the restriction.

(b) For the case where no exercise precedes trading (no prices are given or "known" and no notional trading plans preexist trade), a followed path (e.g. Feldman [1973] and Madden [1975]) is to treat execution as a sequence of utility non-decreasing bilateral trades in order to enquire about optimality. In this case where no predetermined equilibrium prices are assumed, attainment of execution within the confines of

decentralized information has not been investigated, to the best of my knowledge,⁶⁶ but that there is a trade off will become clear in due course. Another more relevant question arises here. Unlike before, we have no reference to gauge the set of achieved trades: in the Walrasian sense, the planned or target trades. But if we are unable to define *full* execution, we gain now extra degrees of freedom in the formalization of exchange. For one, we are now in a position to observe what *could* be attained given the posited trading rule(s), without the strings of necessary conformance with equilibrium, as notional consistency of plans. But, moreover, we are free to postulate whatever transaction rules we may choose with no (necessary) requisite that they comply with (notional) maximizing behavior by the individual - which in case of sequentially assessed trading opportunities may just have no rationale. Under this setting, a window is open to view feasibility as aggregate coherence of any given trading rule. And next, if aggregate coherence under a set of trading rules is shown to satisfy relevant restrictions like informational decentralization, a boundary could be set for the behavior of individual traders.

Be that as it may, feasibility is only a first, but necessary, step to make sense of trading. First, because it immediately invokes a next step, dealing with facilitating mechanisms of feasible trades, be that brokerage, or specialists, with or without a medium of exchange. And necessary, because only if trade is feasible according to some trading rule, it can be facilitated (cf. Ostroy [1973, 609]); even though it may happen that only the facilitating device will enable execution to comply with the restriction of informational decentralization.

⁶⁶For instance, Arrow and Hurwicz's [1960] *Decentralization and Computation in Resource Allocation* deals with convergence (basically the "gradient" method) as an element towards the demonstration of an optimal allocation of resources. Execution is not addressed; in fact, there is only one representative consumer, the helmsman. See also other articles by Hurwicz, in Arrow and Hurwicz [1977, esp. Part IV].

These mechanisms are paid for in that they economize on set-up costs of transacting. And here we can see why it was said above that feasibility doesn't deal with facts of experience. None of the ensuing analyses of feasibility of trading does consider set-up costs of transacting,⁶⁷ and this is enough revealing symptom that all is done there is a 'contemplation' of trading. Even if 'middlemen' or 'money' are called in, they are ad hoc features (cf. Starr [1971, esp.3 and 16-8]). Moreover, search models that generate endogenously the emergence of middlemen or of a common medium of exchange have only a partial claim to be dealing with decentralized exchange; all these models are equivalent to trading of coconuts one for one (Diamond [1982]).

(v) Decentralized execution and sequential trading

Next, we shall consider sequential trading, which means abandoning the neowalrasian 'simultaneous' multilateral barter and adhering instead to pairwise/bilateral barter, either direct or indirect also, in any case sequential.⁶⁸ (Unless we assume

⁶⁷Multilateral trade is assumed to be very costly, and this is the implicit rationale for alternative formalizations to resort to decentralized logistical arrangements based on sequential barter. Of interest here is Feldman [1973, 471], who raises the subject in a very unconvincing way since he substitutes "endless series of bilateral trades" for the multilateral gathering, and thus provides in fact no rationale for his suggestion that information is costless in bilateral trade but "prohibitively costly" in multilateral trade. The transaction cost argument hardly fits feasibility.

⁶⁸Ostroy and Starr refer to two sources of "sequentiality": "The transactions role of money challenges the implicit logistical and informational assumptions of the theory of exchange. To begin, it is vital that trade be sequential, which involves more than the time-indexing of commodities. There are various sources of "sequentiality". One is the costs of making forward contracts in an otherwise highly organized market setting, which creates a need for markets to reopen over time. Another is the simple fact that in most instances individuals trade with each other one at a time." [Ostroy and Starr, 1990, 56]

traders have no 'perfect foresight'⁶⁹ or that contracting in future exchange is not costless, sequentiality may be "inessential" as shown by Radner [1972; also 1968] and Hahn [1971; 1973b]: models of sequential exchange correspond to 'one-shot' exchange as in Arrow-Debreu where all choices are made at one instant of time (cf. Arrow [1968, 387]; Clower [1977, 233-4]).⁷⁰)

Now we have to face the question of how sequential trading has been modelled. Merely presuming that traders meet sequentially in pairs is not enough to characterize the market arrangement. Aspects like the following matter: whether traders search or are assigned a predetermined list of potential trading partners; whether they trade only a pair of commodities at a meeting or they trade any size collections of commodities; whether trading occurs in a sequence of special commodity exchanges (all traders gather at a trading post to exchange two commodities bilaterally), or in a sequence of pairwise meetings (pairs of traders meet to exchange all commodities bilaterally). One possibility is to assume that each trading post opens successively (Veendorp [1970a], Benassy [1975]); another is to specify, parametrically, pairwise encounters of individual traders (Ostroy [1973]; Ostroy and Starr [1974; 1990]); finally, we may let individual traders search for trading partners randomly according to some statistical distribution (e.g. Diamond [1982a] and others for monetary exchange, as in Diamond [1984a], Kiyotaki and Wright [1989] and Aiyagari and Wallace [1991]).

Furthermore, we have to question which 'restrictions' to maintain. At the market

⁶⁹In the sense that traders differ in the probabilities they assign to the occurrence of each state of nature, yet being assumed to form *common* expectations as to which price set will prevail in each such state (cf. Radner [1972]).

⁷⁰On the existence of general equilibrium in a sequence economy with set-up transaction costs (and the consequent nonconvexity), see Heller and Starr [1976], based on Hahn [1971].

level, the market clearing condition is maintained in order to focus attention on the logistics of exchange. But even on this dichotomized approach, this condition can be relaxed, and attempts to drop it were made (cf. Benassy [1975] and Drèze [1975]). As to individual trading rules, we have an important change. Without a central accounting scheme to enforce the budget constraint (as in the one-shot trading scheme of Walrasian ascendancy), a problem is thought to arise which is usually framed in terms of incentive compatibility: under decentralized information and with trade occurring sequentially, the imposition of a sequence of budget balances is thought to be required in replacement of the single budget constraint in order to eschew the moral hazard problem (cf. Ostroy and Starr [1990, 13]; Hurwicz [1972, 443-54, esp.446] and [1973, 27-29]). All this concern is misplaced, it is a shadow of centralized execution which has no substance in the light of bilateral contracting; if two individuals transact, quid pro quo can be assumed to have been 'enforced'⁷¹ between each pair of trading partners. Incentive compatibility in this context is another excrescence on the dichotomization between existence and execution, where notional plans precede actual transactions. In fact, enforcement of budget balance constraint at each bilateral trade is ensured in an informationally decentralized way through satisfaction of quid pro quo, which means that the value of commodities acquired

⁷¹We could say 'greedily' enforced, to borrow Hurwicz's [1973, 25] expression, but this is not needed. In contrast to "the Walrasian price taking paradigm," "[t]he Edgeworthian paradigm (1881) views economics as dealing with those aspects of social organization achieved by free contract between self-interested individuals or groups of individuals. Contract is the voluntary exchange of *quid pro quo*. What is the *quid* and what is the *quo* can vary greatly in character and concreteness from case to case, but purely one-sided arrangements - benevolence or force - are excluded. Self-interest need not be interpreted narrowly. What is required is Wicksteed's *non tuism* condition (1933, Vol. I, pp. 170-83) - neither side to a contract should have the interest of the other at heart, although each may pursue the interests of third parties." [Whitaker, 1987, 575]

equals the value of commodities delivered.⁷² But this is simply the definition of barter: if traders are observed to transact, then $x_y \equiv y_x$.

In our attempt to envision Walrasian general exchange as decentralized we abandoned the central market and replaced it with sequential trading occurring in a set of trading posts; at each special exchange, direct bilateral barter of each pair of commodities takes place. Under this trade arrangement trade occurs successively in each trading post, after all feasible trades at this trading post have been carried out, a new trading post opens and traders meet again for the exchange of a new pair of commodities. At a special trading post, each individual trader will conduct direct barter on a pairwise, quid pro quo basis. The trading rule we referred to in the analysis of Veendorp [1970a] that at each trading post total sales equal total purchases of the two commodities for each other, is just a proxy for the condition of value quid pro quo, given equilibrium prices, and therefore it is a reasonable restriction, enforceable by traders on the basis of decentralized information.

Veendorp concluded that direct barter may not be feasible; planned trades fail full execution by means of direct barter and rates of exchange may be seen in need of revision, at some step of sequential trading. Furthermore, indirect barter is hardly conceivable⁷³ in a trade arrangement made of successive trading posts and it requires the collection of information on excess demands of other traders (that exceeds the

⁷²Notice this ingenious clarification: "The price consistency condition is merely the abstraction of the fact verified by casual empiricism that when one buys something one pays the seller for it. Payment for goods purchased seems a concept almost absent from general equilibrium theory. It is required there that the value of goods demanded equal the value of goods supplied, but there is no requirement that the supplier of goods be the recipient of goods supplied." [Starr, 1972, 94]

⁷³Benassy [1975] tackled this under rather outstretched expectational assumptions.

author's view of decentralized information, that of pure competition). The logistical complications of decentralized exchange were, however, hardly introduced, and it is not quite clear how to interpret his view of trading within each trading post. All we can think of is trading posts opening sequentially and at each one *all* individual traders conducting transactions 'simultaneously' through a 'specialized broker' before they move to another trading post. An attendant will make sure that all traders are present and that, over all traders, no more value goes one way than the other. If this is so, trade is conflated within each special exchange, and its logistics ignored.

If it is granted that this is a fair account of trading in Veendorp, then all the problems dealt with by Ostroy and Starr [1974; 1990] are entirely of a different sort. Their main concern is to model and inquire the feasibility of individual trades, not to examine the consistency of trading in special exchanges with the maintained assumption of equilibrium prices.

In Ostroy and Starr there is no allusion to organized exchanges. In order to introduce logistical decentralization, they consider that the auctioneer "...retires from the scene to leave the individuals to trade on their own in pairs" [Ostroy and Starr, 1990, 13]. Here, each trader meets other traders, one at a time, sequentially. We have a succession of bilateral trades between pairs of traders,⁷⁴ that the authors presume to take place simultaneously.⁷⁵ A sequence of pairwise meetings that allows each trader to contact everyone other "once and only once" is called a round [1990, 31]. Allocation

⁷⁴"We may learn from Niehans [1969] that even when exchange is restricted to pairs it need not be completely decentralized. The selection of a least cost bilateral trading network can be made by a central planner who solves a complicated programming problem." [Ostroy, 1973, 598n]

⁷⁵It is harmless to presume, as Ostroy and Starr [1974, 1097] do, that several pairwise meetings occur simultaneously; this is of no consequence, and useful only for notational purposes: see *t*, *t-1*, ... on decentralization assumptions.

of trading partners is parametrical.⁷⁶

Trading is potentially decentralized; according to the definition of informational decentralization, it will be less so (even though the authors don't acknowledge this clearly, as seen in fn.37, above) as long as in the course of meetings, in order for any trader to execute trades, he collects information on the excess demands of every other single trader; in spite of not being contemporaneous information, it may help each trader "...to make more precise estimates of the probable excess demands of future partners" [Ostroy and Starr, 1974, 1097, 7n].

At each meeting information on net excess demands, based on equilibrium prices, is communicated and trade may take place, if the following restrictions are satisfied (cf. Ostroy and Starr [1990, 33]). Beyond the conditions that (i) no trader can have at any step of barter "a negative holding of any commodity" (no credit), and that (ii) trade is pairwise ("goods delivered are received"), which implies that commodities are conserved until trading is completed (i.e., not consumed, nor disposed of), we may choose to add (iii) the quid pro quo trade restriction. This condition, as applied to pairwise multi-commodity barter, restricts trading between two traders at each "bilateral encounter" so that the total value of sales is equal to the total value of purchases, given equilibrium

⁷⁶Timing coincidence, more than coincidence of wants, is important for the explanation of market arrangements. Timing coordination is exogenously posited in Veendorp by conducting trade in organized exchanges with a timetable associated with any of them; organized exchanges do not mitigate the timing question unless a timetable for every exchange is postulated (or we allow 'organized exchanges' to be run by specialist middlemen and let them create a continuous ready market for other traders). On the other hand, timing coincidence is left to 'atomic' 'collisions' in the search models. Ostroy and Starr, differently, choose to leave it aside; they acknowledge, however, that "...direct treatment of the timing decision would introduce greater complexity than we wish to treat in this model" [Ostroy and Starr, 1990, 34], but they notice that the "...requirement [of explicit timing decisions of individual agents] enters essentially, however, in the analysis of sequence economies with transaction costs."

prices (cf. Ostroy [1973, 598]). That prices are common knowledge is basic for understanding the imposition by traders of this quid pro quo condition on each other.

Thereafter, pairwise trading rules are postulated which define which trades each pair is allowed to perform and the information available to each of them at each step of barter - assumed decentralized at each pairwise meeting. At any pairwise meeting, and at any instant of the sequence of meetings, each trader is supposed to have information of "currently unsatisfied excess demands and supplies" of the trading partner, the names of the trading partners, or, at the most, of (only) the two traders' previous trading history (cf. Ostroy and Starr [1974, 1097]).

Under this roundabout barter arrangement, some conclusions are worth mentioning (Ostroy and Starr [1974]; and [1990, esp. 35-9]). First, full execution of barter trading can be achieved in one round of meetings: there is a centralized assignment of a chain of trading partners for each trader to enter at in the course of the sequence of meetings which allows full execution (besides other unpalatable features, it will require indirect barter (cf. Ostroy and Starr [1974, 1102])). The authors also prove that,⁷⁷ at given exchange rates, there is no informationally decentralized barter rule that will attain full execution in one round, hence their contention that it is impossible to decentralize exchange in a barter economy at equilibrium exchange rates (p.1103). Only given information on excess demands of other traders, either than the two meeting pairwise, could each trader decide which trades to carry out that would be amenable to

⁷⁷ "...within the class of all functions (rules) whose domain is what the traders know and whose range is their sets of feasible trades, there is none which satisfies the stated conditions" [Ostroy and Starr, 1974, 1103]; that is, conditions established in Theorem 2 [1098], namely, (A): admissible trades, (D.3): informational decentralization, and (E): full execution in one round.

achieve execution of planned trades in one round of trades.⁷⁸

Finally (pp.1108-11), the authors aim for a positive conclusion. In a crude form, this is that monetary exchange will allow for decentralized execution that is consistent with planned trades, thereby economizing on information about individuals' net excess demands. Another result [Starr, 1976, 1087] is that "...the use of money economizes on trading time."⁷⁹ But let us be more specific.

If allowance is made for repeated rounds of meetings among all traders, the authors show that convergence to full execution may be attainable in the limit as time tends to infinity. On the other hand, they consider two sets of situations in which full execution is attainable in one round of trades. One is the above referred centralized trading rule (cf. Ostroy and Starr [1974, 1098 and 1102]). The other relies on "...enough slack in initial endowments - either a trader whose endowments are sufficient to fulfill all others' excess demands..., or a commodity such that the value of each trader's holdings of it is at least equal to the value of his planned purchases of all other commodities" [1108]. In the first case, a trader "acts as a clearinghouse"⁸⁰; the second case is inaccurately defined in the [1974] article: a commodity *m* works as a "...counting device to insure that the sum of additions to and subtractions from the value of one's holdings during the course of trade is zero" [1111] - one commodity is chosen as the unit

⁷⁸This centralized solution would require indirect barter and relaxation of the quid pro quo rule. We should grant the authors' point that "...in a world of complete information the requirements for enforcing overall budget balance are met, so quid pro quo is an avoidable constraint on the transaction process." [Ostroy and Starr, 1990, 11]

⁷⁹Adding immediately: "Barter mechanisms can succeed as quickly as monetary trade if coordination and sufficient market information are freely available. In their absence, successful barter may require much longer." [Starr, 1976, 1087]

⁸⁰The possible fact that this trader may fail to have enough "quantities of his own commodities" creates a further embarrassment (cf. Ostroy and Starr [1974, 1110]).

of account of a, let us say, 'central credit' payment system: "[the trading rule] narrows the choice of means of payment to commodity m without, however, imposing the restriction that m be in excess supply before it is given up" [1109].

It is bizarre to call this commodity money, or refer expressly to medium of exchange when the accounting book (commodity m) is just used to cancel out trading accounts when quid pro quo fails to be satisfied (p.1111). This slippage into 'telematic' money (cf. Ostroy and Starr [1990, 11]) stretches the decentralization assumptions. It reveals that the authors fail to cope with execution as something distinct from consistency of planned trades, and so raises the question of what is being investigated.

We must pay attention, nonetheless, to how less confused - though erroneous - the later [1990] version of the subject is compared to the earlier [1974], which was obtained by means of a taxonomic distinction between a monetary and a bank credit economy. More precisely: (i) by narrowing the definition of a monetary economy to the case where "...there is a zeroth good universally held in a quantity sufficient to finance all purchases" [Ostroy and Starr, 1990, 35], and "...failure in quid pro quo is made up by trade in 0" [38]; money is just enough to slacken the budget balance; and (ii) by relabelling the second case "bank credit economy," where the "bank" is allowed to violate the "non-negativity requirement"⁸¹ and "...with the credit instruments working as money" [36].

Some general comments are in order. First, the functional confusion regarding the medium of exchange is not properly addressed. No clear definition of money (and of money versus credit) is provided, the outstanding feature seeming to be that of "blue

⁸¹Which is "...contrary to the idea of informational decentralization" [Ostroy and Starr, 1990, 35].

chips" or a record-keeping device.^{82 83} This is far too clear in the credit economy; it is even granted by the authors that it violates informational decentralization. Whereas the case of slackness of the money commodity seems to imply that existence (and convergence) is not independent from execution, if the 'value' of the medium-of-exchange-commodity(ies) depends on the ease of trade enabled. This is well spelled out by Patinkin [1989, xxxiv], as referring to Ostroy and Starr [1988, sec.1.2; identical to [1990, sec.1.2]): "...who point out that in order to determine the utility of such balances, the household must first have a general notion of the volume of transactions that these balances will have to perform; and this can be known only after the household has determined the outcome of the process of utility-maximization itself."

This conclusion that existence is not independent of execution is here ascertained in the context of a monetary economy, as has been long recognized: "In the usual existence problem the 'initial' position of the participants can be described independently of prices, i.e. in terms of the initial endowment of goods, technological knowledge, etc. The interesting point of a monetary economy is that we cannot do so. For it is one of the features of such an economy that contracts, as Keynes noted, are made in terms of money." [Hahn, 1965, 131-2]. But the reason lies in a separate, and previous aspect. The origin of the problem is not specifically the medium of exchange property of the money commodity but the introduction of "actual transaction opportunities" and "actual

⁸²An obvious record-keeping device is for the clearing-house to issue blue chips to each person in the amount of the excess of the value of the goods supplied compared to those received." Adding, "[b]ecause prices are fixed at market-clearing values, each person can silently spend his chips on the available supplies when he returns to the auctioneer, knowing that all supplies will eventually be claimed by those who have a demand for them." [Ostroy and Starr, 1990, 9-10]

⁸³Alchian's [1977] contention is that monetary exchange cannot rest on a "book-keeping, debt-recording function."

relationships" [Hahn, 1965, 131 and 133].⁸⁴ Trading, and feasibility of trading, is the problem, not money as a facilitating device.⁸⁵

Moreover, we may ask now what meaning has - in this different construct - Ostroy and Starr's [1990, 34] assumption that the money endowment is sufficient to permit feasibility of trades.⁸⁶ Since the problem is a value problem now (as the authors indeed recognize), any quantity will do, it purely doesn't matter; we may assume any given endowment of the money good. If existence is concomitant to execution in this fashion, the sufficiency question loses all meaning.⁸⁷

Overall, the problem in Ostroy and Starr's assessment of execution seem to derive from their trouble remembering the assumptions, namely informational decentralization; still, it has to be acknowledged that their work is the most thorough, and reliable, source

⁸⁴As to the construction of "a model which can serve as an adequate foundation for a monetary theory," Hahn [1965, 131] states: "It must distinguish between abstract exchange opportunities at some notionally called prices and actual transaction opportunities. The latter requires a precise statement of the methods of transactions open to an individual with their attendant costs."

⁸⁵This is why Colander [1994, 10] is misguided in talking about money as "...imposing certain institutional constraints on individuals, which break the [Classical] dichotomy." Constraints surely are present, but they belong in exchange. Arguments of this kind usually don't notice that it is the medium of exchange property of commodities in exchange that originates the constraint. Money brings nothing new, except for helping alleviate constraints, and therefore "...money makes the economy more efficient." (This is altogether different from the proposed idea that: "...money will be defined theoretically in terms of explicitly postulated restrictions on trading alternatives that assign a special role to certain commodities as payment media in organized markets." (Clower [1971, 109]; see also [1967])

⁸⁶"In order for successful monetary trade to take place without violating (A.1), non-negativity, agents must have, at each trading instant, sufficient money to finance their current purchases. The money will come from endowment or the proceeds of past sales. We are interested then in characterizing economies with sufficient endowment of money so that illiquidity due to exhaustion of money holdings in the course of trade need not be a problem." And it is added: "...we will characterize, at least at first, a monetary economy as one endowed with a sufficient stock of a monetary commodity to be used as medium of exchange. It must be distributed sufficiently broadly in sufficiently great quantity (*in value terms*) among the holders that all agents find that they can finance all desired purchases from endowment of the money commodity" [Ostroy and Starr, 1990, 34, italics added].

⁸⁷Even though the problem is primarily one of value, it is plausible to presume that quantity restrictions in money holdings will afflict traders in a notional equilibrium, unless consistency of trading opportunities is part of the definition of equilibrium. The authors' argument may be still valid, though it ought to be properly framed.

in this area. Be that as it may, our attempts at critical analysis are only meant to disentangle the arguments so that our reasoning can lead to finding some positive way out. One conclusion seems reasonable: dichotomization of the existence and execution has not yet provided the basis for the solution to the attempt to view execution as a decentralized affair. Existence of notional consistency of plans as metaphysically postulated in decentralized exchange is possibly tying down understanding of execution. Consequently, existence and equilibrium may have possibly to be brought down to earth were they to become operative concepts in the explanation of the working of competitive markets. Without further elaboration at this point, the suggestion is clear that we will have to venture into a world where existence is not supposed.

(vi) Alternative attempts to formalize execution

Let us attempt a broad classification of decentralized logistical arrangements, where the organizing criterion is the facilitating device (brokerage or specialists, and money). I could glean the following types of formalizations in the literature:

(1) Organized exchange in trading posts ($n(n-1)/2$ exchanges), with trade facilitated by a set of (external) 'specialized brokers'. This is the case of Veendorp [1970a] and Benassy [1975].

(2) Sequential bilateral barter rules, in two different contexts:

(2.1) Given equilibrium prices, and requiring quid pro quo valued at equilibrium prices; this is the case of Ostroy and Starr [1974; 1990]. I will presume that the conclusions of the analysis of Veendorp, and Ostroy and Starr are sufficiently clear from

above, and will not elaborate.

(2.2) In which prices are not defined (and, therefore, not known), exchange is not constrained by the requirement of quid pro quo valued at equilibrium prices, and in which each bilateral barter is utility non-decreasing. This is so in Feldman [1973]. In Madden [1975] we have additionally that there are "small" groups of traders and only the traders belonging to the groups are allowed to meet; Madden allows groups to meet sequentially, and bilateral trades to take place between the members of any two groups at a time. Madden deals with both problems of existence of a feasible trade and of convergence of a bartering process, but his main concern is with efficiency in exchange.

The introduction, by assumption, of a money commodity in sequential bilateral barter will ease the coordination problem in Ostroy and Starr, by permitting to expedite the barter-cum-money exchange, given the slackening function of money. Feldman doesn't deal expressly with the logistics of barter, i.e. "...the conditions for the effectiveness of bilateral trade move sequences" [1973, 471] - rather, an example is presented where, notwithstanding convexity assumptions, optimality is not established pairwise. He shows, though, that introducing the requirement that every trader is endowed with a given commodity ("money"⁸⁸), this guarantees that sequences of barter exchange (among all traders) attain optimality in allocation.

Madden gets to a similar result (p.589:Theorem 5). Another special conclusion in Madden [1975, 588:A.5; and 589:Theorem 4] is the following: if each group contains only one trader ("middleman"), the author shows that for optimality in exchange "...we require that all middlemen are connected irreducibly and all traders who are not

⁸⁸Madden [1976, 589] criticizes Feldman for this misnomer.

middlemen meet at least one middleman." Irreducible connection in this case means (according to Rader [1968]) we have a set of middlemen, such that: (i) they have common, uniquely defined support prices (rates of exchange allowing for utility non-decreasing trades), and (ii) all pairs of middlemen are allowed to meet. Furthermore, for the general case, Madden [1975, 592] shows that, given sequences of rounds of barter - more specifically, infinite sequences of predetermined cycles of bilateral barter among traders of each two groups - "...there exists a sequence of meetings of groups which exhausts the gains from trade."

The final question arises whether these proofs of feasibility satisfy the restriction of informational decentralization. In the general case, where bilateral barter among the traders belonging to any two groups occurs in a sequence of meetings of any two groups, as well as for the two special cases of middlemen and medium of exchange, the logistical construction relies on an indefinite number of rounds, which is not a decentralized procedure (according to Ostroy and Starr's definition).

(3) The consideration of "endogenous" brokers in bilateral trade, based on the assumption of a fixed cost for each bilateral deal. Townsend [1978,1] proposes a non-cooperative game by means of which a subset of agents acting as intermediaries "...economize on the fixed cost of exchange." A more promising approach was attempted by Rubinstein and Wolinski [1987] where intermediation is a time-saving device in a market characterized by a matching process that is time-consuming (cf. Diamond [1982b] and Mortensen [1982a]). Here, middlemen are posited as a third type of agent, beyond sellers and buyers, and the model considers stationary numbers and trading opportunities; an indivisible good is traded, when a buyer and a seller have

transacted they leave the market, but middlemen engage perpetually in search and transacting, though they cannot store more than one unit. The matching process between middlemen and their customers is modeled explicitly, and the extent of that activity is endogenously determined, as well as the transaction costs; the model is extended to study the implication of the middlemen assuming ownership of the good (dealer versus consignment - see Hackett [1992; 1993]).

(4) The explanation of the endogenous emergence of media of exchange, due to transaction costs. The emergence of a general medium of exchange commodity due to search costs is explained in Jones [1976] and Oh [1989]⁸⁹ (in the line of Niehans [1969; 1971]; and as hinted in Brunner and Meltzer [1971, 787-8]⁹⁰).

Information is decentralized, equilibrium prices are given and chosen to be I in terms of a numéraire, trading occurs bilaterally, and quid pro quo is satisfied by the pairwise transaction of any two goods; besides, each individual is endowed with only one unit of a single good (which he exchanges in order to obtain the other good he

⁸⁹According to Oh, Jones' model doesn't explain the emergence of a generally accepted means of exchange, only one good will be money but not for all pairs of goods. In any case, Jones [1976, 758] defines a monetary economy this way: "We shall say that an economy has a *monetary pattern of trade* if the exchanges which actually take place have the following two characteristics: (a) There is one good that enters into every exchange. (b) Any other good entering an exchange, if purchased is not sold, and if sold is not repurchased. The one exceptional good is termed the "medium of exchange."

Differently, Oh [1989, 104] provides the following definition: "A monetary economy is referred to as an economy that has a generally acceptable medium of exchange, rather than one in which every exchange is carried out through a medium of exchange." This obtains meaning given that "...individuals use conditional trading strategies" (and thus "...pure barter trade can exist as a conditional option in a monetary economy side by side with a generally acceptable medium of exchange" [113]).

⁹⁰In a broader context Brunner and Meltzer [1971, 788] state: "Numerous sequences of transactions are open to [an individual]. His problem is to find the optimal sequence of transactions and the optimal investment in information while choosing an optimal bundle of goods or consumption plans."

Their first postulate on acquisition of information (p.786) is akin to Jones' assumption that the cost of exchange depends on the pair of goods involved, and the second postulate on the marginal cost of acquiring information is what drives the "dynamic" result in Jones.

ultimately demands). The central assumptions are, however, that traders "...do not know with whom they can or will make given exchanges", and that exchange involves a cost, which depends "...only on the pair of goods involved and the size of the trade" [Jones, 1976, 760 and 761]; i.e., they propose a proportional transaction cost, though differentiated for each pair of goods. Minimization of search costs or expected time (which is a random variable) means, given a constant rate of search, minimization of the number of contacts. Expectations about the willingness of a randomly contacted trader to supply or demand any particular good are constructed on the basis of previous contacting experience, and it is assumed that goods offered and demanded by any individual are independent. Aiming at a given ultimate demand, before the individual enters the market he "...plans a fixed sequence of trades which will effect this ultimate exchange" [762]. If the expectation is formed by individuals (according to their experience) that there is one commodity most commonly offered in trade, and this belief is common as to which commodity provides a sufficiently high probability of being offered in exchange against some subset of goods in the economy, this commodity will be used as a medium of exchange for the acquisition of such goods. Achievement of equilibrium - meaning that beliefs are correct - will be attained through a recursive meeting process during which the medium of exchange becomes increasingly common in exchange. And, according to the configuration of the probabilities of ease of trade in direct barter or intermediated (two-stage) trade between any two pairs of commodities, (unique) degrees of monetization of this economy can be achieved.

Oh [1989] broadens the previous result by relaxing the assumption that each trader fixes his trading strategy before entering the market. He replaces this by a conditional trading strategy. An ordering of goods is postulated according to their probabilities of

commonness in trading offers, and thereby "...individuals will not pass up the chance of getting a more saleable good by giving up a less saleable one" [Oh, 1989, 102-3]. As to the conclusion of the model, Oh adds: "The conditional trading strategy generates a generally acceptable medium of exchange with partial monetization."⁹¹

Concluding this section, let us distil a few simple, and exploratory, conclusions:

(i) Proofs of existence and convergence of feasibility given restrictions of informational decentralization are in a very poor state. Ostroy and Starr [1974; 1990] and Madden [1975], built upon Feldman [1973], seem to be the only general attempts.

(ii) This collection of articles points towards two basic (generally alternative) facilitating devices: brokers or middlemen, and a medium of exchange.

(iii) In order to show feasibility of bilateral barter in an informationally decentralized fashion, some means of *connection*⁹² is summoned, be it (a) a set of external brokers [Veendorp, Benassy], or "middlemen" [Madden] (here middlemen are posited, but in Townsend, or Rubinstein and Wolinski, they are endogenous); or (b) a commodity with the property of medium of exchange [Ostroy and Starr, Feldman,

⁹¹The conditional trading rule will enable to achieve the good ultimately desired in a smaller number of expected contacts than with the fixed trading rule. (Differently than Jones, who bases evolution to equilibrium on an adaptive learning process, Oh postulates rational expectations (cf. Oh [1989, 107]).)

⁹²This is here used in the broad sense of Clower [1994b, 3]: "...each marketor is economically contiguous to at least one other marketor, so the set of marketors - also the set of marketees - is economically connected." Also of interest is Stigler's [1957, 258-9] reference to brokers in his discussion of "complete knowledge" as one of Knight's assumptions of perfect competition; notice also the role of "intermediaries" in Hayek [1945, 526].

For another, and specific, definition of connected economy (as an assumption complementary to weak gross substitution), see Arrow and Hahn [1971, 227].

Madden [1975, 588], dealing with the needed "...assumption on the smoothness of indifference surfaces," introduces the notion of connected "groups" in order to provide a common supporting price set in trades between individuals (meeting pairwise) belonging to any pair of groups. This is a common feature, though, of topological proofs of existence; the innovation here is the application of the notion to groups, this allowing for the introduction of middlemen (as in Rader [1968]).

Madden, Jones, Oh]

(iv) A link between intermediation and monetary patterns of exchange is ultimately the interesting aspect to explain. This point is clearly made in Clower's *The Money Puzzle*. In the presence of set-up costs of information and transaction, the activity of a trader as a specialized middleman would be paid for by economizing on those costs by other traders. But to have explained that a middleman would specialize (e.g. in trading just two commodities) does not imply that the organization of trade would be "monetary." Even though no firm theoretical basis is easily provided to the historically supported conjecture that "...monetary exchange arises naturally from much the same forces of self-interest that induce individuals to make markets", a conclusion is warranted: if "...business firms and markets organized and operated by them lend coherence to exchange activities by establishing well-marked and easily accessible channels through which household and other transactors may trade", in an ongoing economy money works as the web through which "economic activities are coordinated" [Clower, 1994c, esp.16-7].

The same need to bring together the two salient trade-facilitating devices is equally expressed in Oh, though he has started from money:

...even in a monetary economy there still exist substantial transaction costs given that individuals search for traders who have what they wish to consume. Thus, money solves only part of the problem of the existence of transaction costs. This fact may explain why trading posts have developed. In this sense, money, defined as a generally acceptable medium of exchange, and trading posts seem to be complementary aspects of individuals' attempts to minimize transaction costs. [Oh, 1989, 117]

4.3.4 - The obstacles of the Walrasian program

Decentralization of exchange is a difficult matter and I am not proposing a solution. The intention is only to investigate the implications of possible alternative ways to deal with the subject; each one brings special problems, which have not yet found a satisfactory answer. The task is a simple armchair exercise to map out possible paths to follow. I intend only to locate the obstacles, indicate the bridges to be built, and so on. I envision two general directions to seek a possible way out, yet each one faces apparently insurmountable obstacles.

Equilibrium in a pure exchange economy

When discussing the meaning and usefulness of equilibrium notions I am confined to an exchange, stock economy, knowing however that it is meaningless to make sense of markets, of institutions for trade created to economize on costs of transaction. Especially, decentralized markets can only be adequately understood, and therefore formalized, for the case of ongoing, stock-flow economies where the notion of equilibrium can only be described along the lines of Leijonhufvud and Clower [1973, 89], but for the fact that "...the values of all variables that are considered relevant for describing observable behavior [of an economic system] over time" are not to be related to "...the values of a corresponding set of theoretical variables that define the virtual (notional) behavior of the system along a postulated equilibrium path" but rather to the variables so defined that the mechanics of trade and its feasibility are not left unconsidered. Whether, and how, this can be formalized is not my problem now. I am not venturing into the world of ongoing trade arrangements, or "the continuous market"

in the words of Walras [Jaffé, ed., 1954, 380], not even of the Hicksian temporary equilibrium type (with sequential endowments, and discrete (re)contracting). That is, of the two functions that, according to Hahn [1970, 5-6], the invisible hand is supposed to perform, first, that "...it should establish an equilibrium at every stage of the sequence", and, second, on the "...inducement of a coherent sequence of such equilibria", the second is totally ignored. All I am attempting is to ask what is the implication of the argument above developed on the meaning of equilibrium for a 'stock' exchange economy, with only one "shower" of endowments. If we are to be confined within the Walrasian program, the question to ask is how the incorporation of logistics into the 'static' model of exchange has been attempted or circumvented, and whether the Walrasian program withstands such intrusion.

Framework for a solution

A first direction would be to reinforce rationality, that is, to build price decisions upon the rational behavior of individuals in order to replace the predetermination of prices: bargaining and trading would go together. The real problem is that once we give up the notion of planned trades and attempt a contemplation of the execution of trades, we cannot hold onto notionally determined individual net excess demands; i.e., dispositions to trade of every single commodity determined 'once for all' before trade starts. Trading opportunities are not predetermined, only the mechanisms of exchange will allow for their definition, and thus we lose the anchor of notional equilibrium.⁹³

⁹³Burstein [1968, 25-6] discusses the meaning of disequilibrium, and states that, like in the physical sciences, disequilibrium "...can only be defined relative to a theoretical model." Using the 'Harrodian' growth model as illustration, he succumbs to the obvious: "It would seem that *equilibrium* in economics cannot have precise meaning outside of the notional state of universal pure competition in auction markets."

The question to ask first is then: Is it possible to adapt or redefine the notion of general equilibrium (i.e. for the economy as a whole) to meet the degree of feasibility of decentralized trades?

A deeper problem surfaces, however, that may compromise this line of enquiry, and this is the effect of transaction costs on the generation of equilibrium behavior by individual traders. Rational behavior is incompatible with Lucas' view of economics - in line with Hahn [1973a, 18-28, esp.25-8] - as "...studying decision rules that are steady states of some adaptive process, decision rules that are found to work over a range of situations and hence are no longer revised appreciably as more experience accumulates" [Lucas, 1986, S402], unless some cost is present (information or transaction costs) that leads the individual trader to 'routinize' his behavioral patterns. But as has been shown, those costs are necessary to explain trading arrangements. Markets, created to economize on transaction costs, may well therefore be at the root of stories explaining the viability of convergence of adaptive processes to steady states.

Both patterns of individual behavior, and market arrangements (the observable modes of interaction among individual traders) can be seen as issuing from the same basic mechanism, economizing in information and transaction costs;⁹⁴ trivially, the existence of trading arrangements (and money) catalyzes the convergence of adaptive behavior to observable regularities; not so trivially, both may have the same economic reason.

Without transaction costs (implying trading arrangements) no recognizable patterns

⁹⁴As Hayek's [1948, 106] concise conclusion points out: "Competition is essentially a process of the formation of opinion; by spreading information, it creates that unity and coherence of the economic system which we presuppose when we think of it as one market."

of trading could be expected. Direct barter is a serious contender as the prevailing trade mechanism, and no incentive whatsoever would be present for learning "...as more experience accumulates." If we don't consider transaction costs, the individual can only be seen as going on searching and anonymously pairing up until he would gather his preferred bundle. What sense can be made of learning and "adaptive" processes to "modes of behavior" that are "steady states"? (cf. Lucas [1986, S401 and 402]). Yet, we could surmise that if some regularity of endowments would prevail, individuals would attempt to establish regular meeting patterns, but to raise this possibility is to beg the question! Why would 'manna' fall in regular patterns to start with?

Two doubts arise as a consequence. Once transaction costs enter the picture, a tradeoff will be present between 'desired' consumption bundle and the continuation of meetings (in order to the achievement of the 'desired' (notional) bundle, or more appropriately, the feasible bundle); and this is where our troubles with the definition of equilibrium gain a concrete form and some practical interest.

More importantly, as seen, if transaction costs are lump-sum, intermediation is a reasonable outcome of 'rational' trading. Therefore, we may lack a good reason to proceed analysis of barter in order to understand the working of the economy, but this sounds a rather poor argument; in any case, to frame it more adequately we may ponder the other possible approach.

A second direction towards a solution to the Walrasian program would be to abandon altogether the postulate of rationality as used towards the determination of prices by a fictional agent; rationality here is of limited usefulness if it only allows for a notional consistency of plans. In Arrow-Debreu we start with plans, and we have formal theory of how they are 'coordinated' by prices; but to describe actual trades, we must

append logistical glosses that seldom make sense. We might start the other way around. Do logistics of barter exchange, and then ask the reverse question, namely, about theory of behavior that corresponds to the assumed logistical facts.⁹⁵ That is to say, if the execution of trades could be formalized in a decentralized 'setting', then investigation would proceed on which behavioral rules would be compatible with such a result.

As should now be clear, to formalize the logistics of barter under decentralized information as a basis for understanding 'coherence' in the theory of general economic interdependence has been a hard task, and appears to promise only uncertain payoffs. Or its interest may even be questionable, unless for the purpose of making clear how crucial the mechanism of exchange is to make sense of markets. Barter is an encumbrance and 'solutions' apparently have been found that deal with that: these are markets and money. The real interest of studying the logistics of barter would be then accomplished once it has helped to find a satisfying way to describe the roles of intermediation and monetary exchange in the working of markets and the economy. I am not implying that we have come to this point, nor that dealing with the difficulties that the logistics of exchange pose is not worth a try, or several. All I am doing is basically repeating Veendorp's sensible admonition, in the course of his proposal to

⁹⁵This has a parallel to "the can-opener philosophy," to borrow the image Velupillai uses (as he refers to existence proofs, in the course of his severe criticism of Katzner's unqualified defense of methodological individualism as the ground to erect general equilibrium). Velupillai succinctly writes: "...how to build a behavioral economics based on methodological individualism that does not rely on preferences at all. ...I have constructed agents as decision rules... In the next step, to study and analyze the average behavior of a collection of agents - fashionably, but misleadingly, called aggregate behavior - one investigates the coupled outcomes of a collection of decision rules. It is as if several processes were activated in parallel... Equilibrium, on this context, will be coherent outcomes. Since such an analysis is inherently constructive in the strict sense of computable analysis, existence proofs automatically carry information about the way coherence is achieved." [Velupillai, 1991, 28-9]

reconstruct the theory of barter exchange:⁹⁶

Fortunately, the defense of an analysis of bartering does not depend on the desirability of such an ambitious attempt to demonstrate the intuitively obvious. Even if one accepts the familiar hypothesis that barter "is so inefficient a method of transacting that its cost effectively rules it out of the realm of relevance" [Kuenne, 1958, 2], a better understanding of the inefficiency of bartering may help in analyzing the operation of a money economy. The means of payment function of money has received scant attention in the literature; tracing the implications of the absence of a universally accepted medium of exchange is likely to increase one's appreciation of the essential function of a money commodity. [Veendorp, 1970a, 22]

Despite this pessimistic stance, let us consider each path more closely, with a view to render the Walrasian program fit the facts of logistics:

(i) Bilateral bargaining and the notion of market/general equilibrium

Apparently, the logical outcome of the discussion in the last section is to proceed by dropping the separation between convergence and execution and, as a starting point, model exchange as involving direct bargaining and barter, both in a decentralized setting. According to the suggestions of Veendorp [1970a, 22] and Howitt [1973, 497], trade would take place before the Walrasian convergence is attained; i.e., bargaining and execution would be formalized under informational decentralization at each instant of barter. And a question could then be raised whether traders, by means of bargaining and possibly relying on trading agents, could approach and sustain equilibrium prices in exchange. Howitt's [1973, 494] conclusion is that in the Walrasian barter model "...the

⁹⁶Veendorp's hinted proposal to reconstruct barter exchange is: "In the present context the relevant class of adjustment processes would seem to consist of these mechanisms that allow trading to take place before equilibrium is reached, that explicitly take into account transaction cost, and that restrict trades to those taking place at organized markets or commodity exchanges." [Veendorp, 1970a, 22]

bargaining process cannot be decentralized." The decentralization of bargaining as concomitant with decentralized execution of barter trading seems thus to be a first step - and a primary challenge - in order to formalize adjustment processes in decentralized exchange.

To put matters in perspective, a short detour may be helpful. The question is that the understanding of execution runs up against the ingrained notion of equilibrium in general equilibrium analysis. Apprehensions as to this have been expounded under various moods, fatalistic, somewhat dismissive or tentatively constructive.

If the general equilibrium model is to be explored under the logical implication of the behavioral assumptions of methodological individualism, a quite common view is that "...the economist has no choice but to pursue the relevant formalizations and inquire into the existence, uniqueness and stability of equilibrium in the model", as Katzner stated it, adding:

...as to the full general-equilibrium model ... satisfactory answers are available only in the case of existence. The problem is that, although sufficient conditions for uniqueness and stability are known, these conditions, contrary to the tenets of methodological individualism, are expressed as restrictions on aggregated, that is market, excess demand functions. Furthermore, it is not clear if it will ever be possible to give uniqueness and stability conditions that are stated with respect to the preferences or behavior of the individual agents. Therefore, if methodological individualism is to be maintained, even more resources and energies will have to be diverted to the mathematical analysis of general-equilibrium models [Katzner, 1991, 19-20].

In the same disembodied vein, and missing the crucial implication of logistics, Hahn raises the fundamental problem as regarding the notion of equilibrium:

There is now also a somewhat subtler point to consider: the behaviour postulated for the auctioneer will implicitly define what we are to mean by an equilibrium: that state of affairs when the rules tell the auctioneer to leave prices where they are. But the auctioneer's pricing rules are not derived from any consideration of

the rational actions of agents on which the theory is supposed to rest. Thus the equilibrium notion becomes arbitrary and unfounded. If, on the other hand, we had a theory of price formation based on the rational calculations of rational agents then the equilibrium notion would be a natural corollary of such a theory.⁹⁷

Hahn then adds:

This line of reasoning leads one to a central objection to the auctioneer and indeed the tâtonnement: it sidesteps the important question of the co-ordinating power of the price mechanism. [...] One might just about convince oneself that notwithstanding all these objections, the tâtonnement and its auctioneer are worthwhile, if it were the case that it provided one story which showed how equilibrium was brought about. Unfortunately however, it does not do this for there are only a few special cases for which the auctioneer process leads the economy to an equilibrium. In many others it will not do so. Indeed, in so far as one holds the view that an equilibrium is the normal state of an economy one should not be tempted to understand this circumstance by means of a tâtonnement. (Hahn [1987, 137-8]; see also Hahn [1970, 3] and [1973a, 7-11]).

As seen above, however, a disturbing result is that: "...in the aggregate, the hypothesis of rational behaviour has in general no implications; that is, for any set of aggregate excess demand functions, there is a choice of preference maps and of initial endowments, one for each individual in the economy, whose maximization implies the given excess demand functions" (Arrow [1987, 70], referring to the Sonnenschein-Mantel-Debreu result). Additional, usually strong assumptions are required for convergence, like for instance that all individuals have the same preferences (utility function) but this conflicts with the desirable premise of methodological individualism: "In particular, the homogeneity assumption seems to me to be especially dangerous. It denies the fundamental assumption of the economy, that it is built from trading arising

⁹⁷The failure to provide behavioral microfoundations to the adjustment of price (or quantity) was formerly questioned by Koopmans [1957, 179] and Arrow [1959], and this led to various models of price adjustment based on maximizing behavior (cf. Hahn [1982, 788-91]), like for instance, Phelps and Winter [1970] in a competitive market, and Barro [1972] for monopoly. These constructions are flimsy for they lack a clear underpinning in market arrangements. Their logistics not being clearly defined, price adjustment mechanisms are liable to unfeasibility in a decentralized way (see Chapter V).

from individual differences" [Arrow, 1987, 71].⁹⁸ But this is not very important anyhow, as the assumption of rational behavior is concerned. A shared belief is that "[i]ndeed, in many cases, provided that the factual assumptions are retained, the conclusions reached within the utility-maximization framework could be reached as readily from much weaker assumptions of "reasonableness" in behavior" (Simon [1986, S212], citing Becker [1962]; see also Arrow [1987, esp. 69-70]).

Hahn's argument above is inconclusive: equilibrium as asserted by tâtonnement is of no use as a guide to understand "the normal state of an economy," but he gives no suggestion to replace it. (In a broader perspective, see Hahn's [1981, 136-7] shedding some light on "the correct path" toward "new equilibrium notions," e.g., "non-Walrasian equilibrium concepts". More recently, Hahn [1989b, 106] has attempted to formalize "...the equilibrium of an economy as an economic state such that no agent has an incentive to deviate from the actions he is taking or from his policy of actions"; this notion of equilibrium would be dependent on the history of information communication and learning interaction among individuals, and would dispense with market clearing.)

More constructively, Howitt [1973] emphasizes the role of the bargaining as intrinsic to the exchange process. In his criticism of the dichotomization of exchange and

⁹⁸Though confined to the exercise of convergence to the equilibrium price set, and despite the vagueness of the behavioral basis for the "groups," Kirman's reflections are of interest:

"It is not mere chance that one assumption that leads to strong results as to uniqueness and stability is that society should behave as an individual. Yet we know that to obtain such behaviour individuals' behaviour must be very similar. If we are to progress further we may well be forced to theorise in terms of groups who have collectively coherent behaviour. Thus demand and expenditure functions if they are to be set against reality must be defined at some reasonably high level of aggregation. The idea that we should start at the level of the isolated individual is one which we may well have to abandon. There is no more misleading description of modern economics than the so-called microfoundations of macroeconomics which in fact describe the behaviour of the consumption and production sector by the behaviour of one individual or firm. If we aggregate over several individuals, such a model is unjustified. On the other hand if we do not deal with the aggregation problem then we should be honest from the outset and assert simply that *by assumption* we postulate that each sector of the economy behaves as one individual and not claim any spurious microjustification." [Kirman, 1989, 138]

bargaining,⁹⁹ he touches a question of interest, that of giving non-convergence a tractable meaning:

One qualification is in order here. It might be argued that however the bargaining process is defined it must come to an end before exchange occurs, because whenever two people are observed to engage in an exchange we have no choice but to assume that they agreed to exchange exactly the way they did. Thus their bargaining process must by definition have converged on the agreed exchange. In order for the non-convergence of bargaining to make sense we must have in mind *a more restrictive definition of equilibrium*. What is crucial is that in a market equilibrium the trades being engaged in by any one individual are the best that he could see himself as being able to engage in even if he were able instantaneously to bargain with everyone else in the economy. [Howitt, 1973, 497, italics added]

'Equilibrium' becomes the outcome of the activity of bargaining and exchange by individuals facing 'perceived' opportunities. Even if we postulate that the trader knows prices of the sequence of transactions to come (how?), we cannot presume he knows the transactions he will consummate. Notional equilibrium can hardly have an implication, here. But this problem has been mostly circumvented (as in models of convergence where there is no "auctioneer," e.g. Fisher [1983]).

Because it is not within the reach of the individual trader under decentralized information to know in advance the chain of meetings, the ordering of the exchanges, and the actual exchanges to be entered at,¹⁰⁰ feasibility is an unknown to the individual trader to start with. A possible "idea" would be that the outcome of bargaining would be Walrasian "...if agents are allowed to trade arbitrarily many times and may not be

⁹⁹Howitt criticizes the formalization of bargaining in monetary models depicting a sequence of temporary equilibria (like Grandmond's): "Such an equilibrium analysis would dichotomize the process of exchange and the process of bargaining. [...] Only after the bargaining process had reached completion would exchange take place." [Howitt, 1973, 496]

¹⁰⁰In fact, it is not up to the individual trader to do this; in Ostroy and Starr this is parametric; in search models it is random.

prevented from realizing trades that are beneficial to others" (McLennan and Sonnenschein [1991,1396]; cf. Gale [1986a,787-8]); but then what is the progress relative to Ostroy and Starr's case of non-decentralized execution?¹⁰¹

McLennan and Sonnenschein really take the problem seriously, if only "...at an intuitive level" [1398]. Facing the question whether allocations induced by steady state equilibria (as in Gale [1986a], also with sequences of "entering and leaving" flows of individuals) are Walrasian, the authors recognize the need to have an "initial" economy to compare,¹⁰² and they proceed with artful reasoning:

In the theory of general economic equilibrium prices are not displayed as variables chosen by individuals, and the relevance of the theory therefore depends on the belief that economic equilibrium correctly summarizes the noncooperative equilibria of an underlying game in which all endogenous variables are direct consequences of the choices of individuals. However, there are few principles to guide the modelling of the underlying game, and in fact our belief in the relevance of economic equilibrium rests on an intuition that this concept should characterize equilibrium outcomes for a large class of games. [McLennan and Sonnenschein, 1991, 1398].

Borrowing sundry intuitive support,¹⁰³ their "initial economy" is asserted as characterizing "...Walrasian outcomes by means of axioms that are, at an intuitive level,

¹⁰¹This is incompletely and distortedly acknowledged in Gale [1986b, 808] who doesn't refer to the possibility of repeated (parametric) rounds in Ostroy and Starr [1974], only to imitate the procedure in his model; in Gale [1986b], meetings are random but he posits a sequence of dates where "[e]ach date here represents a complete round of the bargaining game" [1986b, 808]. This wouldn't be expected to comply with the decentralized information, but there is no basic difference between both in this regard. (Moreover, as in Ostroy and Starr, Gale introduces a 0th commodity to "balance the budget" [810], whatever that means.)

¹⁰²In *Sequential Bargaining as a Noncooperative Foundation for Walrasian Equilibrium*, McLennan and Sonnenschein [1991, 1420] assert that: "In order to even be able to talk whether an equilibrium is Walrasian it is necessary to have initial and final economies to compare." What is an initial economy? The authors, as a starting point, just subsume it: "Fix a Walrasian equilibrium of this economy" [1395], which is their Theorem A [1397].

¹⁰³From Aumann's [1964] core equivalence theorem, and from the fact "...that the equilibrium outcomes of fully elaborated extensive form games are Walrasian" [McLennan and Sonnenschein, 1991, 1398] - but see Rubinstein and Wolinski [1985; 1990] for a contrary contention.

consequences of individual rationality in a world in which agents are not prevented from trading with each other repeatedly" [1398].¹⁰⁴ In fact traders don't trade, here. Elsewhere in the article, after pointing out the problem that Gale's [1986a, 794] "introduction of individuals" originates in the formulation of the pairing process - the existence of a continuum of i.i.d. random variables - the authors state, for the case of their continuum economy:

In our approach "Walrasian" is a relation between initial and final measures on the space of consumer characteristics, and ... it is possible to discuss pairing probabilities and the evolution of the distribution of characteristics in the market without reference to any underlying pairing of individuals [...] One might object that we allow pairing probabilities that cannot be justified by any pairing process. This is true in a narrow technical sense, but we believe that limit theorems for finite economies are the correct response. [McLennan and Sonnenschein, 1991, 1403]

¹⁰⁴Differently, Rubinstein and Wolinski [1985], from where this literature was suggested, consider discounting directly as a result of assuming that a delay in agreement in a current negotiation may prevent a trader from meeting comparable bargaining opportunities with other partners, and also the consequence of this, the risk that his partner abandons negotiation, which reflects a competitive pressure. But this time preference didn't prove to be the determining assumption in order for the conclusion that that frictionless bargaining and exchange results in a non-competitive allocation.

The reasons are then to be found elsewhere, namely in assumptions on the numbers of traders, the divisibility of the good, the possibility of repeated bargaining, and whether the numbers of buyers and sellers in the repeated bargaining game is stationary. Gale increased the number of types of traders from two to "many", and McLennan and Sonnenschein to a "continuum economy". Moreover, while in Rubinstein and Wolinski [1985] 'one' indivisible good is only traded once ("[a]fter two agents reach an agreement they leave the market" [1985, 1135]), Gale considers divisible goods and multiple trading (he lets "...them trade as often and with as many partners as they like" [1986a, 787-8]), which is taken up by McLennan and Sonnenschein (cf. Gale [1986a, 802-3]). Finally, contrary to the later two models, Rubinstein and Wolinski [1985] assumes stationary numbers, which according to Binmore and Herrero [1988] is the crucial feature (cf. Gale [1986a, 803] and Wilson [1987, 53-4]). In a stationary equilibrium with a constant number of buyers and sellers, if numbers don't match (cf. Rubinstein and Wolinski [1985]), the surplus would be divided proportionally to their numbers; but if numbers are not stationary, the short side of the market is shown to appropriate all the surplus and the market clears, i.e., "...the classical Walrasian result is obtained" (cf. Binmore and Herrero [1988, esp.17]).

However, the characterization of equilibria at each date in terms of stocks is not adequate to these models. With an indivisible good the market doesn't clear by definition, but this is irrelevant; yet, in any case, if the market is stationary the flows of buyers and sellers into the market must be equal and thus any price can be a flow equilibrium (unless stricter assumptions are postulated; see Gale [1987]).

As an aside, notice that in Rubinstein and Wolinski [1985] (based on, and generalizing, the two players bargaining case in Rubinstein [1982], in a line ascending from Edgeworth [1881]) a *strategic* approach to bargaining was attempted that might help provide a basis to the *axiomatic* literature in this area (cf. Diamond and Maskin [1979], Diamond [1981; 1982b], and Mortensen [1982a;b]).

And when "pairwise transactions" between "individuals" are presumably allowed for [Gale, 1986a, 791], bargaining is modelled under the "as if" assumption that exchange rates are equilibrium (notional or Walrasian) prices; this is in fact so in bargaining models, viz. Gale [1986a; 1986b] where each instant of bargaining in random pairwise meetings of individual traders is marked by the "(rational) expectations" of the outcome of future bargains, in the successive rounds towards convergence to the Walrasian consumption bundle (cf. Arrow [1994, 5]); it is also Arrow's opinion that in these articles "...prices never appear as objective phenomena; they are only subjective, that is, expectations held in the agents' minds." Given the full anticipation that only the Walrasian net trades will be accepted, each trader is willing to continue search and bargaining without any "impatience" cost until the marginal rate of substitution between goods equals their (Walrasian) relative price (cf. Wilson [1987, 54-5]). This artifice erases any distinction between 'target' and 'active' excess demands, and thus no trading can be said, in fact, to be present in the process of bargaining.¹⁰⁵

(ii) In the beginning ... logistics

If we needed to provide a demarcation from the former view, we would argue that this second proposed path derives from the difficulty of understanding "rational behavior" when the actions of an individual are dependent upon the actions of others. As Hurwicz [1945, 506] put it, though in a different context:

¹⁰⁵The main result of the model is that for every market equilibrium, a Walrasian allocation exists such that an agent completes in finite time his preferred bundle and leaves the market (cf. Binmore, Osborne and Rubinstein [1992, 209]).

There is no adequate solution of the problem of defining "rational economic behavior" on the part of an individual when the very rationality of his actions depends on the probable behavior of other individuals [...] [T]he individual's "rational behavior" is determined *if* the pattern of behavior of "others" can be assumed *a priori* known. But the behavior of "others" cannot be known *a priori* if "others," too, are to behave rationally! Thus a logical *impasse* is reached. [Hurwicz, 1945, 506].

Or, according to Hahn:

There is also a canker at the heart of the theory. This arises from the logical necessity that a theory based on rational self-seeking actions ensures that its equilibrium notion is indeed that of a state in which no agent can improve himself by any action. But all General Equilibrium Theory has done is ensure this *provided market prices are independent of these actions*. [Hahn, 1981, 130]

If we understand behavior here to refer not to maximization of utility given prices, but to (the solution to the problem of) exchange patterns¹⁰⁶ - patterns of bargaining and trading of whatever kind we might consider in a decentralized setting - then behavior is not independent of the market arrangement that we choose to postulate and the trading activities therein.¹⁰⁷ This is the question of feasibility of individual behavior to which logistical feasibility can be seen as an "external" constraint that matters: "Any choice can be exhibited as a maximization against constraints; what I have just been saying is that the constraints may be internal to the chooser, as well as external to him" [Hicks, 1983, 371]. Of course, we are not entering the much harder

¹⁰⁶When referring to maximizing behavior, I do not mean to meddle with the question of optimizing versus satisfying behavior, as in H. Simon. I only want to notice the limitations of maximization when its results are plans, which feasibility is ignored.

¹⁰⁷Hahn raises doubts on preferences as given: "...I would suggest that it is not obvious that one is justified in treating preferences as given and quite unjustified in treating conjectures as given. Certainly almost any feasible allocation can be a Walrasian equilibrium for some preferences and certainly we do not believe that we emerge from the womb with formed preferences or that the latter are independent of economic experiences. We treat preferences as exogenous for the very good reason that we have no good manageable theory of an economy in which they are treated as endogenous. In any case I would not be alarmed if conjectures, at least in the short period, are taken as formed by history." [Hahn, 1978, 2-3]

subject of the emergence (or even less the less pressing aim at "optimality") of institutional arrangements for trade; traders are just assumed to be provided some sort of exchange mechanism, the rules of which they are supposed to obey.¹⁰⁸

But this argument may be irrelevant. We have tried to show, first, how inconsequential existence proofs are if we are to think of agents as transacting in a decentralized setting, and, second, that convergence in the general equilibrium approach fails for lack of computability. Therefore, a possibly rewarding approach would be to start with logistics. There are hints where from to bring threads together. One is those models that don't dichotomize, like Feldman [1973] and Madden [1975] (although only paying cursory attention to logistics, relying on individual optimization as the foundation, and primarily addressing the question of optimality in allocation). The other is Ostroy and Starr on trading rules. Still another is Edgeworth on contract.

¹⁰⁸To notice that no claim is implied that the rules of the transaction game correspond in any sense to real-world features. This requires understanding of how such rules are "constructed" which involves "a partly social process" [Arrow, 1994, 5]. The concern here is only with the implication of interaction on individual behavior, and this is where Arrow's subsequent comment is relevant: "More generally, individual behavior is always mediated by social relations. These are as much a part of the description of reality as is individual behavior."

CHAPTER V

CONCLUSION: THE THEORY OF PRICE ADJUSTMENT

By way of conclusion, this chapter focuses on Arrow's [1959] important contribution to the theory of price adjustment¹ in which the decentralization of the marketor function (cf. Clower [1994b, 3n]) is attempted, that is, price and quantity decisions are constructed as a result of maximizing behavior of traders.

Price adjustment to the equilibrium level is common to pure competition and monopoly, both need the function to be performed by some entity. In pure competition such 'entity' is usually referred to as 'the price mechanism,' i.e., the function is attributed to the play of market forces, supply and demand. In monopoly it is assigned to the monopolist. But the problem this 'entity' faces is the same; since the marketor "...cannot be expected to know with certainty the exact shape and location of the supply and demand curves, it is necessary further to suppose that demand and supply conditions are *estimated* and that these estimates are used as a basis for setting current price" [Clower, 1955, 219-20].

¹Beyond Arrow's, the most influential contributions to the theory of price adjustment are Phelps and Winter [1970] and Barro [1972]. Other papers and theories should also require consideration and analysis, like for instance, Thore and Billström [1954], Thore, Billström and Johansson [1954], Gordon and Hynes [1970], Fisher [1970; 1972; 1973; 1983], Diamond [1971], Rothschild [1974], Hey [1974], Irvine [1981], Gottfries [1986; 1991], Bils [1989], Mirman, Samuelson, and Urbano [1989], Balvers and Cosimano [1990]. Comments on parts of this literature can be found in Hahn [1982, 788-91] and Rothschild [1973].

A first question regards the standard adjustment of price in pure competition as conducted by the marketor.² If the marketor fails to choose the equilibrium sales-sales price combination, the market will be observed in disequilibrium by the marketor, and this leads to a new estimate of the sales curve. Further revisions of the sales curve can be thought as eventually leading to price adjustments such that "...current net (estimated) sales and current net demand are equal." "[H]ence, market equilibrium price is defined by *two* conditions: that *estimated* net sales be zero, and that *realized* net sales be zero also" [Clower, 1955, 222]. Uncertainty is present, as it is traditionally considered to exist in traditional price theory.

A different question is suggested by Arrow [1959], that of the uncertainty faced not by the central marketor but by the individual seller. His point is that when the individual supplier ascertains that his estimated sales - i.e., his optimal supply, given the prior market price - and realized sales do not match, he will come to the realization that his estimated individual demand curve is not horizontal (i.e., parametrical) and so he has to revise it in order to decide his new quantity to supply next (period). And the problem ensues as above explained, but for the fact that instead of one single marketor in the market we have now a number of them, each one solving his particular adjustment problem by himself, without the help of a central marketor.

According to Arrow, in disequilibrium the individual seller becomes a monopolist,

²Haavelmo [1958, 33] defends that "...traditional static demand-supply cross does not represent a complete model of actual behavior in a market. Consequently, we can give up the idea of achieving a sensible market theory just by arming the demanders and suppliers with, respectively, a demand and a supply curve - and then letting them loose on each other. If we nonetheless want to stick to the two curves as a practically feasible description of the behavior of demanders and suppliers, we will evidently need to introduce a third party into the game, some sort of *deus ex machina*. An example of such a third party, worth considering, would be an inventory-holding sector with, e.g., the rate of change of prices as its action parameter. Demanders and suppliers could then retain their classical roles as quantity adjusters with the inventory as a buffer between them."

in the quite general sense that his estimate of the sales curve is downward sloping. Moreover, since the seller is a profit maximizer, he realizes the possible gains from facing a sloping sales curve - which are (not possibly but certainly) attainable given that no costs are attached to the solution of uncertainty. This leads him to adjust price. Given uncertainty, this should require successive revisions of the sales curve. Uncertainty surfaces in competitive pricing.³ However, this is nothing special to pure competitors in disequilibrium, it is a feature of non-standard monopoly theory too (cf. Clower [1955]), where the sales curve is not forcibly presumed to coincide with the real demand curve.

Arrow's article *Toward a Theory of Price Adjustment* opens this way:

In this essay, it is argued that there exists a logical gap in the usual formulation of the theory of the perfectly competitive economy, namely, that there is no place for a rational decision with respect to prices as there is with respect to quantities. A suggestion is made for filling this gap. [Arrow, 1959, 41]

Then as now the standard 'textbook' economics suffers from the same drawback: the firms' problem is largely to choose output, and price setting or price adjustment to equilibrium positions are only dealt with in a complementary fashion. Price adjustment is introduced into the picture as a disequilibrium phenomenon; stability or convergence are at issue in order to provide a foundation for equilibrium states.

According to Arrow, for a monopolist - as well as for the perfect competitor turned into a monopolist in conditions of market disequilibrium - that faces uncertainty

³This seemingly untractable problem was simplified in Arrow and Hahn [1971]. The question of information (on the demand side) was shunned by positing the simplifying assumption of an auctioneer "...that establishes unique and public terms on which goods may be traded". And ingenuously it is added: "...and he adjusts these in the light of market observations by some particular rule" [Arrow and Hahn, 1971, 424].

Indeed, "[t]he fiction of an auctioneer is quite serious, since without it we would have the paradoxical problem that a perfect competitor changes prices that he is supposed to take as given." [322]

we have to admit the possibility of a discrepancy between output and demand. This "...informs the monopolist of the extent to which he is in error and yields knowledge to estimate his demand curve; on the other hand, the discrepancy alters his stock of inventories, which may in turn affect his cost situation in the next period" [Arrow, 1959, 45].⁴ Price adjustment happens in response.

Arrow's construction seems at first sight to be quite general; he envisages different markets (goods market as well as labor market), and doesn't ignore market structures: "...the dynamics of prices may be affected by the structure of the market even in cases where there are sufficient numbers in the market to insure reasonably competitive behavior at equilibrium" [Arrow, 1959, 47]. In fact, however, the firms considered by Arrow are presumed to exist in a world of brokered markets.

...suppose we have a situation which conforms in all the aspects of homogeneity of output and multiplicity of firms to the usual concept of perfect competition, but in which the aggregate supply forthcoming at the "market" price exceeds the demand at that price. Then the individual firm cannot sell all it wishes at the market price. [...] Under conditions of disequilibrium, there is no reason to expect that there should be a single market price, and we may very well expect that each firm will charge a different price. [Arrow, 1959, 46]

And Arrow adds next:

Let us consider in somewhat more detail the case in which demand exceeds supply. Assume that no firm can increase supply in a very short period. Then any individual entrepreneur knows that he can raise the price even if his competitors do not raise theirs, because they cannot satisfy any more of the demand than they do already. The entrepreneur is faced with a sloping demand curve and raises his price in accordance with the profit-maximizing tactics of a monopolist.

⁴It is quite true that the new unexpected sales-price points will yield knowledge about the possibility of a shift in demand conditions, but this imparts no sure information about the magnitude of the "error". The estimation of the demand curve is a different affair altogether; even under the *ceteris paribus* assumption the learning process may be quite irregular or long-drawn-out [Clower, 1959].

Despite all the reasonable steps of his thought experiment, one can't avoid raising the possibility of contradictions in his story. The firms face a "market" price; then, for some reason the aggregate supply forthcoming at the "market" price exceeds the demand at that price. Next, each firm adjusts his price along a sloping demand curve as a monopolist would do.⁵ Questions: How do firms first notice the discrepancy between supply and demand? Is disequilibrium perceived in the aggregate or as a localized phenomenon?

First, if it is a localized fact one can assume that only some firms in the market observe the discrepancy between the quantity they choose to offer to the market given the ruling market price and the quantity the market is willing to take. Assuming that the firms are able to read this discrepancy as a disequilibrium, as a consequence only those that recognize it adjust their prices, and to the degree it affects each firm - this "special case" is hinted at by Arrow for a market "...where products are poorly standardized" [48] but this is just an aside, not a necessary fact.

This localized perception of disequilibrium requires that on the demand side information is not perfect (costless and/or instantaneous diffusion of prices set by each firm to the buyers). Certain firms will perceive the discrepancy and others not, and price adjustment will differ among firms, only because buyers take time to notice or incur costs to get the information otherwise⁶ - and this is responsible for the difficulty firms face in inferring their sales/demand curve. Even though he allows for "...a considerable dispersion of prices among different sellers of the same commodity" [46-7], Arrow

⁵Meanwhile he criticizes the common view that there is one price in a competitive market and asserts that the law of one price only is valid under special conditions, which are not those in disequilibrium.

⁶We might guess that his problem wouldn't be present (or so pressing) if Arrow hadn't assumed output 'stickiness' in the "very short run" (cf. Arrow [1959, 46]).

seems to fail to grasp either the necessary informational background on the demand side (information costs on current prices in the market by buyers), or its consequence upon the inference problem faced by firms during the adjustment process.⁷ Both sides of the market would have to show some sort of friction for this situation of localized perception of disequilibrium to eventuate. My contention is that Arrow is not thinking of such a market.

Second, and alternatively, we can imagine that disequilibrium is generally observed. We could think of it as being observed by all firms in "the aggregate", so that each individual firm has information about the existence and degree of the market discrepancy. The question could be raised of who centralizes, processes and conveys this information back to the system, to the firms. For the information to be conveyed to suppliers some agent would be needed to collect it, be it an auctioneer or a set of brokers trading in an organized market.

We could also conceive of disequilibrium being generally observed, not because this information is produced somewhere in the system and brought back to the firms, but because every firm tends to be equally (or proportionately) affected by the disequilibrium between supply and demand. Each firm notices the discrepancy between the quantity it chooses to supply and what the market is willing to take, and reads it as the reflex of an

⁷Arrow, coherently with the originally assumed market perfection conditions, doesn't envision this question at all. First, the competitive firm in disequilibrium is faced with a sloping demand curve due to the supply rigidity in the very short-run: "...any individual entrepreneur knows that he can raise the price, even if his competitors do not raise theirs, because they cannot satisfy any more of the demand than they already do" [1959, 46]. And, second, granting the large uncertainty during the adjustment process, he adds that "[a]ny estimate of the demand curve to a single entrepreneur involves a guess as to both the supply conditions and the prices of other sellers, as well as some idea of the demand curve to the industry as a whole. Under competitive conditions none of these is likely to be known very well". To hint at knowledge of the industry demand curve is absurd (as Arrow [1987, 71] himself recognizes for the situations of monopoly or imperfect competition where "...scientific analysis imputes scientific behaviour to its subjects"), but anyway off the point. The question is that Arrow fails to recognize the implication of the informational problems faced by buyers in disequilibrium, supposedly with price dispersion.

aggregate disequilibrium in the market. This is an orderly market where all the suppliers perceive a disequilibrium of the same sign (meaning either an excess supply or an excess demand) that, besides, is of approximate degree. In this situation we might expect the price responses among firms not to differ significantly. Consequently, in this case it is hard to agree with Arrow on the stress he puts on the amount of uncertainty during the process of adjustment as well as to agree with his conclusion that the "...adjustment process is apt to be very irregular" [Arrow, 1959, 46].

Arrow's story pretends to be quite general but it has some loose links. None of the alternatives is satisfying. Arrow didn't construct a market structure capable of tackling the questions he tries to answer. His model is not applicable to situations "...in which information would be expected to be relatively scarce" [Arrow, 1959, 48], which our first case of localized perception of disequilibrium might fit. In the other case, in which the uncertainty is mostly resolved (either because central agents exist or because the market is very orderly), price adjustment by an individual firm can hardly be meant as a decision of the firm. During the adjustment process, a price signal is contemporaneously given to the individual trader, announced by brokers or a central agent; or, if disequilibrium is perceived in the aggregate because each firm realizes that the effect tends to be equally distributed among firms, adjustment may be expected to be quite smooth as well as quick - each firm's demand curve would provide sufficient information to infer the equilibrium price position. And price dispersion, if existent, would be of little implication on the price decisions of each firm: it could be assumed to be soon arbitrated out.

To sum up, Arrow doesn't fill the "logical gap" in the usual formulations of the theory of the perfectly competitive economy that there is no place for a price decision

as there is with respect to quantities. My conclusion is that he fails to appropriately raise the decision problem firms face in competitive non-brokered markets. But in these non-brokered markets such a gap cannot be left unfilled: the price is not produced externally to the firm, there is no "going price" out there generated in a market in which the firm operates.

A central problem for economic theorists since Adam Smith has been to provide an intellectually satisfactory explanation of the working of observed trading mechanisms. As of the present time, that problem, though often addressed, has never been answered; to this time, indeed, the problem has more often been sidestepped than confronted directly. This may go far to explain why so many of the crucial questions still at issue not only remain unanswered but (as reflected in the queries raised throughout this dissertation) have yet to be perceived as "relevant" by the bulk of the economics profession, whose thinking continues to be dominated by, and whose vision seems to be filtered through, the thick clouds of confusion produced by the neowalrasian diversion.

APPENDIX

NOTES ON THE LITERATURE

A. THE BUDGET CONSTRAINT

There is in Walras a restriction of 'zero value of (planned) net trade' for the individual trader, but this is quid pro quo (Say's Principle), not income constrained utility maximization (cf. Jaffé, ed. [1954, 165]). The concept of budget constraint is not in Walras; it appears to have been suggested by Pareto [1909], contrary to Stigler [1954, 211], who argued: "When income was introduced into consumer theory by Slutsky and Hicks and Allen, their work was wholly in harmony with the line of development the theory of utility had been taking." Hicks acknowledges primarily Pareto,¹ and Slutsky [1915], and all later users of the budget constraint concept apparently drew on the same source.

Walras developed his argument by explicitly introducing maximum utility in his equations of exchange but he presupposed consumer equilibrium (utility maximization) when dealing with the theory of exchange;² he didn't formalize the equilibrium of the individual, as Pareto later did. The budget equation in Hicks [1939/1946, 305]) bears a close resemblance to Pareto's "budget of the individual" ([1909/1927, 160], [1911, 90]) and we might conjecture that constrained utility maximization entered standard price theory by way of Pareto. In *Mathematical Economics* [1911, 65; see fn], Pareto clearly

¹"Our present task [in this book] may therefore be expressed in historical terms as follows. We have to reconsider the value theory of Pareto [and Walras] and then to apply this improved value theory to those dynamic problems of capital." It is Hicks' opinion that "Walras ... confined himself, in the main, to setting out the problem" in mathematical terms. "It was Pareto (*Manuel d'économie politique*, 1909) who began to take things farther," i.e., "Pareto's improvements in value theory." [Hicks, 1939/1946, 2-3]

²"If we suppose maximum satisfaction to have been attained..." [Jaffé, ed., 1954, 165].

states that equilibrium results from the contrast of tastes and "constraints"³ (in earlier writings, as in the *Manual*, Pareto refers to "obstacles"; cf. Allen [1932, 210, 37n]). In fact this is how the problem of the individual is posed in Chs. IV ("Tastes") and V ("Obstacles" on production), and especially how economic equilibrium is defined in Ch. VI of the *Manual*.

In Hicks [1946, 305], dealing with the equilibrium of the consumer, we have: "...provided [the individual] spends all his income, we must have $M = \sum_{r=1}^n p_r x_r$ " (cf. Schultz [1935, 434-6] for a detailed presentation; also Allen [1932, 212-3]). In Pareto the matter is presented in two contexts, and in slight different ways, on maximization of utility by the individual (p.160), and in the mathematical Appendix when dealing with exchange (p.412). First, when the budget of the individual is first introduced (p.160), it is not defined as a condition as Hicks does ("...provided he spends all his income" [305]), rather it is stated as an equality required by exchange: "If there are more than two goods it is easy to see that the receipts must still be equal to the expenditure, because if this were not so, it would mean that the individual had received, or spent, some money in another way than the transformation of goods." [Pareto, 1909/1927, 160]. (To notice Pareto's insistence on his view that "economic equilibrium is independent of the notions of ... utility, of value in exchange, or of ophelimity" and "...price" [393-4, see fn.4; also 406], as well as his emphasis on "...quantities which observation gives" [411-2; also 391n, 394].)

Dealing with exchange in the mathematical Appendix, when the budget plane of the individual is defined (p.412) there is no reference to "income" (cf. Schultz [1935,

³Also, "[i]f there are as many equations of constraint as there are variables, everything in the system is determined." [Pareto, 1911, 65]

437]), yet Pareto states that the total value of an individual's holdings of commodities after exchange "must also" be equal to the total value of initial holdings measured at exchange prices. From this equality of total values before and after exchange, Pareto derives the budget plane of the individual, relating net demands valued in numéraire units (i.e., d_x, d_y, \dots valued in units of x) [412]: "This equation has a special significance in political economy. It gives the budget plane of the receipts and expenditures of the individual under consideration. Whether the prices are constants or variables, the balance plane of the individual, for the exchanges [pour les échanges] d_x, d_y, \dots , is always given by

$$d_x + p_y d_y + p_z d_z + \dots = 0."$$

The conditional character of the Hicksian budget equation is clearly anticipated.

Using Pareto's notation, the parallel to Hicks' budget equation could be so put:

$$x_0 + p_y y_0 + p_z z_0 + \dots = x + p_y y + p_z z + \dots$$

The left hand side is just the numéraire value of the resources of the consumer ("an individual, who has a given sum of money M available for expenditure" [Hicks, 1939/1946, 305]); and the right is the value of expenditures. The assumption is that value supplied (via the "auctioneer") is equal to value demanded: $V^s = V^d$. This is a planning constraint on the individual, which is the same as Say's Principle, that one can plan to acquire only by offering.

B. HICKS ON TRADING AT FALSE PRICES

Trading at "false prices" is considered in Hicks' *Value and Capital* [1939/1946, esp. Note to Ch. IX]. Following Marshall's description of temporary partial equilibrium (two goods/fish market), Hicks considers that "...the process of fixing prices by trial and error ... need not have any appreciable effect upon the prices ultimately fixed" [127].

Since traders cannot be expected to know just what the schedules of total supplies and demands will be, transaction prices during the course of trading will move up or down. Disposing of recontracting as an exceptional feature in markets, if trading at 'false prices' is considered, a problem ensues in regard to demand and supply analysis. Hicks discusses this problem, showing that that change in price in the middle of trading has the same effect as a redistribution of wealth (income effects); "but if [the buyer's] total expenditure on the commodity is small, the gain (or loss) must be small, and his demand for the commodity will be very little affected. Consequently the market will finish up very close to the equilibrium price" [128-9].

In the case of general interdependence, Hicks says that income effects create what he calls "a certain degree of indeterminateness," and that as a result of false trading "this indeterminateness is somewhat intensified". And he adds (p.129):

But I think we may reasonably suppose that the transactions which take place at 'very false' prices are limited in volume. If any intelligence is shown in price-fixing, they will be.

Hicks adduces that gains to the buyers may be expected to be offset by losses to

the sellers, and vice versa. Moreover, it is (oddly) added that the effect of false prices is limited to income effects by his assumption of markets being only open on "Mondays"; equilibrium prices are therefore used as indicators for production and consumption plans carried out for the rest of Hicks' "week."

Here some comments are in order. First, one must bear in mind Hicks' adherence to the assumption of perfect competition, including not only (i) agents' "assessment of particular supply or demand conditions" [6-7] and (ii) "perfect contemporaneous knowledge - that everyone knows the current prices in all those markets which concern him" [123], but also (iii) "an easy passage to temporary equilibrium": "...we need also to try to bring ourselves to suppose that price-changes are negligible during market hours on the Monday, when the market is open and dealers have to fix market price by higgling and bargaining, trial and error" [123]. Now, two comments:

First, why does Hicks bring in the misplaced fact of "price-fixing"? The issue clearly lies outside the confines of his theoretical model. If he is conjoining "perfection" with a radically different real world to support that trading at false prices is limited in volume, that is bad economics. Whether or not his Note to Ch. VIII [110-1] on "Conventional or Rigid Prices" could be interpreted in this context (as applying to any price-fixing, by the government or by firms alike) as § 6 on "Price Rigidities" in Ch. XXI [265] may lead one to guess, this is an instance of real world facts unrelated to his theoretical thread when dealing with temporary equilibrium, and would caution us against his possible mixed argument of theory and realistic description.

Hicks coins the expression *fixprice* market for his "habit" [1988, 9] of looking upon diversified manufactures as a force which makes for stabilization (in contradistinction to speculative markets); he assumes a *fixprice* market as one in which

prices are to some degree insulated from the pressures of supply and demand. In effect, Hicks analyzes income adjustments under the *fixprice* assumption in *Capital and Growth* [1965, Ch.7, 76ff], where it obtains a theoretical dimension, as he stresses in *The Crisis in Keynesian Economics* [1974, 22-30].

Of course, Hicks might have intended to refer to price fixing in the sense of his weekly model. In that model, each price, once contracted, is fixed during the week it is contracted for, and trade takes place at prices defined on the past "Monday." A trade contracted for and due during a later week can be 'recontracted' by means of revision of prices only next "Monday" comes (in case price expectations or trading plans are inconsistent (pp.133-4)).

But his assumption that contracting takes place on "Monday" is just a convenient way to separate contracting from trading, and to give his model a flavor of "dynamics" (contracting occurs by means of a sequence of temporary equilibria). The fact that plans carried out by consumers and firms during the "week" are based on equilibrium prices obtained on "Monday" only has relevance because Hicks is working on the presupposition of "perfect" markets. If he didn't allow for an easy adjustment to equilibrium, how could information on "equilibrium" market prices be so taken by traders? Hicks doesn't seem right when he states that the effect of false prices is limited to income effects by his assumption of markets being open on "Mondays," i.e., the separation between contracting and execution of plans. The reason seems to lie, differently, in the assumption of an easy passage to equilibrium.

Wherever Hicks' Note fits, as a real world interference, as it stands, it is an object lesson of bad economic theory. One wonders what the Hicksian model of the economy really is, it certainly isn't the one discussed in his mathematical appendix. The

problem is that the entire argument runs in terms of an implicit conception of real world that Hicks does not share with his readers, so the entire argument has an otherworldly aspect.

C. PRICE-MAKING MECHANISMS

Ralph Cassady ([1967, 8-14]; [1974, xix and 3]) distinguishes three basic price-making schemes:

(i) Take-it-or-leave-it administered pricing, in which the price-maker (usually the seller) posts a price at which he is ready to transact, the other party being supposed either to accept or reject the offer without negotiation.

(ii) Private treaty pricing through individual negotiation, in which a selling price is negotiated between individual seller and buyer for each transaction. The starting point of bargaining can be a "specified" or list price that both parties know is open to negotiation, which will take place if the buyer is willing to treat that price as a take-it-or-leave-it proposition; or, when no price is "specified", a quotation is made by one of the parties, usually an asking price enunciated by the seller, expectedly at a level that, attending though to current market conditions, leaves him with room for negotiation, without risking alienating the buyer. If a counteroffer is quoted by the buyer, bargaining between the seller and the individual buyer may then ensue, by means of which adjustments (downward adjustments of asking-price, and/or upward adjustments of offer-price) are discussed,⁴ until they possibly arrive at an agreement on the transaction price.⁵

⁴Which will be mostly dependent on market conditions, knowledge of these by the two parties, and their tactical skills. This is all very much loose and informal. As to Fudenberg and Tirole [1983, 239], the form and outcome of the bargaining "game" may be very sensitive to the institutional 'setting' (e.g. number of bargaining periods) and other parameters (e.g. valuations, (a)symmetry of information, discount factors); notice also the authors' conclusion that "...general assertions about the effects of parameter changes on the bargaining process are suspect."

(iii) Competitive bid pricing, in two varieties: (a) Sealed-bid arrangements either by vendors who compete by underbidding (e.g. for a job), or by buyers who compete by getting to outbid other prospective bidders (e.g. for a given right or property).⁶ And (b) second, auctioning which is a price-making method whereby competing buyers are led to outbid each other so that the vendor may be able to obtain a price tending to approach the highest demand price of bidders. The auction house usually operates as a broker-agent representing the vendor.⁷ The role of the auctioneer in the ascending-bid auction is "...to recognize one bidder at each level, and to announce the amount of the bid, in

⁶In a market so organized that pricing is conducted by private negotiation between seller and buyer, both seller competition in gaining or retaining custom and buyer competition in "acquiring supplies" are present; but also each trader when dealing with a potential transactor will be attempting to obtain "the most favorable terms" without compromising profitable dealings in the future, if he deems this favorable to his business with given buyers (cf. Cassady [1974, 97]). Thus, both "antagonistic" and "cooperative" efforts are themselves felt in the making of negotiated pricing. This is at the root of the fact that, although this price mechanism is best suited to those situations ("product and market conditions" [206]) where the setting of prices is required to conform to the particular circumstances of each transaction, it does require attention by traders to the market circumstances, which establishes a range of reasonableness in price quotations. As to the gathering of market information, sellers may observe market dealings, but their reliable, though indirect, information about the market may only be assessed through their private negotiations; buyers, on the other hand, will benefit from sounding out several sellers on their quotations (not only for informational reasons, but also for the strategic interest of patronizing more than one seller).

⁶The distinctive features of sealed-bidding comparatively with auctions are quite smudged: they are the time interval between reception of bids and assignment of the right, and, more importantly, the period of time that bidders can count on to devise their strategies before they file sealed bids (Cassady [1967, 12-13]).

⁷However, often auction firms operate also as merchants, through acquisition of title to the property before reselling; or as "merchant-middlemen", where beyond the transmission of title, there is also physical acquisition of the property (cf. Cassady [1967, 9-11]).

Hackett [1992], referring to Stern and El-Ansary [1982], distinguishes two main types of intermediaries, dealers and brokers. Merchants or dealers acquire title to the intermediated goods, and obtain compensation by reselling them on their own account for a profit ("residual surplus"). On the other hand, there are brokers, who are agents of the buyer or seller in the intermediation, they do not acquire title to the property of the intermediated goods, and are compensated with a revenue-sharing commission. (Consignment agents are identical to brokers, and are compensated by a commission (Hackett [1993].) Hackett searches for reasons to opt between the two contracts. He builds a model that considers demand variance, as well as the responsiveness of demand to sales efforts by the intermediary; given the compensation forms, the two schemes generate different incentives for the intermediary to exert sales efforts. (See Hackett [1992, 300] for references to the literature on intermediary structures, as especially concerning financial intermediation.)

order to establish a basis for increased bids" [Cassady, 1967, 57]; and in the descending-price auction, "[a]fter selecting the starting point, he calls out the prices at successively lower levels, recognizes the first and high bidder, and announces the amount of the successful bid and the name of the buyer" [1967, 60]. Auctions can be ascending-bid, descending price, or combine both in simultaneous bidding, but the purpose of every one is to drive prices to a high level, in a quick and expeditious manner (which is not synonymous to being economical).

Exchanges differ from auctions. A rudimentary form of exchange is just a meeting place for buyers and sellers to negotiate individual deals. But, as in the case of stock or commodity exchanges, it may also be a place where competing buyers and competing sellers enter a multiple negotiation through appointed brokers, who deal with each other in order to accomplish transactions for their customers. According to Cassady, though, "[e]xchanges really are not a different type of price-making arrangements: the simple exchange involves merely private negotiation between individual buyers and sellers, while the more complex exchange is based on competitive bidding by both buyers and sellers" [Cassady, 1967, 14]. "The stock market has been designated by some as a "double" auction because the exchange process is based on competition among sellers as well as among buyers" [1967, 13].⁸ But this seems a poor reason since it is true of all markets.

A two-good (one-market) "double auction" in a purely brokered market

It could be of some interest to attempt a representation of the working of this

⁸Walker [1990a, 660-3, esp.662] is very critical of the application of the notion of auction to this unfamiliar market scheme.

"double auction" mechanism in a 'perfectly' organized market. For the sake of simplicity, let us be confined to a purely brokered market, and moreover to a two-good, one-market case. (The objective here is to make sense of Walras' description of the Paris Government Bond Market. I paraphrase from Walras [Jaffé, ed., 1954, 84-6 and 87ff] with the guidance of Howitt [1973, 490].)

Let us assume a given price for a commodity. Those agents who have received orders to sell at this price or lower, will offer a certain amount for sale at such price. Conversely, those agents who have received orders to buy at this price or higher, will demand a certain amount for purchase at such price. If the amount proposed to purchase by an agent is matched by another agent's proposed amount to sell at the given price, a transaction takes place between these two brokers. Then, "[t]he terms of this trade are announced publicly, and the rest of the brokers attempt to carry out all the trades their clients wish to engage in at that rate of exchange" [Howitt, 1973, 490].

Consider, next, that either seller or buyer agents don't find in the market a counterpart for a proposed transaction. Suppose this is a broker formerly on the demand side who was unable to carry out all his desired trades at the assumed price. He will recalculate his present outstanding orders to purchase at a higher price (dropping his orders to buy at the previous transaction price, and it is further assumed that no new orders have been placed meanwhile), and will announce a certain proposed amount to purchase at the new higher price. If he finds a matching offer (at this new higher bid there may be now proposed supply), trade is consummated, otherwise a revision of the demand price will have to be next considered, and bidding is continued until he will be able to meet an agent with a counteroffer in the market.

If it were an agent formerly on the supply side, the opposite situation would

occur: he would propose a trade at a lower price in order to find a matching 'counterbid.'

This is a depiction of a "double auction," with the broker who found himself unable to fulfill his proposed transaction at the given price acting as an auctioneer: if he is on the supply side, he is facing competitive buyers and underbidding; if on the demand side, he is facing competitive sellers and outbidding. Of course, this is not necessarily so simple. Even for a market in which only brokers are assumed to operate, and therefore no bargaining is present on their own account, there is to begin with the question of establishing the starting price. We must introduce some explicit or implicit form of bargaining proper, before the market settles to some first transaction; this is obtained in some securities markets (new U. S. Treasury Bills, for instance) by means of "static double auction, relying on sealed bids and offers" [Wilson, 1992, 258]. But bargaining has an explicit role in most organized exchanges.⁹ For instance, in the case of exchanges where trade is conducted by specialists, bargaining is crucial for the working of the market: by trading for their own account, and changing his quotes of ask or bid prices, the specialist allows for a continuous market.

⁹In case an agent-buyer is bidding against a group of competitive suppliers, will there be any room and incentive on the part of each prospective agent-seller to bargain, or not? If there is, how to explain how it works?

In the case where specialists or dealer-brokers operate, these in fact, by quoting ask or bid prices on their own account, are clearly bargaining in the ongoing "double-auction" mechanism; in the New York Stock Exchange, for instance, bargaining is a continuous feature of the operation of specialists as market-makers.

In any case, in the NYSE, orders are of various types which contributes to the continuity of the operation of the market. The two main types of orders in the NYSE are unrestricted market orders (to be "...bid or offered on arrival at the trading post until executed"), or limit orders (to be "...executed at or better than the specified price...upon them, or not at all"); other types of orders are placed in organized markets, but these are quantitatively less important (cf. Osborne [1965, 90]; see also Demsetz [1968, esp.40]).

D. THICK-MARKETS

Thick-market, parametrical pricing, and price-taker are intertwined notions. Let us attempt a clarification.

As to the definition of a thick-market, let us quote from Clower [1994b, 3-4]:

...to stay within the Marshallian tradition we must suppose that trading in every market is sufficiently brisk, hence markets sufficiently thick, that the subjective price expectation assumptions defining competitive marketor behavior, viz.,

$$\partial p_j^e / \partial q_j \equiv 0, \quad \text{and} \quad \partial w_j^e / \partial n_j \equiv 0,$$

are not disconfirmed by experience. In short, marketors not only subjectively believe, but also objectively "see" their markets as "thick" or, more colorfully, as experientially continuous.

Notice that each marketor "...plans its output (prospective sales) in the expectation that its probable sale price, p_j^e , is independent of its output: $\partial p_j^e / \partial q_j \equiv 0$ ", and that "...each marketor ... in fixing the planned input of factor services n_j and the associated bid price w_j^e , proceeds on the competitive presumption that the probable wage rate required to attract and hold factors is independent of the planned quantity demanded: $\partial w_j^e / \partial n_j \equiv 0$."

The concept of thickness¹⁰ captures an essential aspect of parametric pricing, which being also a matter of perceived "continuity," means that the estimated price function of the seller is independent of sales and output (cf. Bushaw and Clower [1957,

¹⁰Impressionistic descriptions in the literature suggest that a thick-market is characterized by atomistic competition, high aggregate volume of trade, and high frequency of transactions, but there is no logical basis for any of this.

184]). For instance, in adjustment (disequilibrium) situations, the firm may be adjusting price, a function of the discrepancy between sales and output or of unplanned inventory holdings, and still take its sales estimates or pricing decision as parametric - or perceive market as thick, if its price function is perceived to be independent of planned sales at the new price.

Parametric pricing agrees with Pareto's view of free competition:¹¹ "Assume that all individuals follow [free competition] in their exchanges... That means that each of them accepts the market prices although in reality the latter are *indirectly* modified by the exchanges made by these individuals" (Pareto [1909/1927, 431];¹² cf. [1911, 86]; also see Allen [1932, 213] for a short, and slightly distorted mention to this); and "[a]ll the sellers (and buyers) of rentes [on the Paris Bourse] clearly modify the prices, but they modify them without previous design; it is not the purpose, but the effect of their actions" [116]. Pareto's view is that free competition "...corresponds to very numerous concrete facts" and "...includes a very large number of transactions among which are the majority or even all the transactions relating to household consumption" [115-6]. (It is interesting how this focus on the 'purpose' of actions of individuals led to a change in perspective in the concept of free competition from Walras to Pareto.)

¹¹Pareto distinguishes two types of attitudes of a trader in face of the market (Pareto uses the word "contract"). Type I is the case of free competition ("The determination of the market price does not depend on [the individual]"). Type II is the case of "[s]omeone who ... intends to modify the price" in order to which "...he compares mainly the positions which he reaches *via* different prices" [Pareto, 1909/1927, 114-5]; also "[a]ssume that individual *I* does not accept the prices as he finds them in the market, but endeavors to modify them, with a view to achieving a certain end. This case includes the one which is commonly called monopoly" [433]; moreover, Pareto distinguishes "...between an individual's *power* to exercise a monopoly, and the *fact* that the individual does exercise it." [438]

¹²Here Pareto adds this footnote: "As we have already remarked, this condition must never be forgotten. Its omission would make the proposition, of which it is an essential part, false. We often repeat certain things because they are constantly neglected, forgotten, and ignored by some persons who write about economic theory." [Pareto, 1909/1927, 431n]

Parametric prices have, however, a different meaning when referring to prices as data in the calculations of agents.¹³ A trader may be in a situation whereby the transaction he is entering leads to a change in price (through bargaining, or just a change of the posted price), and still take prices elsewhere in the market as given "in the interim." For this agent, other prices are given data, and in this sense prices are parameters.

The notion of price-taker is commonly associated with both parametric pricing, and price being a given (parameter), in contrast to the monopolist ("...parametric pricing is associated only with selling under conditions of pure competition in the existing economic literature" [Bushaw and Clower, 1957, 184-5]).¹⁴ The monopolist firm is supposed to be the only seller in the market, which brings two consequences: first, he faces a downward sloping demand curve, and, second, he has no given price to follow and has to pick the best price. Contrary to the competitive firm, its price is not a given (parameter). This distinction between price-maker and price-taker seems to me liable to some confusion, and this for two reasons:

- (1) Even though the monopolist doesn't receive a price signal from the market

¹³Burstein [1968, 25] writes: "...what I should view as the central ground, namely the distinction between the *objective* constraint posed by the vector p in idealized competitive markets and the *subjective* evaluation by 'monopolists' of their sales possibilities now and in the future." Every seller may be thought of meeting an objective vector of prices of relevance elsewhere in the economy, as well as facing a subjective sales curve. (See Burstein [1968, 135] on producers, both in states of competition and monopoly, being "...governed by the feasible-sales region..., a subjective notion leading to all-round monopoly pricing.")

Notice also: "Professor Hicks *does* point out 'false trading' leads to shifts in asset positions, parametric for $f(p)$, but the real problem is much more serious. In a *disequilibrium* economy *à la* Clower, or in a world of all-round monopoly, traders treat parameters of probability distributions of recognizable quantities as parameters for their decision-process." [Burstein, 1968, 25]

¹⁴Referring to Jevons' concept of competition, which "...was a part of his concept of a market," Stigler defends that "[t]he merging of the concepts of competition and the market was unfortunate. [...] A market may be perfect and monopolistic and imperfect and competitive" [Stigler, 1957, 244-5]. On this latter aspect, see Allen [1932, 209-10 and 214].

place as the competitive firm may be supposed to, similarly to the competitive firm its sales estimates or pricing may be parametric. The whole revenue curve is fixed by "impersonal forces"; thus "...there is no *a priori* reason why such behavior [parametric pricing] cannot occur in a one seller market since even in this case there may be fierce competition in a relevant sense among sellers in different but closely related markets " [Bushaw and Clower, 1957, 185].

(2) In every market (atomistic or "small numbers")¹⁵ every seller can be said to have an asking price.¹⁶ Perhaps it is set and changed by someone or something else - but it is still the price at which the seller stands ready to deal with the willing buyer. Here, the relevant distinction is not between competitive and monopolistic pricing but between brokered and decentralized markets. In organized brokered markets, transaction prices become a price signal contemporaneously issued and rendered available to traders. Therefore, in organized brokered markets, the seller has information about a price to ask so that his expectations are that he will be able to find a buyer at that price for a given quantity at his discretion. He will experience his market as thick for a broad range of quantities proposed for sale. On the other hand, in decentralized markets the seller will have no given price at which he could sustain the expectation to be able to dispose of (sell) any quantity he chooses to offer for sale; whatever his choice of an asking price, he has no guarantee that he will be able to contact willing buyers and sell the quantity

¹⁵Thickness is a general concept without specific reference to the characteristics or degree of market organization (brokered or non-brokered, competitive or monopolistic).

¹⁶Alchian and Allen's comments on how the "price-searcher" "sets" his price are of interest here. In a price-searcher market as defined in contrast to a price-taker market, regarding the "wealth-maximizing output and price program": "Whether sellers are described as using their "market power" to "set" prices or merely searching for the best (wealth maximizing) price in the market is all a matter of semantics. [...] All prices in all markets are administered in the sense that each person decides at what price he shall sell (in the light of market demand)." [Alchian and Allen, 1972, 344-5]

offered for sale.

Summing up, the distinction between price-taker and price-maker may be unwarranted. First because the sales curve is estimated, or perceived by the seller; and independently of the shape of the "real" demand curve, the seller may have no grounds (informational or experimental) to disconfirm that his is a thick-market. The standard (partial equilibrium) distinction between competitive and monopolistic (one-seller) markets provides no secure prediction regarding the estimation of the sales curve by the seller (standard theory deals only with "perceived" revenue functions).

Second, because in the case of decentralized markets we are at odds to make sense of taker and maker. In the case where prices are the object of previous negotiation, or bilateral bargaining, the distinction is meaningless. There is also the other possibility that a price is posted by the trader, more commonly an asking price by the seller; also in this case, the distinction is basically off the point. The reason is that such markets are better understood with sellers as quantity-takers: whatever the choice of price may be, with attention to market demand nonetheless, the seller has an asking price and will sell a minimal-size "lot" at discretion to any single buyer. The market may be perceived as thick or thin, but the seller is a quantity-taker.

Furthermore, the case of a decentralized "quantity-taker" market may be considered as thick if each trader "...plans its output (prospective sales) in the expectation that its probable sale price, p^e , is independent of its output" [Clower, 1994b, 3]. Which means that the quantity put up for sale is not expected to have effect on the price at which that quantity is expected to be sold. The expectation may be in error, and

in general will, unless the amount sold (or put up for sale) is 'infinitesimally' small.¹⁷ We can make sense of this belief¹⁸ by the seller as the best guess available to him in case of absence of a well defined relation between price and quantity/sales, given the difficulty to disentangle effects (viz. identification problem; lagged effects; informational costs; computational costs and feasibility).

The upshot of this note is that in thick markets expected transaction prices, regardless of being given or obtained by way of bargaining are thought of, by individual transactors, as being uninfluenced by the amount of planned sales.

¹⁷This relates to continuity of the demand curve (cf. Burstein [1968, Ch.6, esp.134ff]). Also, as quoted above: "Formally, the concept of "thickness" requires continuity (or "effective" continuity, somehow defined) of the marketer's sales function." [Clower, 1994b, 4n]

¹⁸As quoted above, in a thick market "...the subjective price expectation assumptions defining competitive marketer behavior ... are not disconfirmed by experience. In short, marketers not only subjectively believe, but also objectively "see" their markets as "thick" or, more colorfully, as experientially continuous." [Clower, 1994b, 4]

E. SEARCH MODELS OF TRADING

If we preclude individual traders from exchanging directly with a central market authority, we will have to envision individual traders as in need of inferring exchange opportunities. And if costs of searching for prospective transactors are in any sense considered, the expeditious meeting of transactors cannot be taken for granted. We will have to have traders looking for trading partners, or, in an extreme case, we may have to start with individual traders carrying out exchange as a do-it-yourself activity.

Let us start by considering a market 'setting' where the central determination of market equilibrium prices creates an allocation inefficiency in case we allow for the decentralization of exchange 'locations.' Meyer et al. [1992] discuss the coordination problem that stems from central pricing when trade of a single good occurs at two separate places. Let us embark towards the South Seas and imagine two islets. The authors define a market for fish in two islands (the only element of decentralization they introduce), where exchange takes place separately in each island between its "perfectly" competitive consumers and those fishermen who decide to sell in this island. Price in a numéraire commodity is set by auction.

Proceeding to suppose centralized market pricing by an 'auctioneer,' the authors then state that the announcement of an equilibrium price wouldn't be a sufficient condition for general market clearing, since fishermen would have no information which

island to supply,¹⁹ so that it would be a matter of chance that either of the markets clears at the announced price set. Thus, the conclusion is that "...traditional Walrasian models of general market clearing do not formalize and cannot analyze the allocation problem inherent in decentralized exchange" [Meyer et al., 1992, 295].

This problem of coordination of trade was raised by Peter Diamond, who proposed a search model with pairwise exchanges between individual traders. Peter Diamond's [1982a] barter model falls in this setting. This parable dispenses with the (neo)Walrasian clearing house but keeps central pricing; it assumes correct forecasts of future prices and rates of trading and production opportunities (the author is interested in steady state equilibria). In this island coconut market, the matching of traders is left to a search process but the ruling unitary rate of exchange is obviously known at all times by all traders. Prospective traders with a "coconut worth of purchasing power" search²⁰ for another transactor with a coconut on hand, given the respected taboo that no individual can consume what he himself has produced. When two transactors in possession of one unit of the coconut-good meet, exchange takes place.²¹ Pairwise matching of traders obeys a random process, and trade is bilateral (and costless²²).

¹⁹Without a centralized allocation authority, prices alone provide no information to any specific supplier concerning which island to supply" [Meyer et al., 1992, 295].

²⁰In such a search model, demand is made to depend on the distribution of stocks of inventories of others (meaning the proportion of others that hold a coconut, and are therefore employed in trading), as well as expectations about future production and trade opportunities (cf. Diamond [1987b, 368]).

²¹By the artifice of sticking to a single good, and still forcing trade, price is one by assumption; the problem of the determination of the equilibrium price is assumed out. On the other hand, this indivisibility assumption is thought of as a proxy of transaction costs, for "[t]echnically, lumpiness of transaction can play the same role as transaction costs by ruling out small entries into markets." [Diamond, 1987a, 82]

²²This model fails in an important aspect: costs are only considered on the supply side (production), let us say. No cost is attached to the demand side, strolling along the island with a coconut on hand searching for another trader is not costly: if time spent in this search process were costly in some meaningful way (for instance considering time preference in exchange explicitly, not only through the

Coordination problems arise because this trade technology is expected to exhibit increasing returns to scale in the aggregate (cf. Diamond [1984b, 2-6]). The idea (more of an unproved, or biased, conjecture) pushed through is that if more people are attempting to trade (i.e., with increased inventories for trade²³), each individual trader will find it easier to contact prospective transactors and this creates an externality. In addition, a positive feedback arises because easier trade (i.e., a greater stock of inventories for trade by others) increases the expected profitability of producing for inventory.²⁴ Thus, the parable goes that the trading externality can originate an inefficient production level, since a decreased number of buyers in the search process reduces the probability of a sale and, as a consequence, production activity is discouraged. "Moreover, this externality involves a positive feedback: increased production for inventory makes trades easier and easier trade makes production for inventory more profitable and therefore justifies its increase. This positive feedback with an externality implies the possibility of multiple equilibria" - in this barter model, one equilibrium dominates the others (Diamond [1984b, 5]; also Diamond [1987b, 368]).

In order to make sense of the search models as applied to barter exchange, a clarification is due and a possible confusion needs to be avoided. We need, first, to

production decision), an incentive would arise for some investment in information - only a step from the inclusion in the model of a trade specialist of the commission agent type [Hicks, 1976, 299].

²³In an economy where a trader is prevented of accumulating inventories, an increase in inventories is equivalent to an increase in the number of individuals employed in the trade activity.

²⁴The externality is introduced by making the rate of arrival of potential trading partners (b) a function of the fraction of the population employed in the trading process (e): $b(e)$. And the positive feedback is forced into the barter model [1982a] due to the consideration of a variable cost of production (or of a disutility of effort in production), and of making the "reservation" disutility a function of $b'(e)$ (with $b' > 0$) (cf. Diamond [1982a, 885-6]; and [1984, 5-6]). See Diamond [1984a, 3; and 1984b, 27] where the assumption of increasing returns is explicit; in order to model a barter-cum-(outside)money exchange economy the assumption is equally rather contrived, but may however be acceptable.

distinguish between the effect of an increase in the number of potential trading partners on search opportunities, and the "strategic interdependence" (how does this differ from non-strategic interdependence?) in the choice of search intensity of unmatched traders (cf. Mortensen [1982a, 234-5]). In "two-sided"²⁵ markets of the "the mating game" type [Mortensen, 1982a; 1982b], the solution of the repeated bilateral matching game is a Nash equilibrium²⁶ in search intensities (each agent's strategy is a choice of search intensity). In the barter models there is not such an ex ante choice of search intensity. Here search obeys a Poisson process where the rate of arrival of trading opportunities may be posited as constant (Kiyotaki and Wright [1993])²⁷; or as a function of the fraction of unmatched traders, where "...individuals think of b [the rate of arrival] as a parameter and do not recognize the relationship between b and the aggregate stock of inventories" [Diamond, 1984a, 10].

Peter Diamond [1982a] assumes that search opportunities increase with the increase in the number of unmatched traders: the arrival rate of potential trading partners (b) is a function of the fraction of the population employed in the trading process (e): $(b(e))$, with $b' > 0$. This is the result of complete absence of trading arrangements -

²⁵"...two sided matching markets. The term "two-sided" refers to the fact that agents in such markets belong, from the outset, to one of two disjoint sets - for example, firms and workers. This contrasts with commodity markets, in which the market price may determine whether an agent is a buyer or a seller." [Roth and Sotomayor, 1990, 1] But this is all confused: either in one or the other type of markets the behavior is similar if we are talking of decentralized/non-brokered exchange. Transaction costs in general prevent any individual from the possibility of choice of being a buyer or a seller; why this tendency of seeing the economic world under the lenses of brokered markets?

²⁶In these articles "...it is assumed that a meeting is concluded with an instantaneous agreement which divides the associated surplus in an arbitrary predetermined way (when the surplus is assumed to be divided equally, the division rule is, in fact, Nash's axiomatic bargaining solution." [Rubinstein and Wolinski, 1985, 1133; also 1149]

²⁷Kiyotaki and Wright [1993, 65n] assume a constant-returns-to-scale meeting technology by choosing a constant arrival rate of trading opportunities (see p.75, 19n).

ex ante a trader employed in exchange (holding a coconut) cannot be told apart from another trader hunting for coconuts. This creates an externality, and with it increasing returns in the trading technology. This is not the adequate formalization of exchange, to rely on complete anonymity in exchange. If we would assume that islanders can be spotted as traders, thus an increase in the number of traders would just mean an enlargement of the market, not a higher density in trading opportunities; and consequently an increase in the number of traders would imply a proportional increase in the total number of meetings. Such a trading technology creates no externality and doesn't present increasing returns to scale.²⁸

There is also possibly the confusion between a two-sided non-interchangeable market (a "bilateral" market like the labor market, or, in general, "the mating game") and a market where demand and supply go together (e.g. "one good" barter model). In the former case, there are two separate and fixed sets of traders, one of individuals on the demand side, another on the supply side. In the barter models, we have only one set of individuals on both sides (either on the demand or on the supply side) since every trade is both a sale and purchase for both traders.

In the former case, an increase in the number of people on the supply side

²⁸A model by Albin and Foley [1992] simulates 2-good decentralized exchange with informational or search costs, where bilateral bargaining takes place sequentially at non-Walrasian prices, and "boundedly rational" rules of interaction are used by traders. The authors associate their study with Diamond [1984b], and extend "technology specification" to Diamond's assumption of "...correct forecasts of future prices and rates of trading opportunities" [Albin and Foley, 1992, 49; quoting from Diamond, 1984b, 1-3]. This is the main focus of the study: traders use a "limited computational" algorithm with local interaction (parametric neighborhood size is assumed) in order to define communication and search intensities for ensuing rounds of trading. "It is interesting to conjecture that, with the local formulation we use, the unit cost of coordination does not rise with the size of the economy. In other words, for an economy of N agents sensitive to the costs of computation and organized in neighborhoods of radius r , the efficiency outcome is essentially ruled by the radius parameter and is independent of N " [50]. Diamond's model could be seen as relying on "fully rational strategies" of individual traders who "...maintain a model of the state of the N -agent economy" [ibid.], save for the fact that agents don't anticipate the externality effect.

expectedly makes it easier for any employer to find a match, which means an increase in the density of traders on the other side of the market; and in this two-sided market the externality could possibly be present. Moreover, this interdependence gives rise to the definition of search intensities as a strategy in a bargaining game. In the case of barter, however, an increase in the number of people on the supply side exactly mirrors the increase in the number of people on the demand side - they are the same people. There is no increase of the density of trading opportunities faced by any trader, and consequently there is no externality in the trading technology. Therefore, a linear matching technology ("...the possibility that a match will form in a short time interval is independent of the number of unmatched agents" [Mortensen, 1982a, 235]), which in a two-sided market originates strong externalities, need not do so in case of exchange with interchangeable agents (simultaneously on the demand and supply side) if only traders participate in the meeting process. Thus, the modelling transposition from the labor to the barter models is unwarranted, contrary to Diamond's [1984b, 5] wishful thinking.

F. MARKET-MAKERS, AND PRICE AND QUANTITY ADJUSTMENTS

I am not going to explain the presence of a trade specialist from first principles, starting with individuals in a foggy island searching for trading partners. I am going to make a big jump over the difficulties posed by the coincidence of timing and wants in barter trading, and presume them "abated" to start with by the presence of specialist traders. These will be our market-makers, operating in an ongoing exchange environment where media of exchange either exist, or are 'made' by means of credit facilities by these trade specialists. All the problems raised in the body of the dissertation are deemed resolved. The concentration will be directed towards understanding price versus quantity as the variables of choice by a (decentralized) market-maker.

The first goal is to characterize a market-maker. One side of the question regards which functions turn a seller or a supplier into a market-maker; the other is logically interrelated and regards the characteristics of demand that favor such market arrangement. Transaction costs will be considered next, and how the seller can reduce costs of information and shopping on the demand side by incurring in selling-costs. Finally, an attempt will be made at the scope for adjustment of price and quantity of the 'ongoing' market-maker.

(i) The functions of the market-maker

It has been hinted above that the basic functions played by the trade specialist are stockholding and price formation, and that in substance these belong together.²⁹

First, and attempting to make it general, every seller can be said to have an *asking price*. Perhaps it is set and changed by someone or something else - but it is still the price at which the seller stands ready to deal with the willing buyer (cf. Demsetz [1968]). Alchian and Allen's comments on how the "price-searcher" "sets" his price are of interest here (a price-searcher market as defined in contrast to a price-taker market, regarding the "wealth-maximizing *output and price program*"):

"Whether sellers are described as using their "market power" to "set" prices or merely searching for the best (wealth maximizing) price in the market is all a matter of semantics. [...] *All prices in all markets are administered in the sense that each person decides at what price he shall sell (in the light of market demand)*" [Alchian and Allen, 1972, 344-5].

Second, using stocks of inventories as a 'shock absorber' may be thought of as

²⁹Because I will be quoting from Hicks [1989] on the pricing of manufactures, let us introduce his producers as market organizers. Hicks brings out a market organization based on the producers as the market-makers in his *A Market Theory of Money*. In the case of those goods for which the conditions do not apply that favor the emergence of what he calls speculative markets, Hicks proposes a production system with primary producers, manufactures and consumers and two sorts of intermediaries in between, primary and secondary trades. Regarding the latter he conceives of an economy where "the product, as soon as it was completed, would be sold to secondary merchants (wholesalers) at a price which was mainly determined by trading among the wholesalers themselves" [20]. Then Hicks raises the possibility that at occasions decisions to introduce new products had been made; when this happens "[o]ur entrepreneur has to devise a new product, make arrangements for manufacturing it, and also make arrangements to get it sold".

And Hicks goes on: "For since the product is specialized, no other manufacturer producing anything exactly like it, any merchant to whom he sells it directly must be dependent on him for supply. The merchant must thus be acting, in this part of his business, as a manufacturer's agent. So we have here ... manufacturing and selling come in substance under the same control.

There were two functions which we were attributing to our secondary merchants and their markets: stockholding and price-formation. As we saw, they are nearly allied; so it is here. The selling department is able to set a selling price and make it effective by holding stocks. That is to say, it can do its own buffering; and can do it relatively easily, since producing and stockholding have been brought so close together. So the price that is set can be chosen, as a matter of policy" [24].

a possible feature of any trade specialist. But it is quite a different thing to make the trade specialist's capacity to trade dependent on the holding of stocks;³⁰ however as a simplifying assumption,³¹ we will stick to inventories from here on (in fact, the quantity controls the seller can rely on are of two kinds, a stock of inventories or a backlog of orders). Besides, stockholding is anyway a poor instrument for making effective the price that was 'set'.

Alchian and Allen establish a relationship between stockholding and pricing quite neatly:

"...it will pay sellers to maintain an inventory of buffer stocks and predictable prices for consumers to meet the transient fluctuations in daily market demands rather than to try to produce to order instantly as buyers are faced with transient, unpredictable price changes. Inventories stabilize prices and make the momentary supply schedule a horizontal line at the selling price, out to the limit of the existing inventory." [Alchian and Allen, 1972, 338]

Third, if the trade specialist is said to provide a 'ready market' for prospective buyers, i.e., to offer a good for sale and post an asking price, the next function we may consider is that of providing information, and well as incurring "...the main 'selling costs' of putting his good into his customers' hands" [Friedman, 1989, 391],³² i.e., to deal with the marketing function (the organization of the logistics of trade). This is central to understand the workings of competition in a non-brokered market.

³⁰This is an illusion, except in a two-way market for a good handled by numerous secondary sellers - e.g. auto parts, grain.

³¹Cases exist also where either the period of time the inventories are held or the time taken to satisfy orders are negligible. These cases shouldn't possibly be discarded not only on logical but also on empirical grounds; for instance, most services seem to fall in this category.

³²Our market-maker can be so defined as in Daniel Friedman [1989, 381]: "Markets can be usefully distinguished by asking two questions: (a) who sets prices? (b) who handles the logistics of exchange? By a *producers' market*, I mean a market for which the brief answer to each question is 'the producers of the good'; that is, each producer publicly announces his current price and incurs the main 'selling costs' of putting his good into his customers' hands."

Competition among sellers cannot be perceived as ruled by the blind forces of the market place (this does not happen in any case), clearly it can only be assessed as carried out with more or less ability by market-makers. The situation is that readiness to sell, and the organization of the logistics of trade come both now under the responsibility of the seller/market-maker.

Goods and services are offered for sale to buyers who, before the purchase are supposed to have had access to information about the good, by any means, in a more or less purposive or costly way. Information on price, quality, location, availability of inventory or risk of stockouts, payment arrangements, quality of service, or whichever aspects concern the buyer (and for the differentiated good, the buyer may have to appraise it, and possibly to learn to use it).

If this is so, scope exists for advertisement and salesmanship.³³ And buyers may also depend on varied services that increase the information, convenience, reliability, or dependability of the good or service. Firms incur costs with a view to "...cement customer relations by many methods. They may appeal to customers on the basis of quality, transportation arrangements, credit terms, and speed and reliability of delivery" [Okun, 1981, 150]. These are meaningful to suppliers of services that are not easily evaluated by shopping, and sellers of differentiated items where the price tag offers only

³³Hicks [1989, 24-5], in a setting where producers are constructed as having taken over the merchanting function, emphasizes this aspect: since the producer is now "...selling, at least at the end of the chain, to a consumer who is not an expert", "...it is now the producer himself who has to take responsibility for the quality, and usefulness of what he is offering."

And Hicks goes on: "That is why at this point there is a function for advertisement, which is basically a promise about the character of the thing being sold. It is a promise like that which is given by the retailer, when he opens his shop. In each case it is given by a professional to a non-expert, so it quite ordinarily needs to do more than just give information. The attention of the customer has to be attracted, by a smart shop-front in the one case, by pretty pictures and suchlike in the other. But he has then to be persuaded on the strength of the information given to him, including a promise, explicit or implicit, that the information is correct."

limited information to prospective buyers. But information problems are pervasive also in the case of homogeneous goods ("...the amount of dispersion of asking prices of sellers ... is ubiquitous even for homogeneous goods" [Stigler, 1961, 213]³⁴). Okun stresses also "...the importance of dependability and reliability to *professional* buyers, even to those procuring physically *homogeneous* products"; some industries of this type have established "...a rather unusual two-price, two-market system" [151].³⁵

(ii) Set-up costs

Now let us give a closer look to the demand side of the picture.³⁶ Customers incur search costs and transaction costs each time they search and they trade (cf. Alchian

³⁴"That they do not wholly vanish (in a given market) is due simply to the fact that no combination of advertising media reaches all potential buyers within the available time." [Stigler, 1961, 223]

³⁵Daniel Friedman also recognizes that this may matter even for the homogeneous good case ("technically the simplest and cleanest"): "A producer who can deliver the goods and receive payment at a time, place and manner that is convenient to the customer will attract more orders. But this service is costly to provide, since it requires such things as friendly sales representatives, local sales outlets, toll-free telephone lines, lunch invitations, flexible credit terms, etc." [Friedman, 1989, 382]

³⁶Alchian stresses the role of information and transaction costs throughout his work. "We can now identify a "perfect" market - one in which all potential bids and offers are known at zero cost to every other person, and in which contract enforcement costs are zero. Characteristics of every good need to be known perfectly at zero cost. A "perfect" market would imply a "perfect" world in which all costs of production, even of "exchanges," were zero. It is curious that while we economists never formalize our analysis on the basis of an analytical ideal of a perfect world (in the sense of costless production) we have postulated costless *information* as a formal ideal for analysis. Why?" [Alchian, 1969, 42n].

Also of interest: "Because most of the formal economic models of competition, exchange, and equilibrium have ignored ignorance and lack of costless full and perfect information, many institutions of our economic system, institutions that are productive in creating knowledge more cheaply than otherwise, have been erroneously treated as parasitic appendages. The explanation of use of money, expertise with dealing in a good as a middleman specialist with a trademark or brandname, reputability or goodwill, along with advertising of one's wares (and even unemployment) is often misunderstood. All these can be derived from the same information cost factors that give rise to use of an intermediary medium of exchange." [Alchian, 1977, 123]

[1969]; Hirshleifer [1973]). These costs have a lump-sum component, that is to say, are largely independent of the size of the transaction. To the extent that these are set-up costs, customers are better off not collecting all the information which might be relevant for their shopping decisions: information about the variety and quality of all the goods which compete for the satisfaction of a customer's need, and information about price and service by their suppliers.

Now we may ask: Can the supplier help alleviate these information costs? Can he do it more efficiently than would the customer alone be able to gather that information?

Customers' search about products, the identification of the sellers and their prices and conditions is costly. Sellers can help. They can advertise so as to bring that information onto customers' horizon and thereby reduce their set-up costs, either by replacing search and shopping altogether³⁷ or by funnelling it into a smaller set of alternatives. Sellers may advertise their presence in the market, their good(s) or varieties and, in some situations, their prices and conditions. But as to prices, as Stigler [1961, 216] has suggested, an alternative to advertising is "...the development of specialized

³⁷This may be a critical effect. For instance, Daniel Friedman [1989] on "producers' markets" may have failed in this respect. Let us see how. By producers' markets Daniel Friedman means that "...each producer publicly announces his current price and incurs the main 'selling costs' of putting his good into his customers' hands." The producer sets prices and handles the logistics of exchange. Also "...the selling costs incurred by producers are primarily regarded as a means of reducing the cost to customers of searching for the best price and attribute mix" [381-2]. In his set-up, customers are meant to search for prices, but selling costs by firms provide customers with sufficient information to generate an "efficient" price searching by customers. Since the diffusion process of information has enabled convergence to a single price in equilibrium search doesn't occur.

The question is that the demand characteristics that may be conducive to generate such type of market organization are only implicitly formalized; price uncertainty vanishes in equilibrium, and thus Friedman's model "...has essentially assumed away search costs" [383n]. This model is therefore lacking a seemingly basic element to explain the role of the producers as the market-makers. In any case, the author shows that in his *non-cooperative* model of producers' markets for a *homogeneous* good, "...sticky, asymmetric price responses can arise in the absence of search costs or collusion" [383].

traders whose chief service, indeed, is implicitly to provide a meeting place for potential buyers and sellers" (as an example, mention is made to dealers in used cars). And as both prices and conditions are concerned, market-makers may replace advertising for a less conspicuous activity, that of "...price stability as an information economizing device" [Alchian, 1969, 50; also 37-9, 49]. As Okun puts it, firms may pledge continuity of past offers and foster the customer's belief that he can rely on past information as a guide to present and future offerings: "The firm wants to promote a reliance on intertemporal comparison shopping."³⁸ Or more at length:

Customers are valuable to sellers because of their potential for repeat business ... The firm comes to recognize its ability to discourage customers from shopping elsewhere by convincing them of the continuity of the firm's policy on pricing, services, and the like. It knows that its customers have indicated by their previous purchases that they regarded the firm's offers as satisfactory. It can encourage them to return to buy, or at least to shop, by pledging continuity of that offer, ensuring them that past experience will be a reliable guide to present and future offerings... Customers are attracted by continuity because it helps to minimize shopping costs. They know the terms of the previous supplier's offer without shopping if they can count on its continuance; but they must shop to determine the offer of unfamiliar sellers. That information is available, but it can be obtained only at a cost ... If the status quo is satisfactory, the expected value of the information about alternatives is low [Okun, 1981, 141-2].

Alchian has stressed the importance of recognition and assessment costs as inducing the provision of services by the seller, as for instance the assurance of quality by "...specialist, expert middlemen of high reputability" (Alchian [1977, 111; also 122];

³⁸The upshot is well put forth by Hicks: "The price is one aspect of the offer that is made; there are some characteristics of other aspects which are shared by it. The chief is that it must not be changed arbitrarily, at a moment's notice. Arbitrary changes 'unsettle' the consumer. He may be taking time to decide to buy; so if, when he finally decides, he finds the price has risen against him, his confidence is lost, and the seller's reputation is damaged. And it can happen that there is a similar obstacle to price-reductions; they cast suspicion on the quality of the product, they suggest that something is wrong. Thus the diversified market had a tendency to be what I have called a *fixprice* market, meaning not that prices do not change, but that there is a force which makes for stabilization, operated not by independent speculators, but by the producer himself." [Hicks, 1989, 25]

cf. Clower and Howitt [1993b, 7n and 8]). Moreover, an obverse informational economy will be generated that will contribute to cement customer relations: by means of continuity, the seller will be able to gather information on the buyer - on his dependability, could we say - and this will make it feasible (less costly) for him to offer convenient payment arrangements, or trade credit, in a regular fashion (cf. Clower and Howitt [1994, 8-9]; see also 12).³⁹

This implicit commitment to avoid disappointing the customer is a feature of our market-maker's behavior radically different from sticky prices brought about by menu-costs. Menu-costs relate to the administrative costs of altering offers about price and conditions, and providing customers with that information.⁴⁰ Menu-costs generate price stickiness not as an informational device but quite the opposite, as an interruption in the regular (and efficient) flow of information the market would otherwise display.

Distinctly, the customer market appeals to a process of acquisition and diffusion of information (which can hardly be made sense of in a static context). That pledge needs to be repeated in order to keep recurrent purchases and feed the flow of customers. The search diffusion process may drive customers away but it may as well bring some shoppers in. Customers are attracted by continuity (of offers) because they save on set-

³⁹"Most transactions in a monetary economy are not spot but credit transactions involving explicit contracts in which one side promises to deliver goods or services." Clower and Howitt [1994, 9] add: "This is perhaps most evident in trades involving labor services, where some degree of future commitment is almost always involved on both sides. But it also involves markets for consumer goods, where retail organizations implicitly offer their customers future delivery on demand, and in markets for industrial goods, where long-term supply relationships are crucial to the smooth operation of manufacturing process."

⁴⁰The inclusion of menu-costs, as of any transactions costs, enriches the standard model of price adjustment and may generate interesting predictions. Yet, menu-costs lack any logical basis in the market, apart from the strict "...direct administrative costs to the producer (seller)" [Barro, 1972, 21]. And empirically it hasn't been easy to justify. Estimates of such costs, even by users, suggest that they are too slight to be of significance. Overall, menu-costs may be less promising than who use them tend to suppose.

up costs of information gathering. They create attachments to sellers, which encourage recurrent purchases. But, as attachments are built and information about the broad market becomes obsolete, information may require updating.⁴¹

Some fortuitous (though costly) search may interrupt or break attachments, or an intermittent assessment of the competitors' advertisements may bring relevant information thereto. These take place so that the customer can check whether he is doing the right thing by sticking to his supplier. But he may have a surprise: in that case he may have to look for some broader picture of the marketplace by continuing his information gathering for a while. Let us simplify by considering that, on the aggregate, this gives origin to a diffusion process of uncertain consequences, and spread over time. (The more the seller responds the quicker the information of the customer wears out, and the more his need to update it increases. All this leads towards continuity and the status quo.)

As we saw, the firm invests in several ways to further a clientele. A clientele constitutes capital to the seller, and its rate of obsolescence mirrors, in great measure, the liveliness of competition in the market; this meaning that an interruption or a failure of these investments on maintaining a clientele may seriously undermine the seller's position in the market, despite other strengths of the seller - technical or otherwise - being untouched. This is a picture of the seller as competing to keep its pool of customers and to attract new shoppers away from other sellers. The seller is attempting

⁴¹Okun, on concentrating his attention on the demand side, loses some sight of the competitive drive of producers; he overlooks the role of selling costs in breaking attachments of customers to individual sellers, at least fortuitously. Okun pays only cursory attention to the possibility of customers to initiate some shopping around at intermittent points in time, under the belief that some price moves may have happened meanwhile.

both not to disappoint repeat customers as well as to encourage disaffected or disappointed shoppers of others to stick with him.

But the same forces that allow for this continuity increase the payoff of an 'entrepreneur' who ventures an incursion into the competitors' field. A small start may gather moment by means of the diffusion process, although at the cost of a high uncertainty. Settled sellers may take time to notice raiders but when they recognize them, it may be too late to recover lost ground. This raider is a market-maker. In an uncertain world, he competes away the settled sellers. Since the signals these receive are mostly particular to their individual business, some time elapses before they realize some innovation has occurred in the market(place). The same forces that have worked to sustain settled suppliers are called for to explain the process by which new suppliers get settled.

Both the settled seller and the raider are market-makers; the point is just made clearer for the case of the latter. Both have appealed to a clientele and devised ways to sustain a continued flow of customers, but in neither of them that is guaranteed. In either of them this has to be made, on a continued way.

We have introduced the market-maker, presented economic incentives for his emergence, and discussed his functions in general, but little was said about his decisions or behavior, as adjustments of price and quantity are concerned. This is attempted in the next section, in the course of a story constructed on evolutionary lines whereby, by playing his functions, the seller gets to adapt to this environment (no attention will be paid to the broader questions of his actions with a view to transform it for his benefit).

(ii) The scope for price and quantity adjustments

Having as a departing point Arrow's question of the scope for decision on price versus quantity, let us now handle the forces that underlie price adjustment in a non-brokered market. Our market has no device to produce a central price signal. Sellers are left to their own perception of their market and there is no price signal (currently available in the market). The seller is not a price-taker but, in Alchian and Allen's terminology, he is a price-searcher.⁴² Before we address the question of which are the signals a market-maker can observe on a regular basis so as to direct his price and output decisions, we have better attempt first to identify those choices available to him that are previous to our thought experiment.

We have an ongoing market and concentrate our attention on a supplier in that market; he is representative as far as observable signals and decision processes are concerned. The supplier's characteristics are a given; both decisions and market responses have interplayed in shaping our market-maker as an ongoing concern. To begin with, it is assumed that the supplier has made some previous decision regarding technology and capacity in their material, human and organizational components. It has been incurring selling costs (viz. advertising, salesmanship) and possibly investing in research and development, in order to consolidate a clientele. It has evolved through time and today it has a given *capacity* that is used to bring a good to the market and get it sold. We assume that the costs of altering capacity (increasing or decreasing) are far

⁴²"...the price to the price-searcher is not determined for him as if by some impersonal market mechanism. Instead he must search out the optimal (wealth-maximizing) price. And, not knowing the demand schedule exactly, he will have to resort to retrial-and-error search processes. No demand-and-supply intersection principle determines his price, although the demand (and ... the costs of production) plays a crucial role in determining his prices." [Alchian and Allen, 1972, 118]

too great for it to be a short-run consideration; this is Marshall's short-run.⁴³ As a consequence the supplier uses given capital, and incurs fixed costs.

Fixed costs are important here. Under the assumption of a given capacity, their total amount can be known ex-ante, and thus 'present' fixed costs anticipate incoming ones fairly well. As a consequence, a distinction is called for: total fixed costs, and the variations of fixed costs per unit of output impinge on pricing quite differently. The fact that the *variations* of fixed costs per unit of output can only play little part in price adjustment⁴⁴ has no bearing whatsoever on the *level* at which the price shall be (cf. Marshall [1920, 376-7, 458-9]). The seller will post an asking price that is expected to permit its viability, and if fixed costs are not expected to be recovered this will be quite improbable.

Thus, the supplier has a given technology and capacity; and, for the ensuing construction, costs are assumed to be only partially adjustable (cf. Marshall [1920, 374-7]; Wiles [1961, esp.8]; also Clark [1923, 72ff and 90ff]). Capacity is here defined as the rate of output above which marginal cost starts gradually increasing, so that output ultimately faces a cost barrier. The definition is independent of the shape and slope of marginal costs at rates of output below or at the capacity level; in any case a clear upward turn may be expected. Capacity is not an objective limit, physical or otherwise. It is a cost barrier: the seller can only extend its rate of supply in the short-run to a

⁴³"The supply of specialized skill and ability, of suitable machinery and other capital, and of the appropriate organization has not time to be fully adapted to demand; but the producers have to adjust their supply to their supply to the demand as best as they can with the appliances already at their disposal" [Marshall, 1920, 313].

⁴⁴"Overhead costs ... are assumed by definition constant under partial adjustment, and to have merely to be borne by more or fewer units of output. But since output is never known in advance, as it is determined by the market, these variations in fixed costs or overheads per unit of output, although well known, play little part in price determination." [Wiles, 1961, 51]

limited degree, and at the expense of rising marginal costs. This is a consequence of both limited substitutability (law of diminishing returns), and of high transaction costs in order to adjust (some) factors of production in the short-run. Planned capacity is thus the level of output above which "partial adaptation" is expected to lead to a marked increase in marginal cost. (Of the vast literature on cost and supply curves, a noteworthy reference is Joel Dean [1976], where his statistical studies of short and long-run cost curves are compiled, and a generalization is attempted in the Introduction.) The question of the shape of the long-run cost curve is here sidestepped for the two reasons: one is that in order to discuss quantity and price adjustment in the short-run we need not presume (precise) static equilibrium, the other that the effect of variations in capacity on long-run costs may be presumed harder to anticipate than the effect of short-run partial adaptation, so that the firm may be thought of as carrying out short-run adaptations under the belief that these don't affect long-run average costs (cf. Andrews and Brunner [1975, 26]).

To begin with our thought experiment, let us assume that in the near past the environment has been quite smooth - in the sense that, sales having evolved according to some tendency, the seller has achieved to adjust. For instance, he has adjusted the level of operations, or price, so that he could maintain positive holdings of inventories at virtually all points in time (cf. Clower and Leijonhufvud [1975, 184]).

Again, the market-maker has no precise current guidance on the price to post; as we have seen, he is a price-searcher. Nonetheless, under the circumstances price can be expected to inhere in a certain range. I raise a twofold hypothesis. The first one is that a range of *survival prices* exists: this is a range of prices that could have been

posted during the foregoing period (characterized by a stable environment), and that would have permitted the seller to survive. As regards the future, it is a range within which a price may be posted and survival expected. The second hypothesis is that this price range is on the neighborhood of what we may call - despite the confused connotations - *normal* or *full-cost*,⁴⁵ along the lines discussed by Andrews and Brunner [1975, 25-8], Andrews [1949, Ch.5], and Wiles [1961, Ch.5]. This hypothesis is very weak. Its main use here is that it allows to circumvent the question of defining any precise asking price as a starting point of analysis (and therefore eschew discussion of the static equilibrium of the 'firm'). We only need to make the not unreasonable assumption that the observed posted price is within this set.⁴⁶

The market-maker aims at survival and uses rules of decision⁴⁷ that have

⁴⁵Notice that full-cost here is not a decision rule (nor in any sense a norm, like standard cost is for accounting purposes). Let us quote from Alchian: "These constructed rules of behavior should be distinguished from 'rules' which, in effect, do no more than define the objective being sought. Confusion between objectives which motivate one and rules of behavior are commonplace. For example, "full-cost" pricing is a "rule" that one cannot really follow. He can try to, but whether he succeeds or fails in his objective of survival is not controllable by following the "rule of full-cost pricing." If he fails in this objective, he must, of necessity, fail to have followed the "rule." The situation is parallel to trying to control the speed of a car by simply setting by hand the indicator on the speedometer." [Alchian, 1950, 218n]

⁴⁶An avowedly not very reasonable 'solution' to the problem is raised by Wiles, but he drops it in favor of the full-cost *principle*: "How, then, would profit maximization look in this sector? The firm would set a price which would result in an output such that (price-a.c.) \times output was maximized. By *logical necessity* at this price and output true m.r. = true m.c.(partial adjustment), where 'true' refers to the (wisely) chosen length of 'run'. Just because practical thought is not conducted in marginal terms we may not conclude that analytical thought is precluded from applying them.

Moreover all the lines would be thick bands, ... owing to uncertainty, and profits would be maximized *ex ante* by a price and output combination anywhere within the lozenge-shaped continuum [at the top of the figure]. The upper lozenge gives, to be exact, an upper and a lower limit to the profit-maximizing price, and accordingly to the exact price chosen a range of probable outputs. Of course one of these prices and one of these outputs gives the *maximum-maximorum* of profits, but uncertainty prevents us from knowing which it is. Nor, if we did happen to hit on precisely that price, would we necessarily find ourselves asked to sell just that output." [Wiles, 1961, 59]

⁴⁷For an assessment of this point, as well as to clarify concepts, let us quote from Alchian: "The pursuit of profits, and not some hypothetical undefinable situation, is the relevant objective whose *fulfilment* is rewarded with survival. Unfortunately, even this proximate objective is too high. Neither perfect knowledge of the past nor complete awareness of the current state of the arts gives sufficient foresight to

conformed to that goal.⁴⁸ The objective of survival drives current decisions insofar as their repercussion is expected to extend into the future; and in the case uncertainty and the resulting response by the firm of valuing continuity of offers (cf. Okun [1981]) is allowed for, current decisions might even restrict the range of possible decisions in the future (in a way that is not present in brokered exchange).

The hypotheses are then that current decisions of the seller are influenced by its anticipation of survival potential; and besides, that the price rule must have led its asking price to lie within a range in the neighborhood of full-cost.

Now the seller has survived for some period of time characterized by a smooth environment, and we assume that the seller anticipates the period ahead to be as smooth as during the foregoing period - whatever its duration has been; the only relevant aspect is that the seller has adjusted to the environment in such a way that he has no motives today to change his rules of action since they have proved viable.⁴⁹

This survival range doesn't set limits on observable prices, though; we don't constrain our market-maker to survive. He may be representative as far as signals

indicate profitable action. Even for this more restricted objective, the pervasive effects of uncertainty prevent the ascertainment of actions which are supposed to be optimal in achieving profits. Now the consequence of this is that modes of behavior replace optimum equilibrium conditions as guiding rules of action." [Alchian, 1950, 218]

⁴⁸Adam Smith's view of competition "...as rivalry, as a process" was, according to Coase [1977, 318] "quite robust" and this he documents at length. Of interest to us here is the following: contrasting the price of monopoly with the price of free competition, Smith writes: "The natural price, or the price of free competition, on the contrary, is the lowest which can be taken, not upon every occasion, indeed, but for any considerable time together. [...] [The price of free competition] is the lowest which the sellers can commonly afford to take, and at the same time continue their business." [A. Smith, 1776, Bk.I, Ch.7, 27]

⁴⁹We should notice that survival can only be ascertained ex post. Survival is an ex post fact, and decision rules towards that goal are only good given environmental stability (cf. Alchian [1950, esp.213 and 219]).

observed and decision processes are concerned but fail to survive due to cost or demand factors not adequately dealt with. There is not such a thing as survival decision rules.⁵⁰ Survival is only defined ex post; and, although the seller's decision rules are meant to have a survival goal, they do not guarantee survival (cf. Alchian [1950]).

At any point in time, asking prices could be observed within a broader range. It is now presumed that the upper bound is only governed by 'particular' demand and this will in general be dominated by competitive forces (cf. Andrews and Brunner [1975, 24]). (Entry considerations, especially cross-entry or vertical integration, may play a role but these are beyond my concern, since they would call forth long-run considerations involving expectations of competitors whether a certain price level by the seller is temporary or permanent, of expectations of prices in the competitors' field, as well as of anticipation of responses by competitors.) Conversely, the lower bound has a cost anchor; we can assume that the producer has no incentive to post an asking price below the marginal cost level of current output (cf. Marshall [1920, 374-5]). The supplier is assumed to be capable of approximating current marginal costs, which is not too unreasonable since a large fraction of these costs - except for "the user cost of machinery, and also the risk that fast running entails of bottlenecks and breakdowns" [Wiles, 1961, 51] - can be computed without the need to maintain expectations about future performance.

Now, let us assume our seller's supply at a certain rate, somehow adjusted to the

⁵⁰Although drawn in another context, Winter's view is relevant: "Let us suppose, tentatively, that what corresponds to a genotype in the theory of the firm is a rule of action or strategy. What the environment operates on, and rewards and punishes, is not the rule but the actions evoked from the rule by variables in the environment itself. This is a major objection to any claim that economic natural selection tends to produce situations in which the surviving rules are optimizing ones" [Winter, 1975, 97].

current rate of sales; besides, the price rule for the *level* of price has proved viable.⁵¹

We observe the asking price and let time flow. What rate of sales can be expected? Expected sales volume obeys to some distribution affected by a rate of departures and a rate of arrivals, which are due to a diffusion process. The technology of information gathering by customers involves search (either triggered by surprise, or initiated on a random fashion be it fortuitous or intermittent) as well as advertising or other selling costs (these reduce the amount of search and thereby change the rate of arrivals); conversely, the rate of departures depends also on these activities by competitors. However, the basic element in this process is that the expected rate of "stickers" (Hicks [1954]) is large because on a smooth environment information depreciates slowly. Sellers help reduce the information costs of customers by means of adjusting prices and conditions only parsimoniously, this allowing customers to maintain the belief that information collected in the recent past is valid in the near future. Inertia is to be expected in the circumstances.

Moreover, the seller has not perfect information about current prices by competitors as well as about their selling costs (and all they stand for). The seller has limited information about the current state of demand in his broader or in the aggregate market; and it takes him some time to recognize new cost advantages of actual competitors as well as the presence of new sources of competition.⁵² In a decentralized market the seller faces a complex inference problem (an additional complication is that several factors affecting the parameters of the current distributions are only possibly

⁵¹Viable rules (as to the decision variables we are concerned with, price and rate of supply) are those that permit the firm to sustain the anticipation of survival.

⁵²We may consider entry to be open in the sense of Andrews [1964] - cross-entry competition as he names it, which is quite reasonable in the case of a market composed of multi-product suppliers.

known with delay and/or at a high cost).

We might possibly conceive of the seller as sustaining the belief that he faces a stochastic revenue function that is downward sloping.⁵³ The relevant question in the circumstances is whether it compensates the seller to experiment with the market in order to know better or whether experiments⁵⁴ might be conducive to produce information that could be reliably extrapolated into the future. To begin with, the adjustment of prices will interfere with the customers' constructed beliefs about the market conditions and may set off a wave of search activity of uncertain results; a rise in price might expectedly increase the rate of departures, and a reduction in price would expectedly increase the rate of 'stickers', although at a risk of 'unsettling' the customers. But these evolutions will be spread over some future period of time, so that two conclusions ensue: first, experiments to estimate demand would require that price be kept constant for a period of time for the full effects to be observable; second, no standstill in competition can be assumed in the meantime. Experiments take presumably more time than that over

⁵³The following reflection by Wiles seems appropriate, even though he has it all mixed up: "...the genuine marginal revenue, which is marginal to the demand curve, is not known. Moreover even if they were known the true m.r. and demand curves would not be thin lines; for there is a great deal of tolerance among buyers of heterogeneous products to small differences in price, so that each output can in fact be disposed of at all prices within a range. The demand curve, then, is not a line but a band; but in any case no one knows where the band runs" [Wiles, 1961, 47].

For one, the last sentence is trivially inconsequential; where the band runs doesn't matter if "...each output can in fact be disposed of at all prices within a range." All that matters is that current output can be expected to be disposed of at the current price.

⁵⁴Considering a market in which consumers get price quotes for purely informational purposes and continually search for bargains, the supplier may find the determination of the demand function an impossible task.

Rothschild and Yaari analyzed a model in which suppliers face a dilemma. The answer to 'What price to charge to increase knowledge about the demand function?' is likely to be different to the answer to 'What price to charge to maximize expected profits?'. Their conclusion is that it doesn't pay for the firms to be curious and the optimal strategy does not entail knowing their demand function with certainty. Following the optimal strategy, the firm will, in the course of its history, with positive probability charge the wrong price infinitely often and the correct price only a finite number of times. If there are many firms, price variability will persist (cf. description of results of Rothschild and Yaari in Rothschild [1973, 1299-301]).

which the *ceteris paribus* assumption can be supported.

In order to carry the argument forward, let us assume that the seller doesn't expect experiments with the market to produce a well defined relation between price and quantity demanded; or, if such is envisioned, that the expected net gain of the experiments is of uncertain sign. (This is not at all a trivial assumption, and for completeness it needs further discussion. In any case, our presumption is that the argument wouldn't be radically affected, otherwise.⁵⁵)

So, given his asking price the seller's only expectation about the rate of sales is that it will oscillate erratically around his "existing goodwill" (cf. Andrews and Brunner [1975, 25]). The seller has created a ready market and will sell what the market will take. Thus, given the seller's current asking price, the relation between price and quantity demanded defines a sales curve: "...for naturally the setting and sticking to a price creates an infinitely elastic *sales* curve while it lasts. The sales curve is of course by no means a demand curve" [Wiles, 1961, 47]. Wiles is close to the point but this is a little metaphysical. Contrarily, Alchian and Allen [1972] are closer to concreteness: they give a material reason for a 'momentary horizontal supply schedule,' as well as a limit, and this is existing inventory.

Now let us allow for a surprise. The seller begins realizing that the rate of sales must be increasing since inventories are being depleted faster than expected, and this tendency becomes more clear as time passes. Our construction implies that the firm will wait and see; the problem is for how long and to what extent?

⁵⁵For a possible case where the monopolist's demand curve is uncertain and where "...if price rather than quantity is the firm's choice variable ... no experimentation occurs", see Mirman, Samuelson and Urbano [1989, 26].

First, sales will be satisfied drawing on inventories, and no change in price is considered yet. An interesting proposition is made by Alchian and Allen:

...prices in price-searchers' markets are not "less adaptive" to changed market conditions than are prices in price-takers' markets. Because of inventory availability, price-searchers will provide amounts wanted by demanders during transient fluctuations without having to change price. This stability is not a reflection of price rigidity or power of seller to control price. It reflects instead the greater ability to provide price predictability by use of price-searchers' inventories. [1972, 338]

But this buffer may be short-lived. Most significantly, however, this change in inventories *signals* some adjustment is required. Before long, in order to maintain an appropriate level of inventories, the supplier may have to adjust *quantity offered* and/or its *asking price*.

Under the actual circumstances the producer can be expected to have been operating at a level of supply around capacity (given that we have allowed for the producer to adjust to the previously 'stable' environment). If this is so, an apparently sustained higher rate of sales can be satisfied by increasing supplies in order to restore and sustain the stock of inventories. The rate of supplies is geared to the level of inventories. The degree to which this margin extends is limited by capacity; that is to say, depending on the rate of increase of marginal costs, these will eventually attain the level of the asking price, so that extending output above such level is not satisfactory (unless for rather temporary episodes, given the eventual benefits accrued to the seller from continuity of offers).

Thus, the producer will try to accommodate that apparently increased rate of sales by adjusting the rate of output in order to keep inventory levels at an appropriate level. The case may be, however, that marginal costs are so pushed up that the extension of

supply above that level is not sustainable, given present capacity and despite all partial adjustments envisioned and implemented⁵⁶ (for a list of possible measures to extend output under partial adjustment, see Wiles [1961, 51-2]). Before the seller is assured that the new tendency in sales is not temporary and reaches the decision of investing in increased capacity (which we assume is not feasible for the short-run), he may raise the possibility of increasing its posted price with a view to stabilizing the level of inventories at an appropriate level. (Now the operation of the quantity control of the trade specialist has to be worked out, possibly along the lines drawn out by F. Owen Irvine [1981]; see also Thore, Billström and Johanson [1954], and Thore and Billström [1954].) Irvine [1981] builds a model where the price adjustment policy is a "short-run inventory-based pricing policy." He follows a suggestion from Clower and Leijonhufvud ([1975, 184; as in Irvine [1981, 247-8]) that middlemen firms would play a critical role in coordinating trade: such firms would vary their prices "...with a view to maintaining average quantities traded at levels that will ensure positive holding of traded commodities at virtually every point in time."

The converse observation of an increased unsold stock of inventories will bring about an adjustment process of similar characteristics but opposite direction. It seems harder to tackle, however, as far as the decision to adjust price is concerned; this question of devising a reasonable control mechanism for price reductions requires further examination. In what concerns an increase in price, marginal costs would provide a justification, but for a price reduction the role of marginal costs is harder to justify. In

⁵⁶We might presume that some of these adjustments hadn't been fully anticipated and only discovered under the pressure of the actual circumstances, so that the notion of ex ante marginal costs will have to be slightly discounted as a precise guide for decision.

any case, even for price increases, the upward bend of the short-run marginal cost curve may be of limited implication for pricing by the individual seller in a competitive market since it may not affect competitors (cf. Andrews and Brunner [1975, 27-8]), but this is beyond the scope of this exploratory note (the anticipation of responses by competitors, and the possible increase of capacity would enter the picture). For the moment, let us stick to inventories as the only relevant variable of control, and let us end up this note by quoting from Clower's *The Fingers of the Invisible Hand*, where the relation between price adjustment and inventories is discussed:

Over short intervals of time, there is no need for quantities purchased to equal quantities sold. Differences between commodity inflows and outflows to any shop can be buffered in the short run by variations in inventories. If the shopkeeper attempts to increase sales volume by offering lower prices to customers, he will sooner or later run out of stocks or find himself forced to pay a higher price to his suppliers. Conversely, if he attempts to increase his inventory by offering higher prices to suppliers, he will sooner or later be swamped with unsold stocks or he will be forced to offer lower prices to buyers. [...]

The adjustment of prices by shopkeepers in response to variations in inventories might be less prompt and smooth than the preceding remarks suggest. No shopkeeper can discriminate in the short run between variations in net sales that are transient and changes in net sales that are permanent, much less link particular variations with particular causes. An ongoing economy is subject to many random and inexplicable shocks. The representative shopkeeper's ultimate actions should be much the same regardless of the source of such variations. If, on average, inventories are declining, he will sooner or later raise both his selling price and buying price. If inventories are increasing, he will sooner or later lower both his selling and buying price. We should not expect unanticipated variations in inventories to be accompanied by immediate price changes. Lacking knowledge about the factors responsible for variations in inventories, we should expect the typical shopkeeper to follow a policy of wait and see - which is to say price changes will lag behind changes in inventories and will take place sporadically and by finite jumps. [...]

In a common sense way, we may thus say that prices are governed by "demand and supply"; but to say (or to insinuate) that current prices and price movements correspond at all closely to currently observed conditions ... would be a mistake. [Clower, 1994a, 10, 11 and 12]

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